Proceedings for the Workshop of IMPRS for Astronomy and Astrophysics Braunfels, Hesse, September 14-17, 2009

Workshop of IMPRS for Astronomy and Astrophysics took place at r at Fuerstenhoff hotel in Braunfels, Hesse. A very specific scientific program which was meant to strengthen the team work has been followed. In Particular, teams of 2 to 3 students invented a topic from three broad fields:

1. Stellar Astrophysics (code: SA)

2. Galactic Astrophysics (code: GA)

3. Extragalactic Astrophysics and Cosmology (code: EG)

Each such team then presented the selected topic by splitting the work over the team members. Each member approached the common topic by contributing, either of:

1. Review-Introduction

- 2. Milestone Discoveries
- 3. Black-board problem solution

Each talk will have available 30-40 minutes hence each team will have 1.5 hours. Each Session was chaired by the last speaker of the previous session.

Day 1:

September 14, 2009

Session 1: Stellar Astrophysics

Chair: E. Angelakis

Rainer Rolffs Energy Production in Stars and Elsewhere

Alex Kreplin Circumstellar disks around young stellar objects

Marion Wienen Overview of star formation

Session 2: Extragalactic Astrophysics and Cosmology

Chair: W. Wienen

Filomena Volino Introduction to General Relativity

Er Xinzhong Cosmology without General Relativity

Sibylle Anderl Space and time in the philosophy of Kant

Day 2:

September 15, 2009

Session 3: Extragalactic Astrophysics and Cosmology

Chair: S. Anderl

Chin-Shin Chang Active Galaxies

Rusen Lu Active Galaxies

Marios Karouzos Active Galaxies

Session 4: Extragalactic Astrophysics and Cosmology

Chair: M. Karouzos

Jiannis Nestoras Gamma-Ray Bursts

Frank Schinzel Gamma-Ray Bursts

Day 3:

September 16, 2009

Session 5: Galctic Astrophysics

Chair: J. Nestoras

Xuyang Gao Galactic Plane Surveys

Fangchun Liu Chemistry in Star Forming Regions

Fujun Du Chemistry in Star Forming Regions

Session 6: Extragalactic Astrophysics and Cosmology

Chair: F. Liu

Brenda Miranda

Ocejo Sunyaev Zel'dovich effect

Xun Shi Sunyaev Zel'dovich effect

Felipe Navarrete Sunyaev Zel'dovich effect





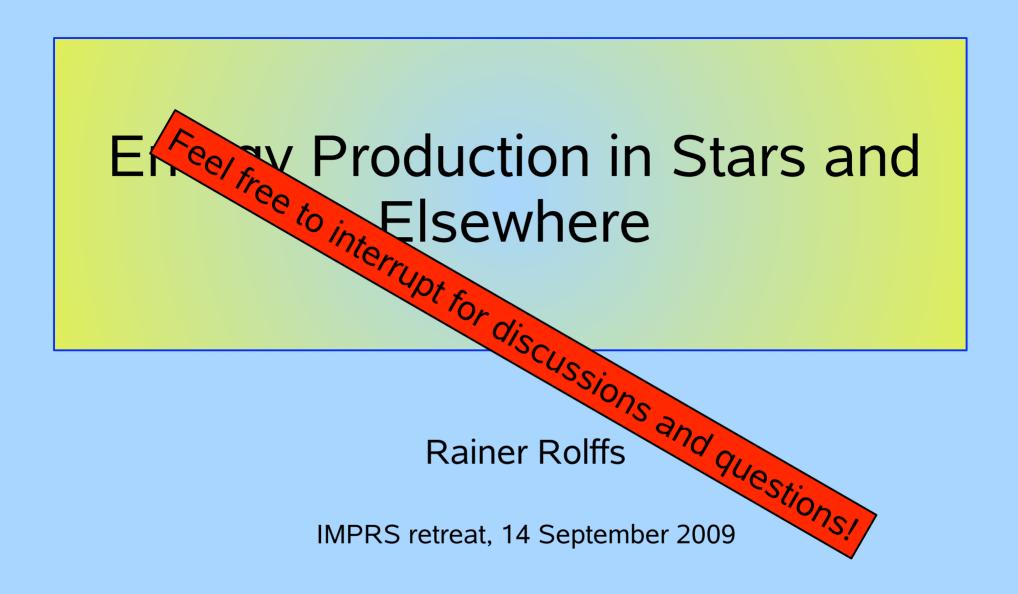


Energy Production in Stars and Elsewhere

Rainer Rolffs

IMPRS retreat, 14 September 2009

International Max Planck Research School (IMPRS) for Astronomy and Astrophysics at the Max Planck Institute for Radio Astronomy in Bonn and the Universities of Bonn and Cologne



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No Outline...

... to keep the story suspenseful and enthralling

... ok, a glance:

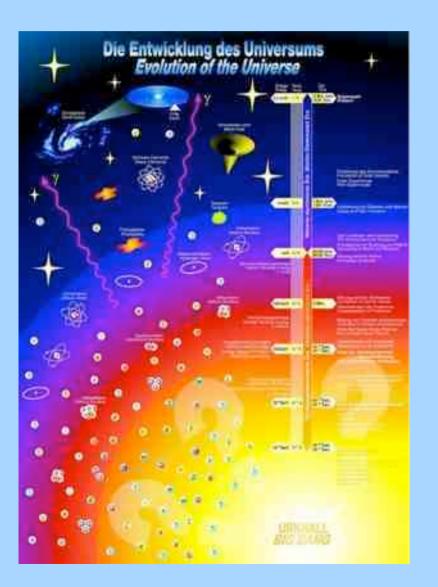
there will be huge adventures of our tiny hero, who will travel from cold, lonely outer space to the fervent heat of inner stars.... will he be able to escape from that hell?

Maybe he will even visit us here in Braunfels.

And there will be exciting calculations and enormous numbers (hey, we're scientists!)

Once Upon A Time...

Once Upon A Time...

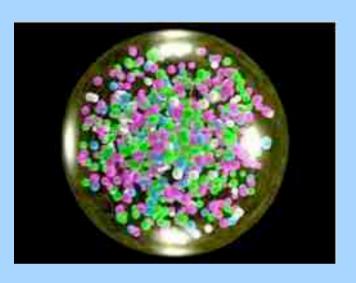


- beginning of space and time?
- energy conserved?
- what is powering inflation and expansion?

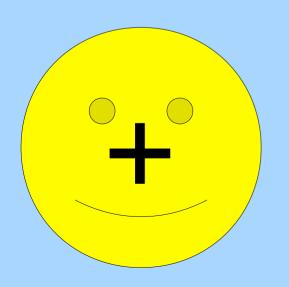
Energy is *produced* in the Big Bang and stored in matter, light, expansion field. After that, it is only *transformed*.

The Second Law of Thermodynamics leads to a dispersal of energy.

The Birth of Proty



A millisecond after the BB, Proty condenses out of the quark-gluon plasma, switching between neutron and proton.



After 1 second, he decides to be a proton.

His rest mass is $m_p = 1.67262158$ (-27) kg, his size about (-15) m.

His kinetic energy is around (-3) m_p , but with time he loses it to these nasty photons which stretch out.

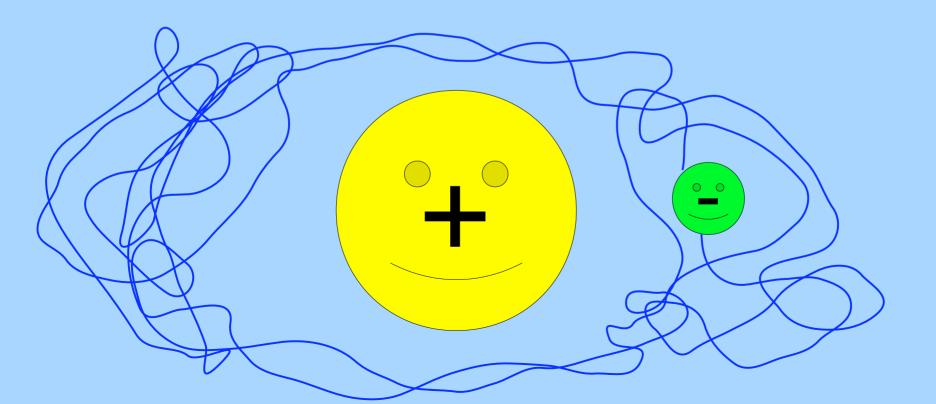


Finding Elly

He is attracting electrons, but these nasty photons don't let them stay together.

After some (5) years and a kinetic energy of only 3(-10) m_p (3000 K), the photons have lost enough energy that he finally finds Elly.

He doesn't care that she is exactly like all other electrons.



Density Rises Again

More and more other atoms collide with them, even two at almost the same time – now Proty is part of molecular hydrogen!

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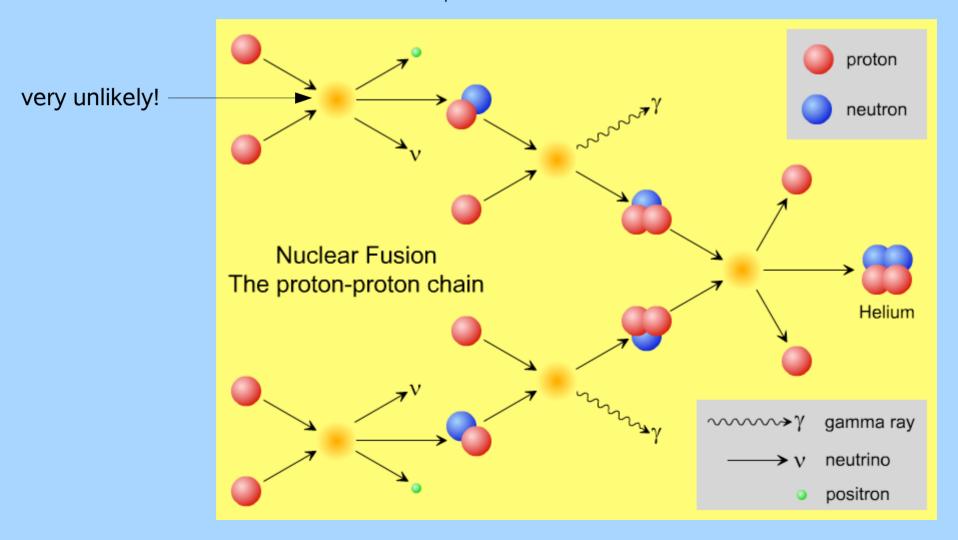
It gains kinetic energy. The collisions become so hard that it's ionized again.

Where is that energy coming from?

It's Getting Crowded

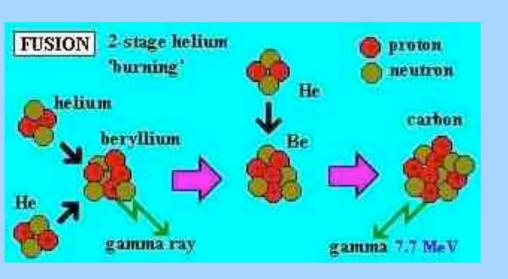
Proty does not want the other protons to get so close – but what can he do except for the electric repulsion?

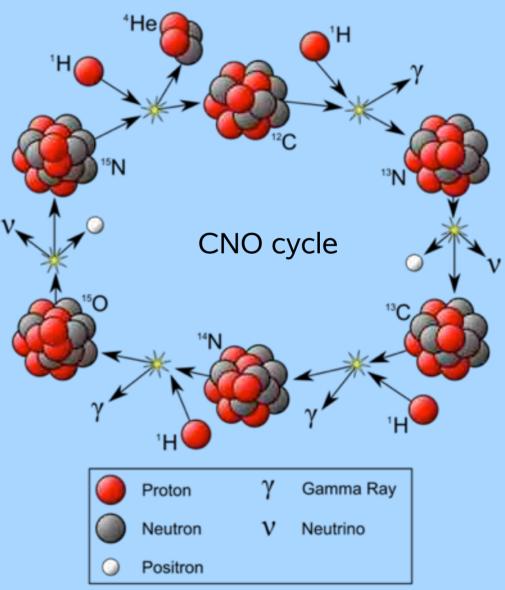
His kinetic energy reaches (-6) m_p – puh, all those collisions...

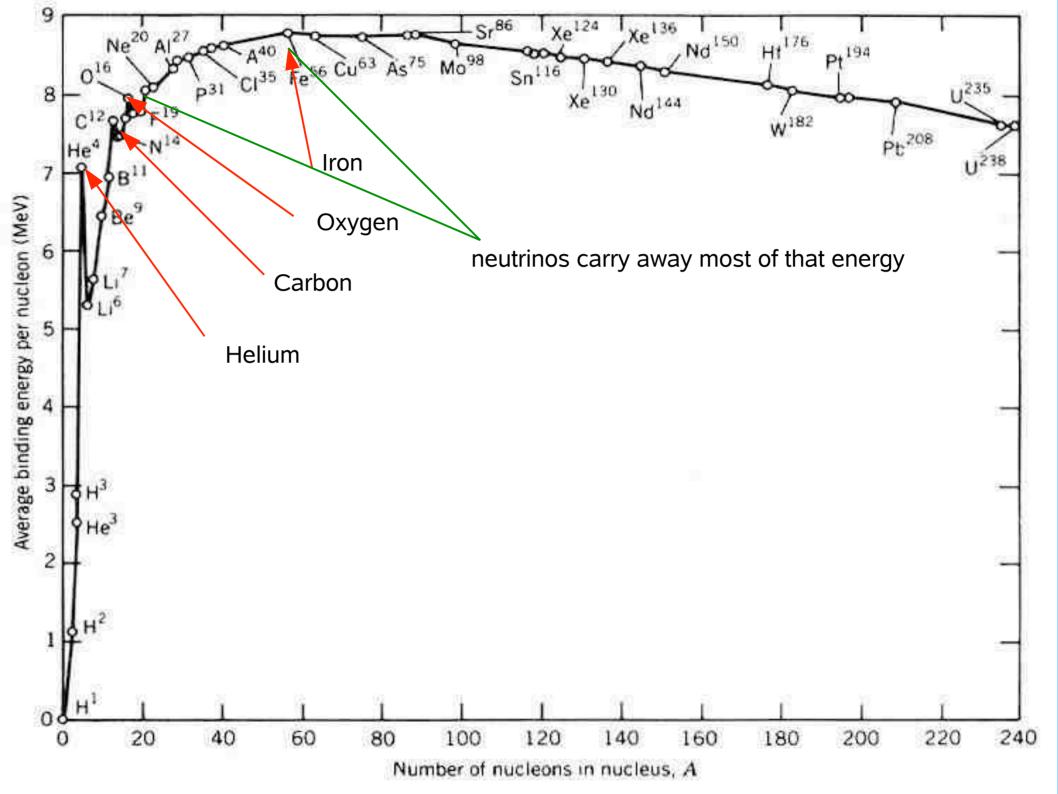


New Neighbors

Proty is not used to such close vicinity – but at least he's still a proton! Now even more neighbors are arriving.







Escape From Hell

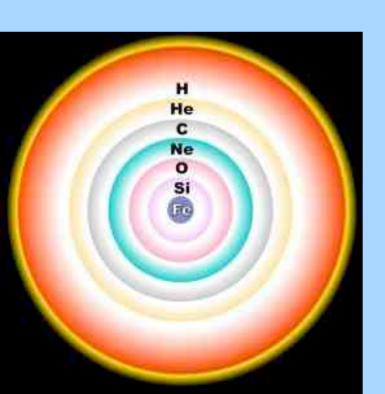
Trapped in such a strong gravitational potential, how would he ever get out of hell?

Escape From Hell

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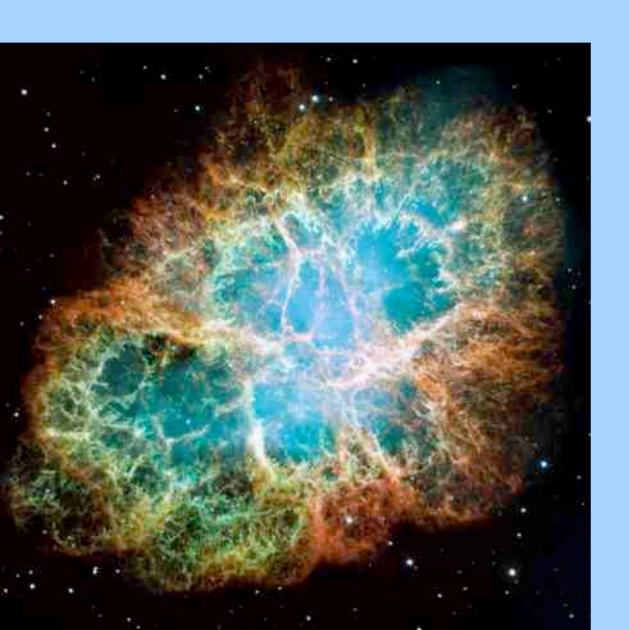
Ironically, the answer is again... gravity!

The iron core collapses when it's too heavy, a small fraction of the energy released disrupts the rest of the star - SUPERNOVA!!!





From Uranium to Helium

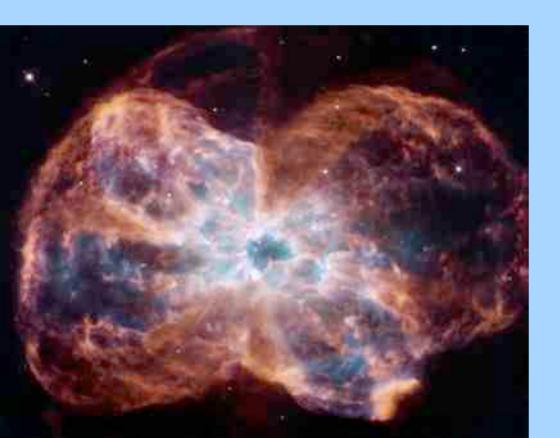


After that really explosive event, Proty finds himself in Uranium. As he doesn't feel comfortable with so many others (232), he leaves the nucleus with his nearest neighbors: α -decay

They calm down and find electrons, and help to cool their surroundings by collisional excitation and radiative de-excitation.

From SNR to PN

It's getting denser and cooler... now again hotter, he's ionized and ...right back in hell!



Well, it's not too bad in a carbon nucleus, escpecially now in the star's envelope. The shell burning expands it and... Proty's carbon is illuminated by a White Dwarf.

Again? - No, Earth!!!

This time he has enough angular momentum to prevent the hell, instead he's going to paradise – with a bit of patience though



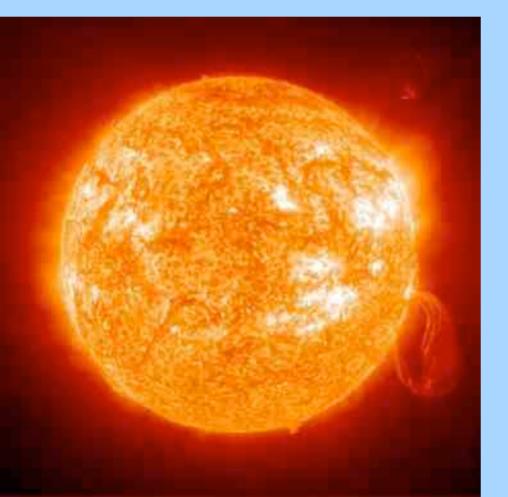
Proty is incorporated by a plant using photosynthesis. It stores around 5(-3) of the incoming radiation as biomass.

But then a volcano erupts – he is buried for a long time.

Why Does the Sun Shine?

In the meantime, a certain species of animals develop. They start to talk and discuss this question.

The solar luminosity is 3.846(26) W



Reason Time Scale [years]

God makes it shine As long as He wants

Burning Coal 2(3)

Heat from formation 3(7)

Contracting Radius prop. 1/Time

Radioactivity 1(10)

Hydrogen Fusion 1(11)

Since 1919, fusion idea developed by Perrin, Eddington, Bethe and many more

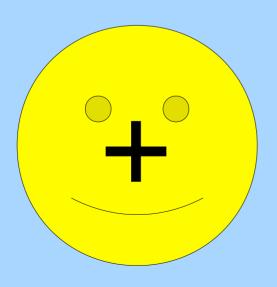
Where Is Proty Now?

They also grub out Proty's ancient plant and bring him into the atmosphere again. In fact, 80 % of mankind's energy use relies on fossil fuels, causing an energy and climate crisis.

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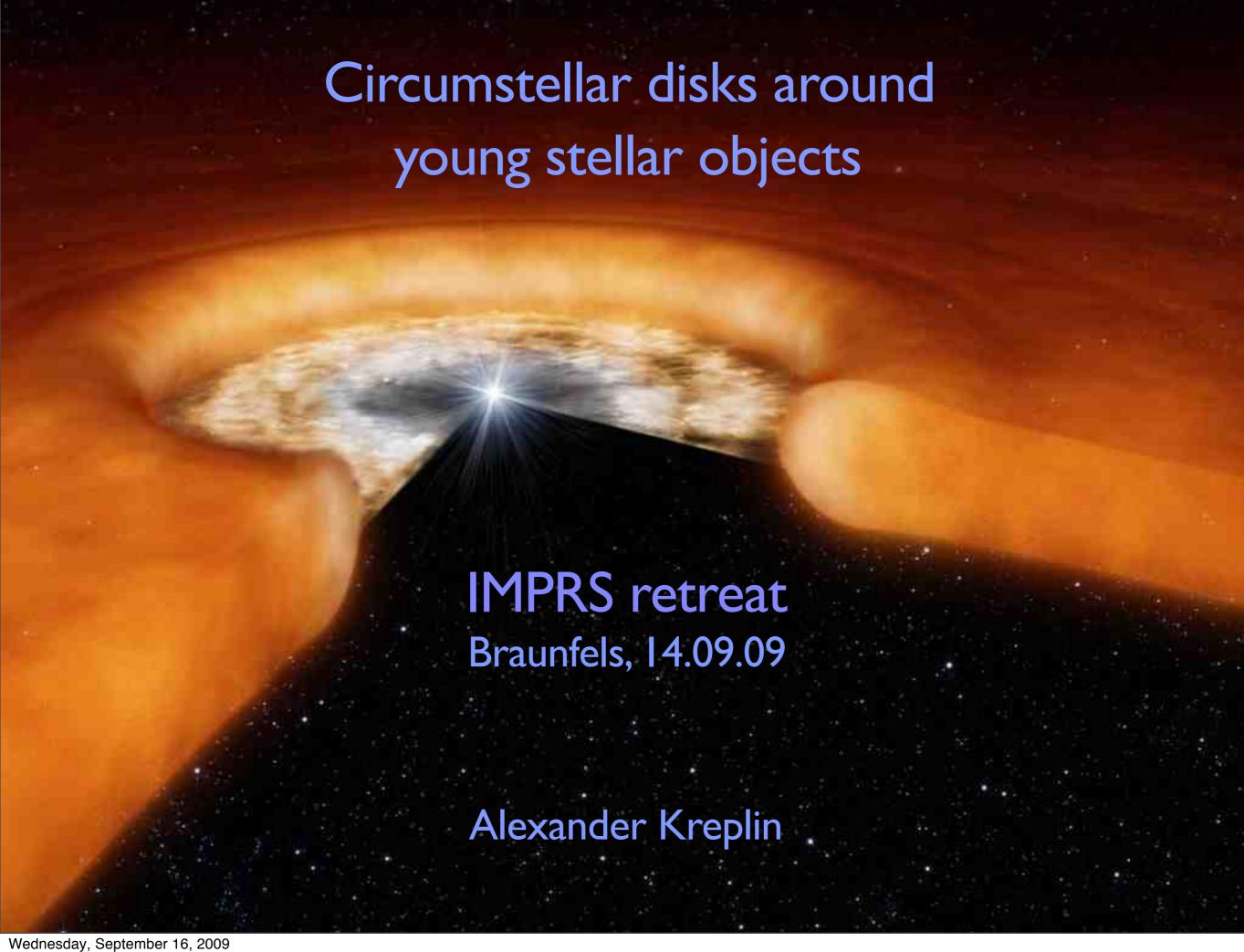
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Proty is respired by a tomatoe plant; maybe one of us ate him a few weeks ago and he is now dust in this room.

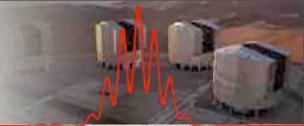


What will be Proty's future?

More adventures to come until his death in a Black Hole!

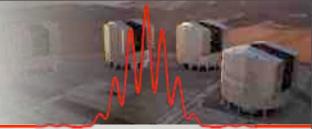


Outline



- Overview: circumstellar disks
- Disk models
- The inner rim
- Observational techniques: V921 Sco
- Future Instruments
- Summary

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Evolution of young stellar objects

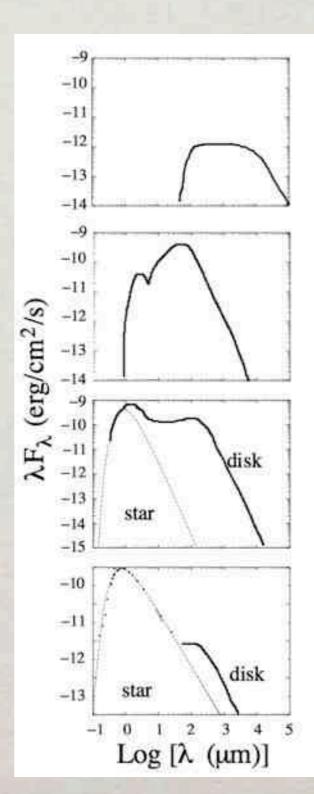
- Classification scheme of YSO's (Lada 1987)
 - Class 0: only submm-emission which indicates a deep embedded object
 - → Class I: steep positive spectral slope due to the presence of large amounts of circumstellar dust
 - Class II: negative spectral slope indicates less dust than class I sources
 - Class III: the weak mid- and near-infrared excess emission indicates little or no circumstellar dust

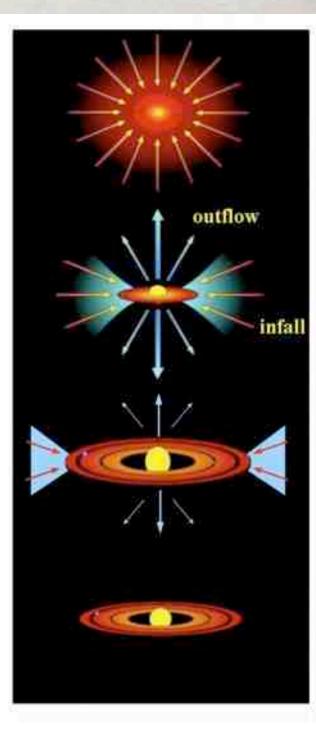
Class 0

Class I

Class II

Class III

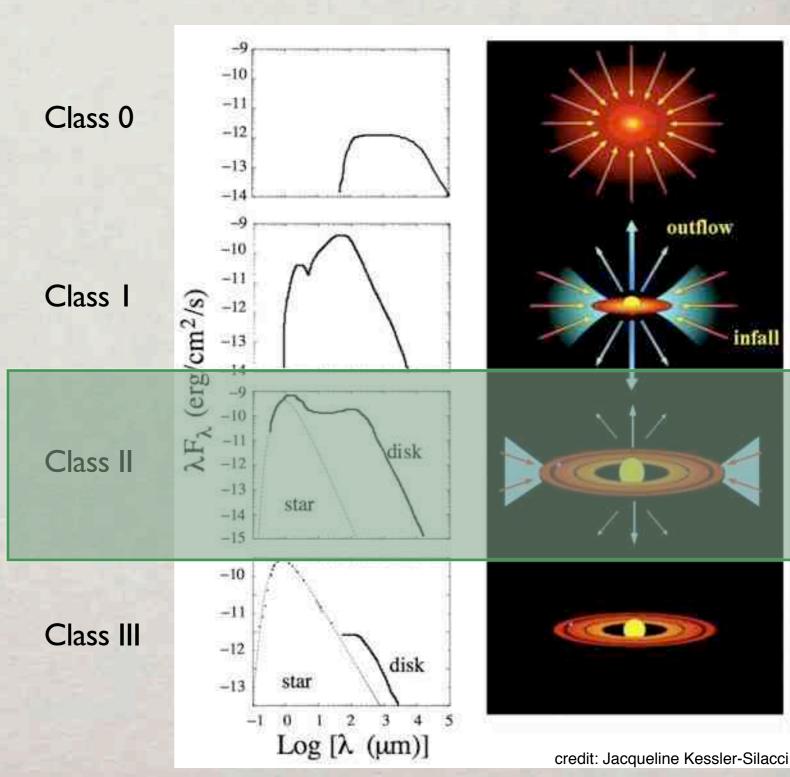


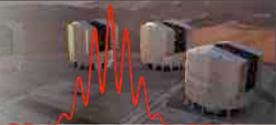


credit: Jacqueline Kessler-Silacci

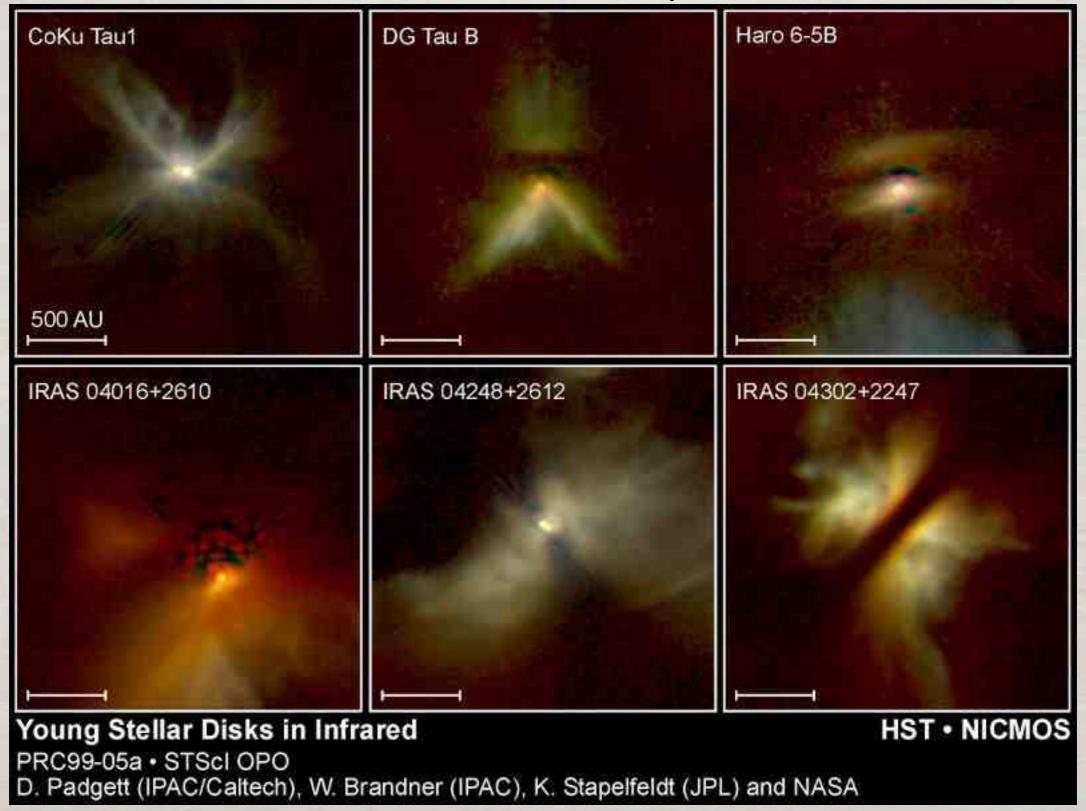
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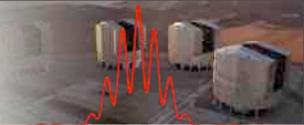
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Circumstellar disks are visually detected

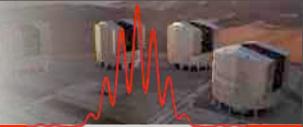


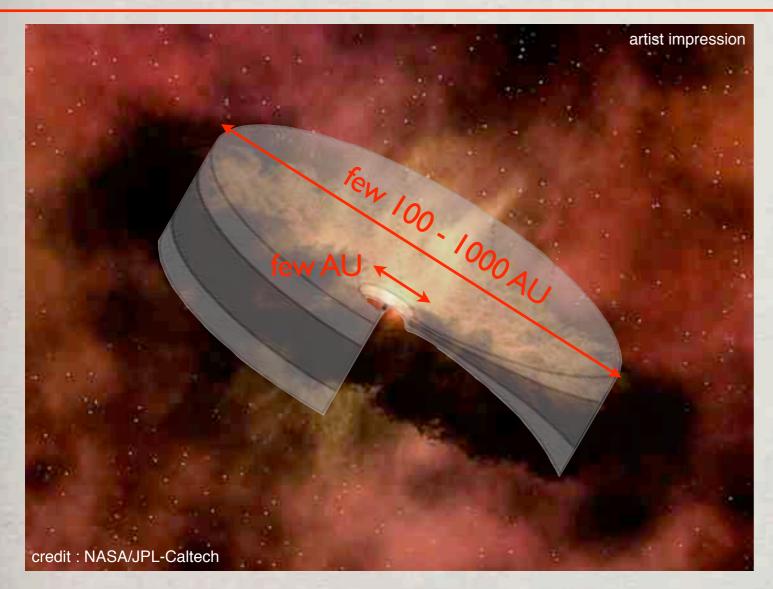




- Protostar is surrounded by a circumstellar dust and gas disk
- disks also detected in the case of intermediate-mass stars (Millan-Gabet 2000)
- Since the nearest star forming regions are about 140 pc away, high angular resolution is required ($IAU \approx 7$ mas)
- Interferometry

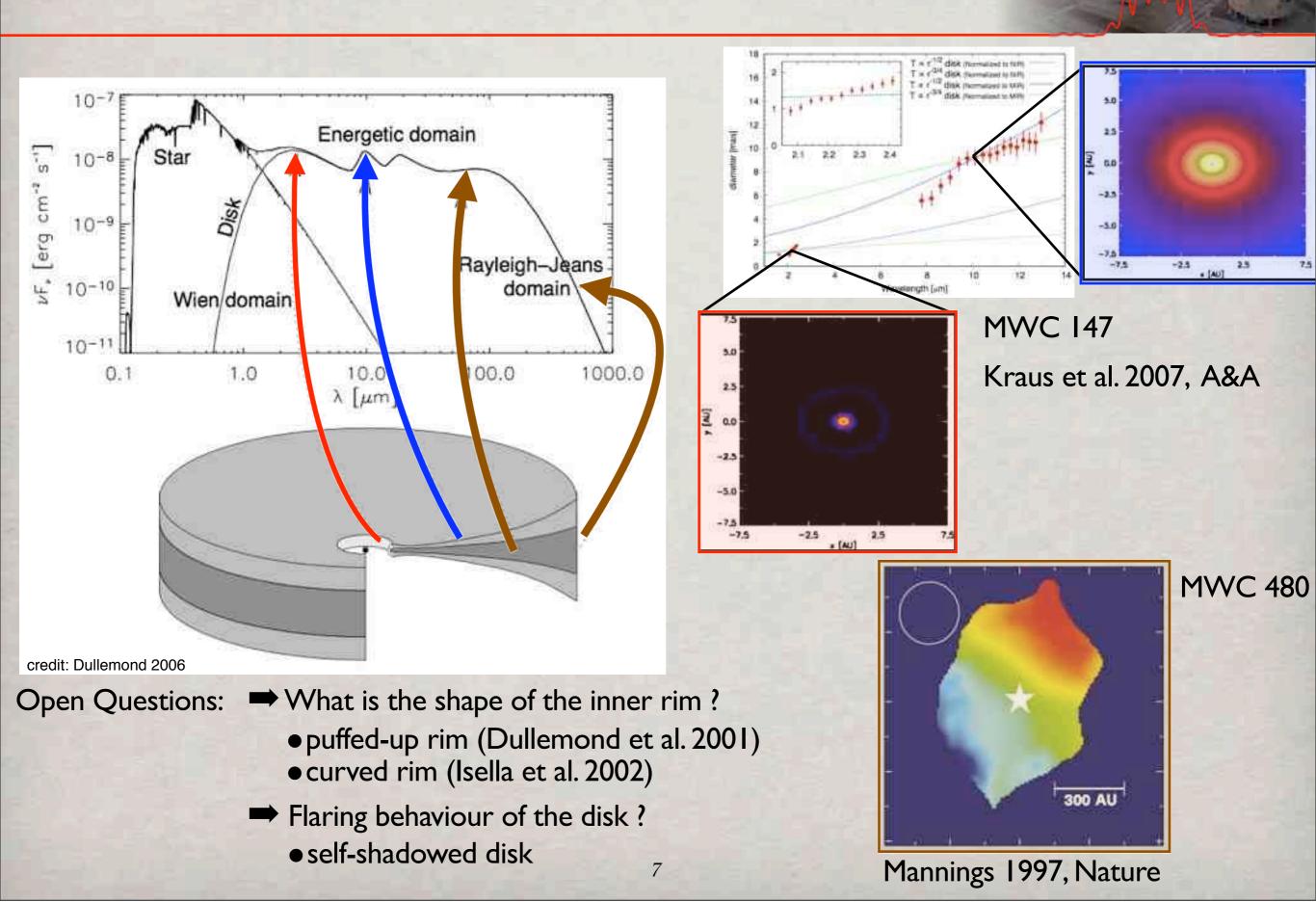
 (e.g. with a 200 m baseline at $\lambda = 2.2 \mu m$ one gets an angular resolution of a = 2.7 mas)
- Observations at different wavelengths provide information about different regions of the disk!
 - → Multiwavelength analysis required to study the whole disk

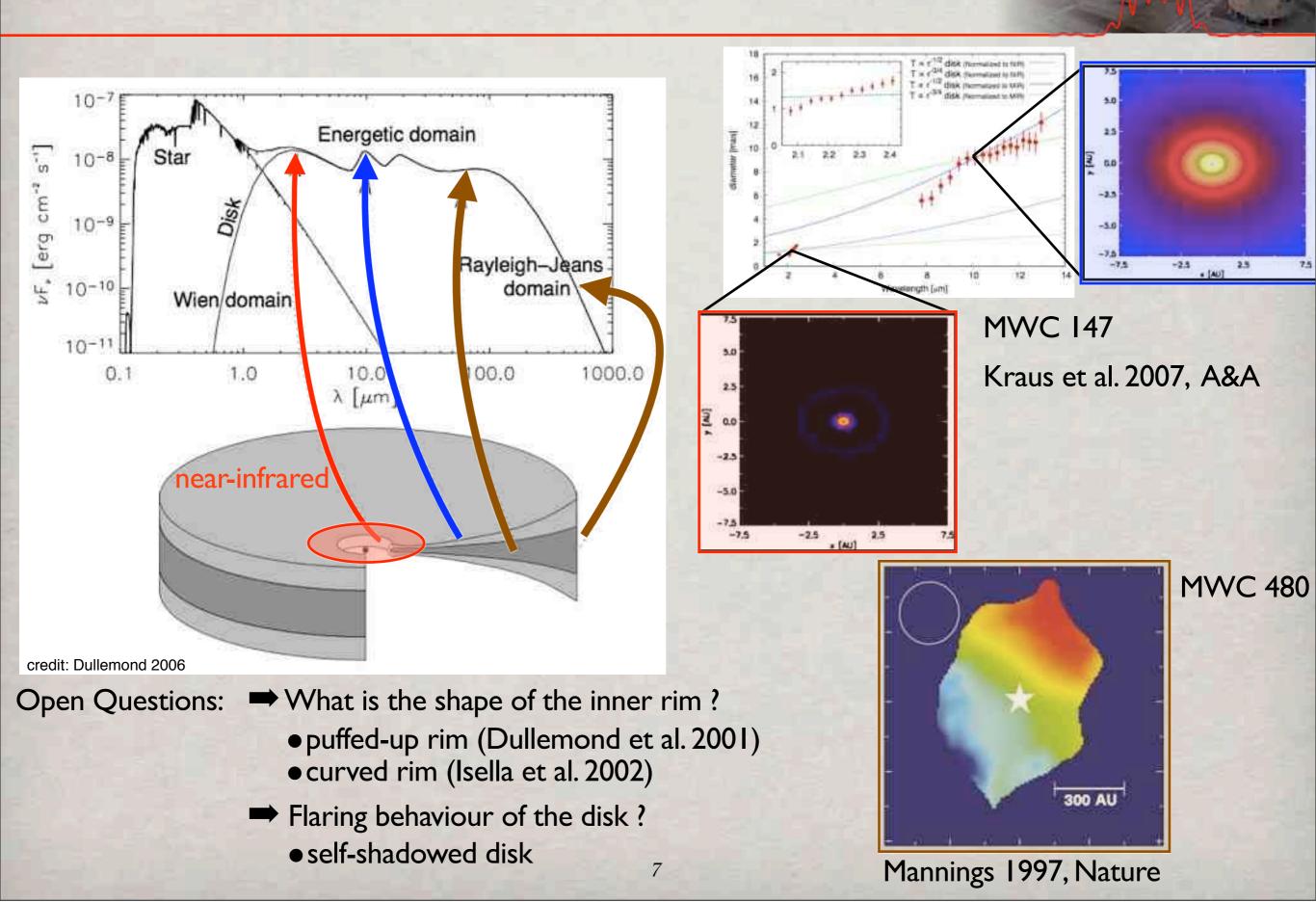




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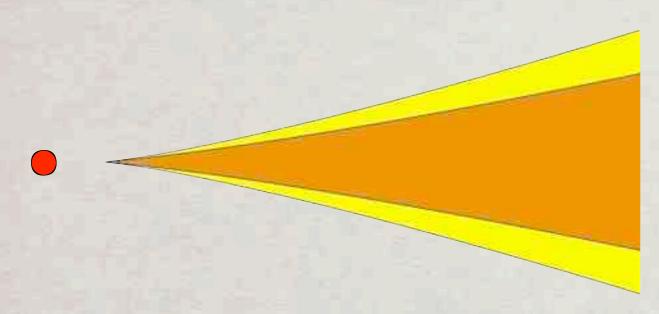


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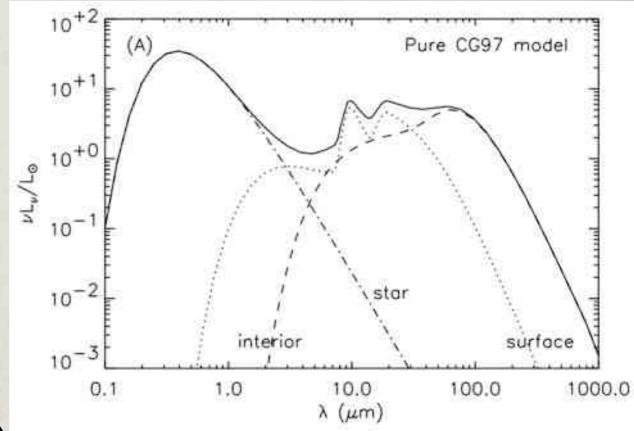
Disk models

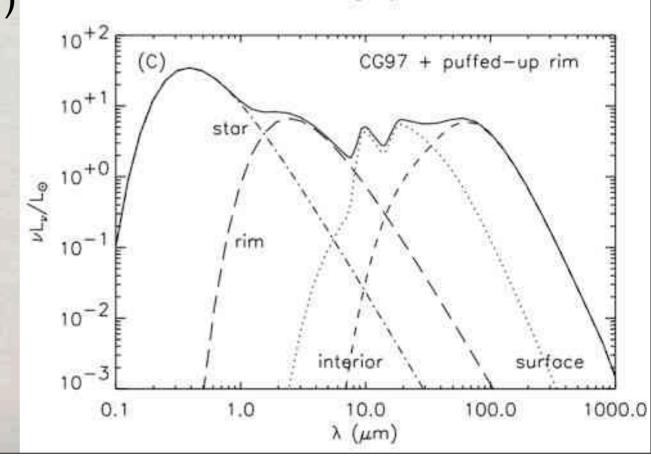


• Chiang-Goldreich model (C & G 1997)

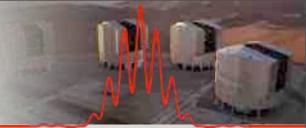


• Puffed-up inner model (Dullemond et al. 2001)

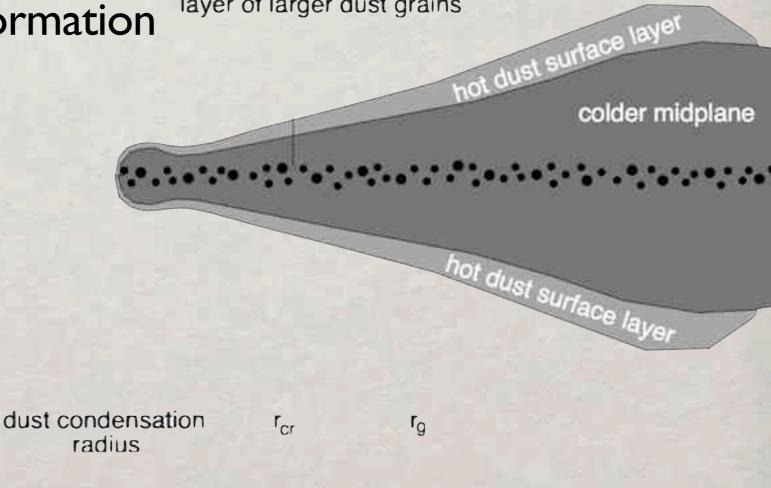




Dust disk



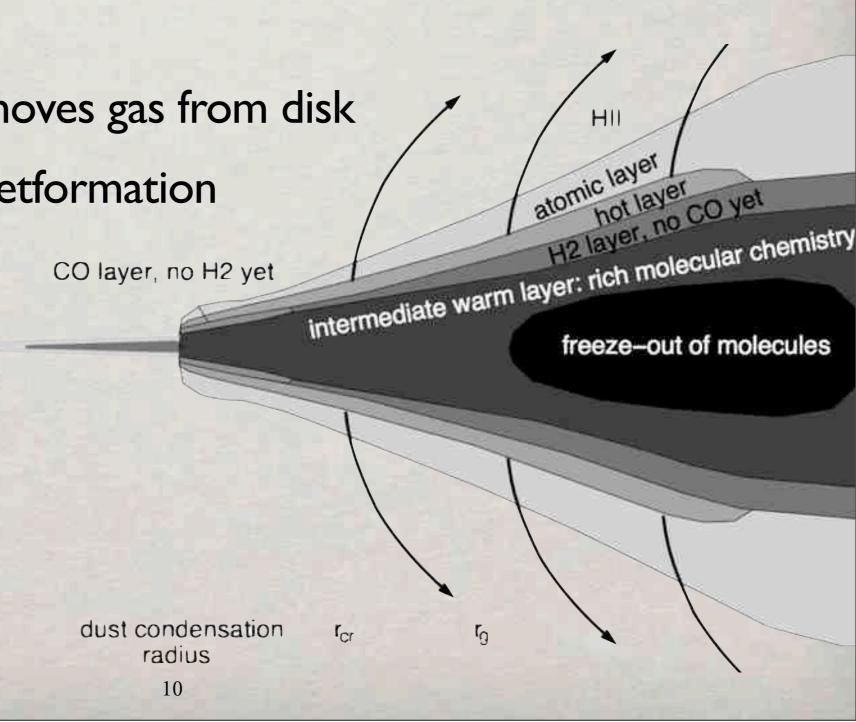
- Dust settling in the cooler mid-plane
 - ----- grain growth
- Photoevaporation removes gas from disk
 - influences planetformation
 - dust particles follow the gas flow
 - formation of gas planets is supressed



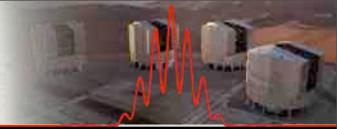
layer of larger dust grains

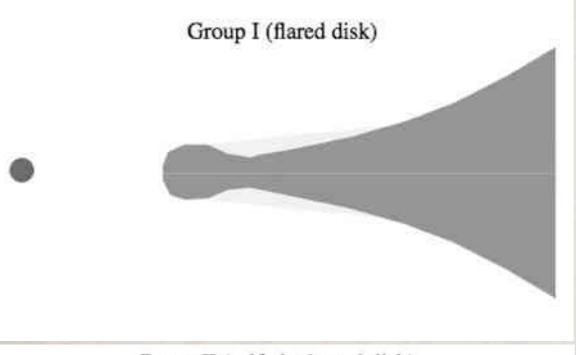
Gas disk

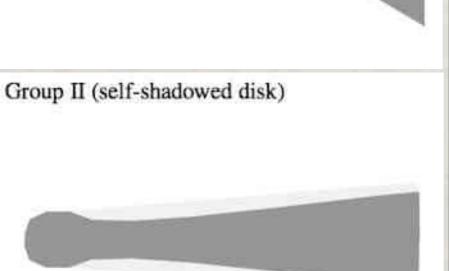
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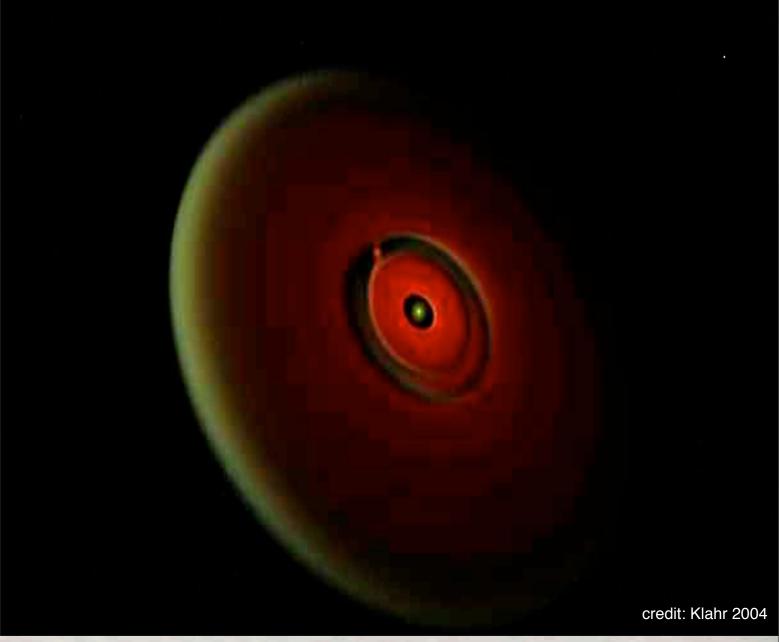


Shadowing or planetary gap?





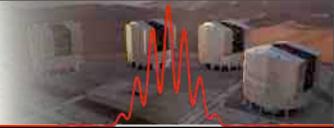


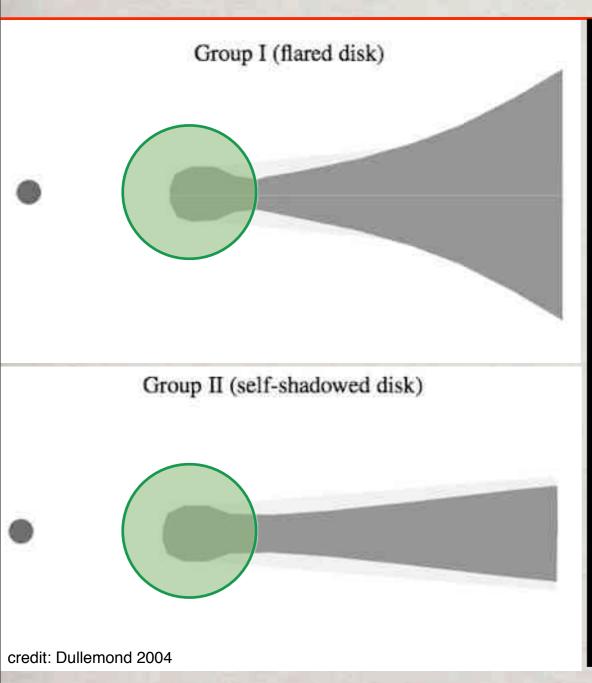


- Puffed-up inner rim leads to shadowing of parts of the disk
 - detectable, but still confusion with planetary gaps

credit: Dullemond 2004

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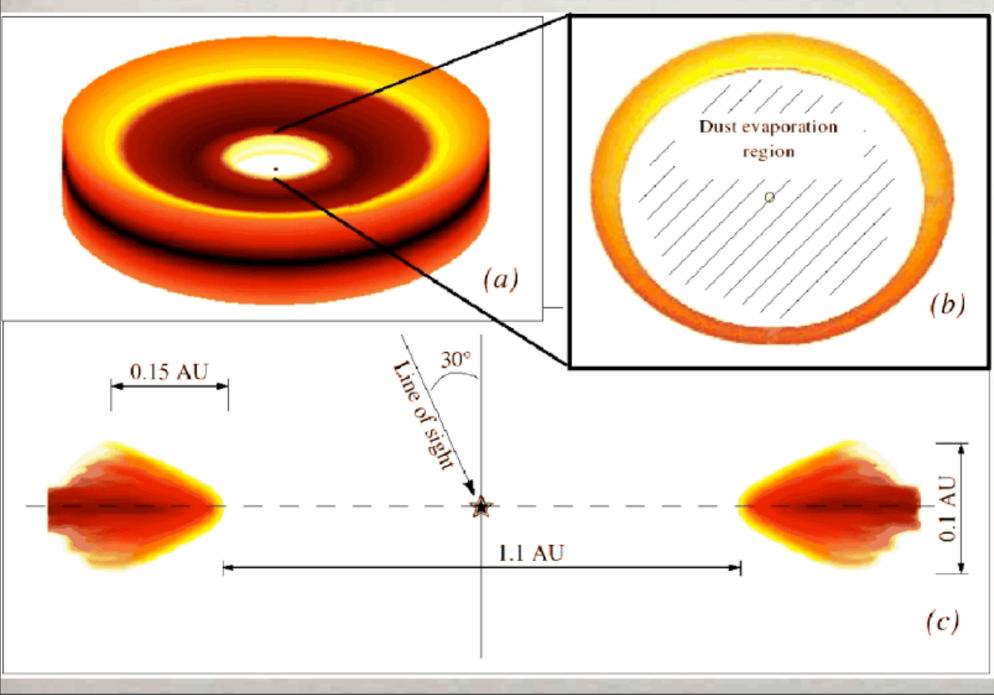
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The inner rim

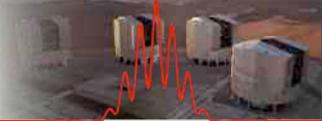


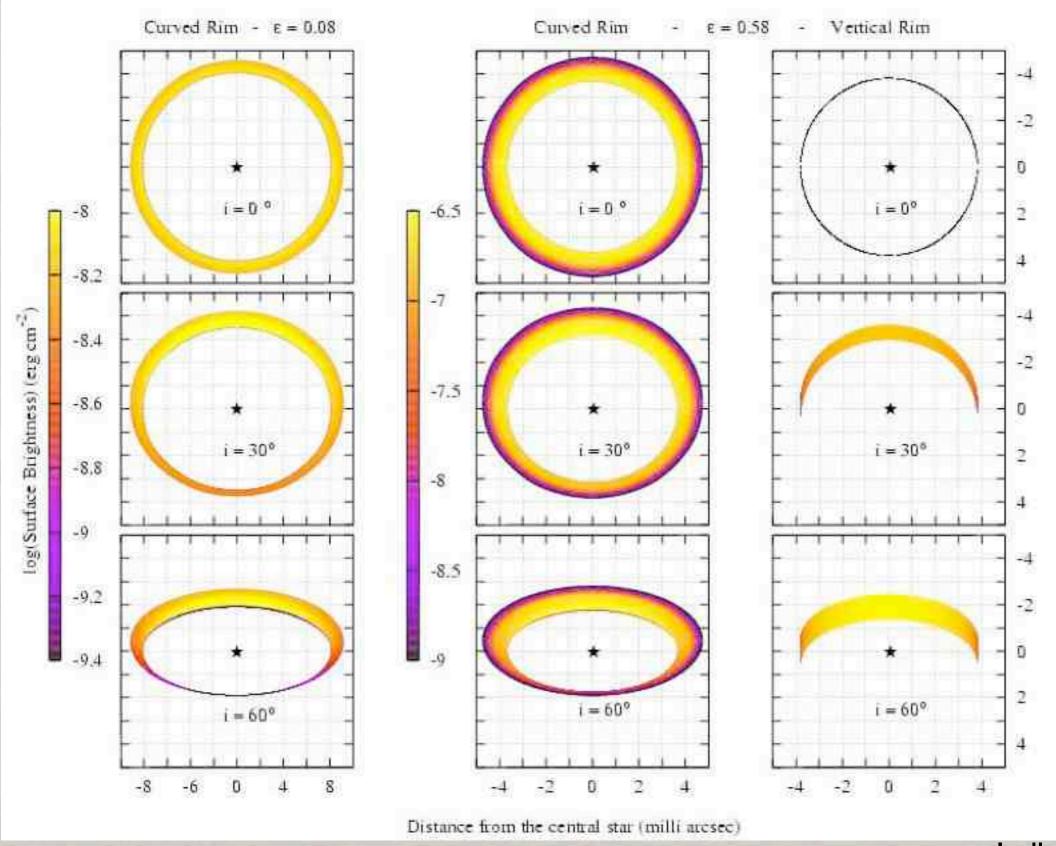
The inner rim should be curved and NOT be vertical



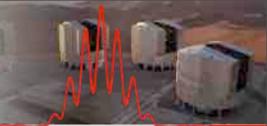
Isella et al. 2007

The inner rim



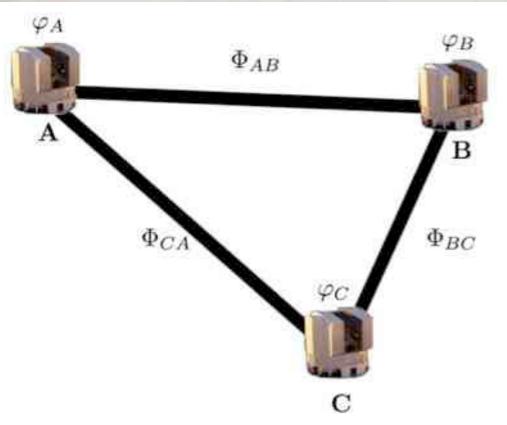


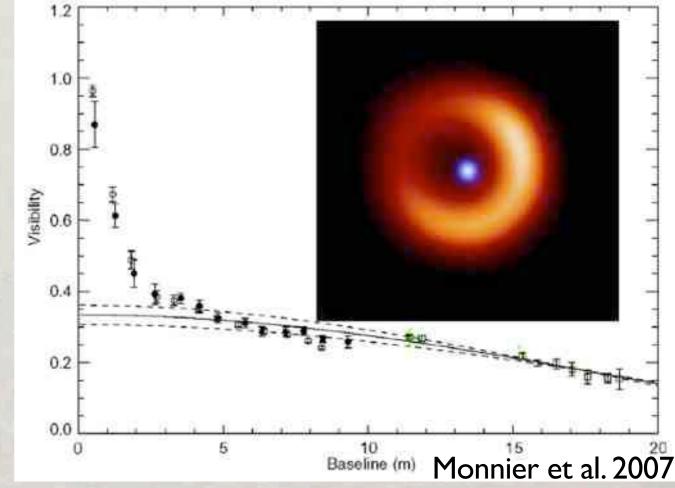
The inner rim



- Closure phases contain information about the inner rim
 - CP measures the degree of asymmetry of the brightness

distribution on the sky



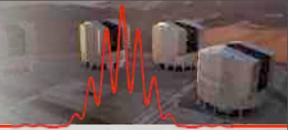


$$\tilde{\Phi}_{AB} := \Phi_{AB} + \varphi_B - \varphi_A \qquad \Phi_{CP} := \tilde{\Phi}_{AB} + \tilde{\Phi}_{BC} + \tilde{\Phi}_{CA}
\tilde{\Phi}_{BC} := \Phi_{BC} + \varphi_C - \varphi_B \qquad = \Phi_{AB} + \varphi_B - \varphi_A + \varphi_B - \varphi_A + \varphi_{CA}
\tilde{\Phi}_{CA} := \Phi_{CA} + \varphi_A - \varphi_C \qquad = \Phi_{AB} + \Phi_{BC} + \Phi_{CA}$$

$$\begin{split} \Phi_{CP} &:= \tilde{\Phi}_{AB} + \tilde{\Phi}_{BC} + \tilde{\Phi}_{CA} \\ &= \Phi_{AB} + \varphi_B - \varphi_A + \Phi_{BC} + \varphi_C - \varphi_B + \Phi_{CA} + \varphi_A - \varphi_C \\ &= \Phi_{AB} + \Phi_{BC} + \Phi_{CA} \end{split}$$

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Very Large Telescope Interferometer (VLTI)

Dates: 2007-05-13

2007-05-14

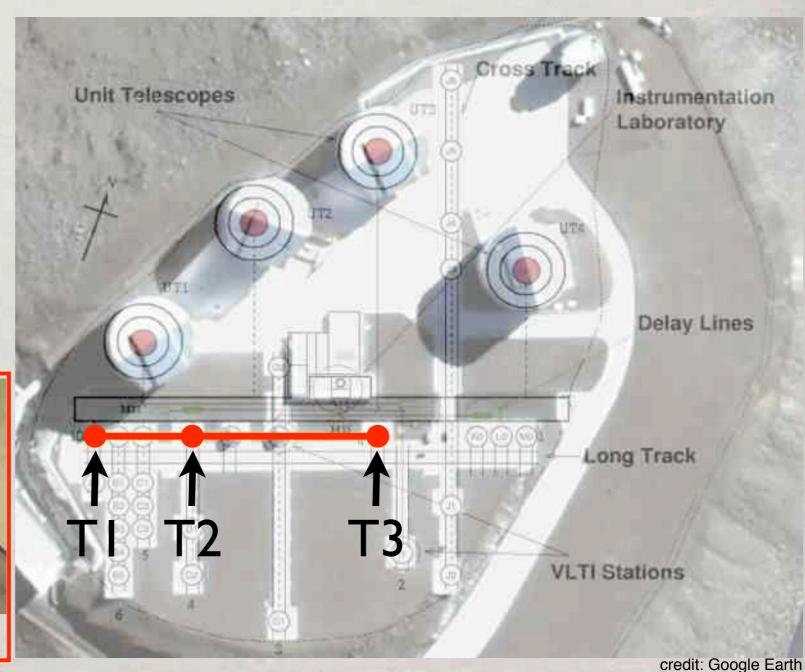
Telescopes: 3 AT's in a linear

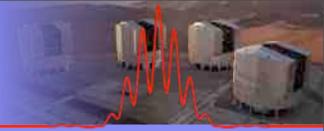
configuration

Aperture: 1.8 m

Baselines: 32 m, 64m, 96 m







AMBER produces spectrally dispersed Michelson Interferograms



photometric beam I

beam 2

photometric interferometric photometric beam

beam 3

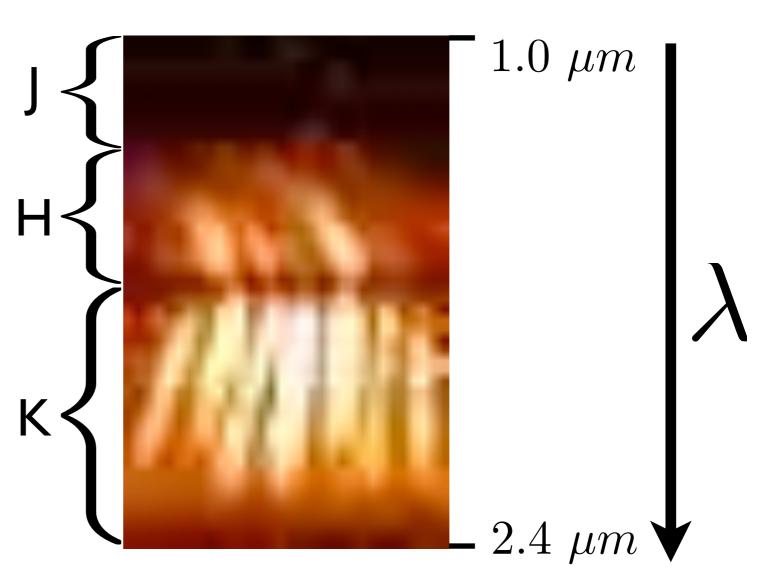


AMBER provides different spectral resolution modes

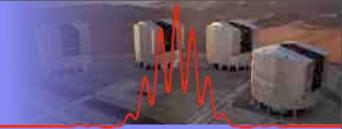
HIGH (R = 12000)

MEDIUM (R= 1500)

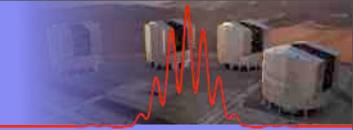
LOW (R = 30)

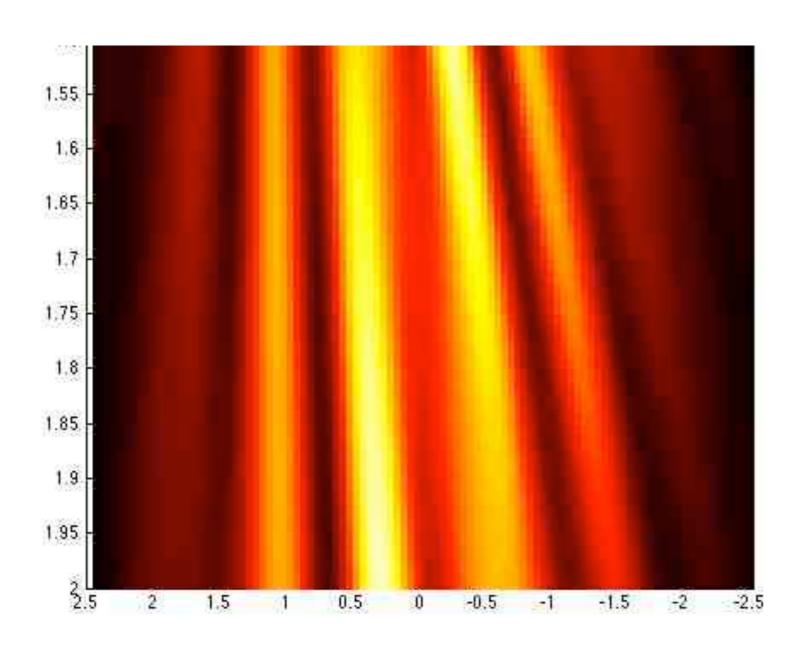


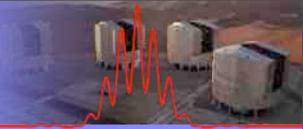
observation carried out in LOW resolution

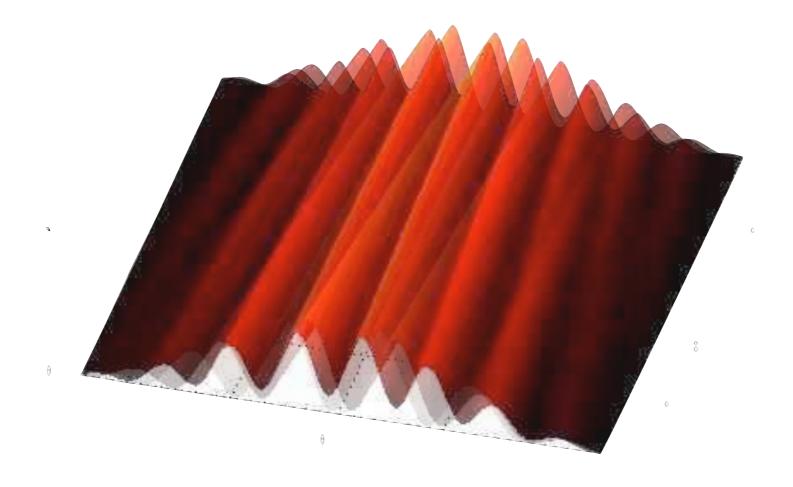




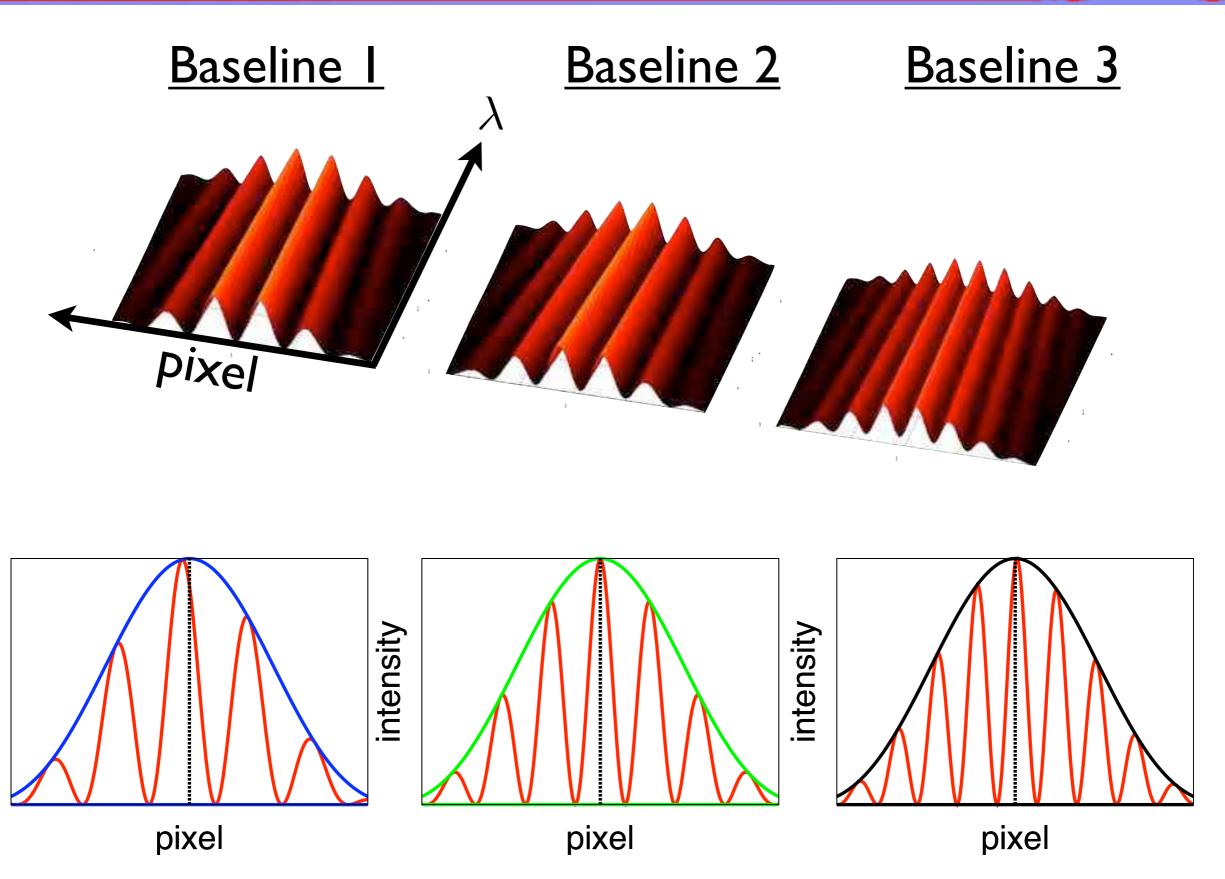






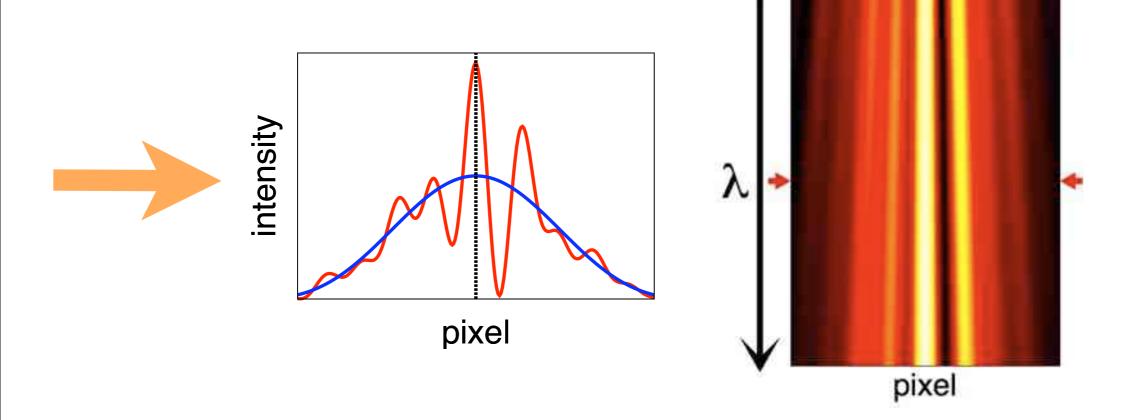




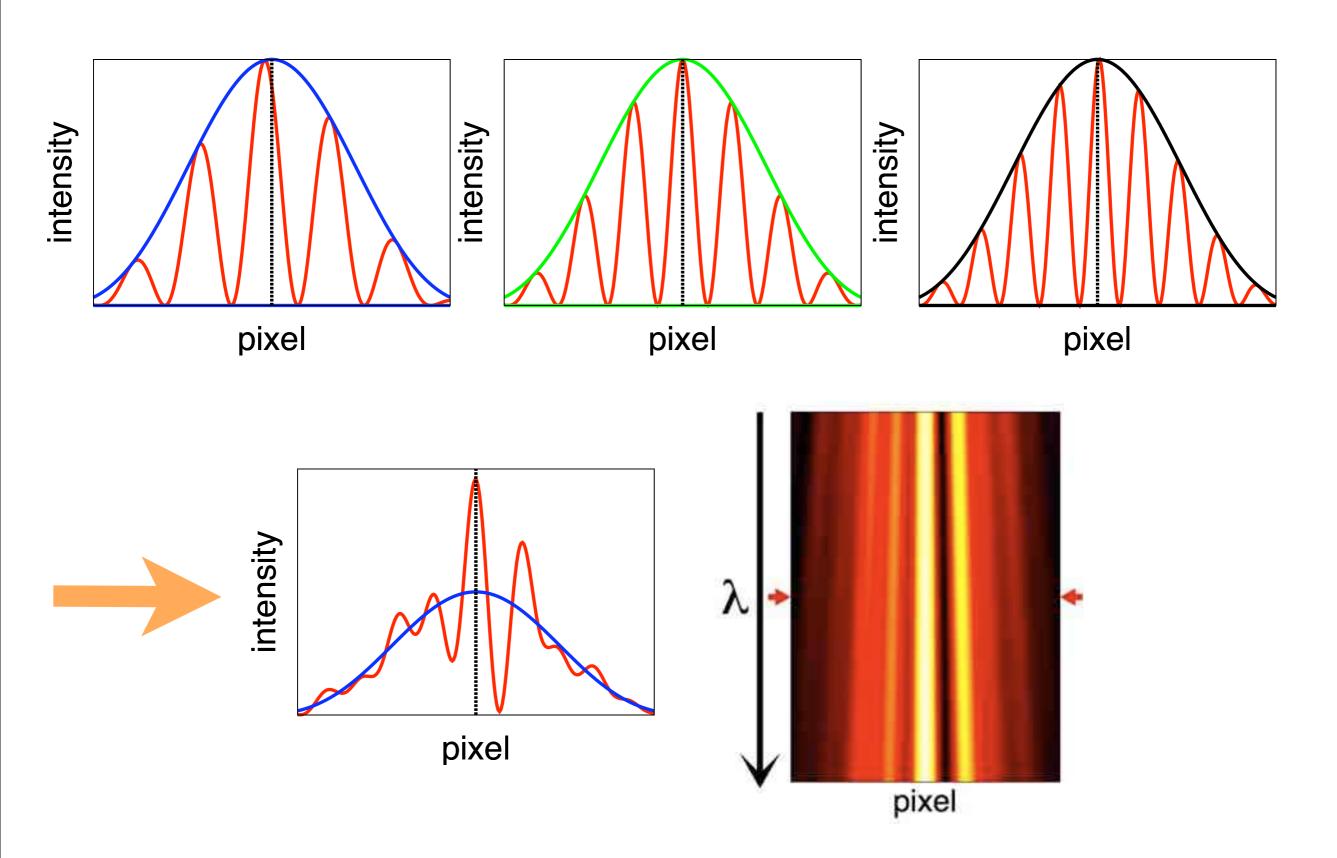


intensity

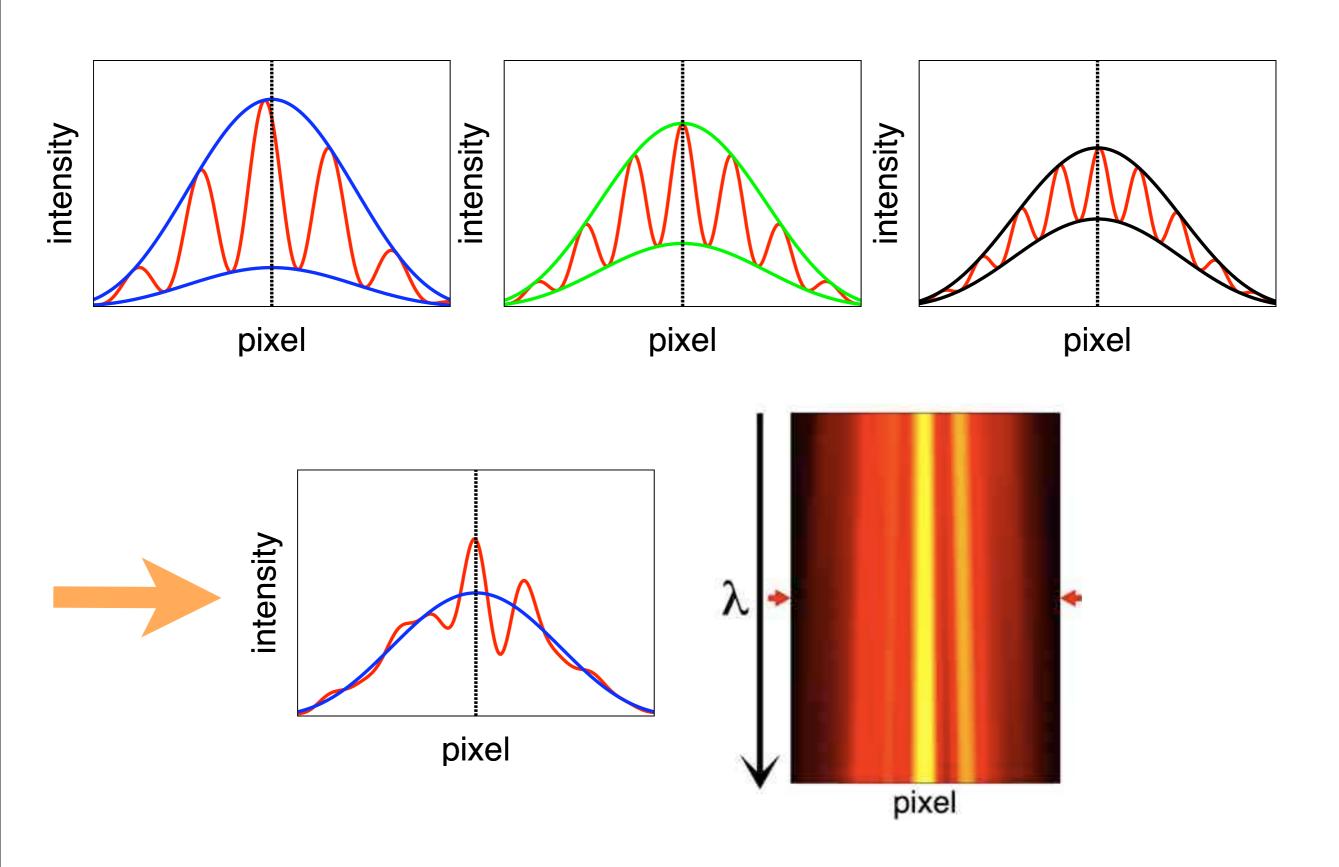


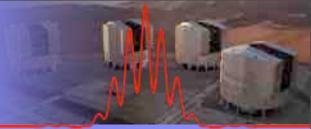




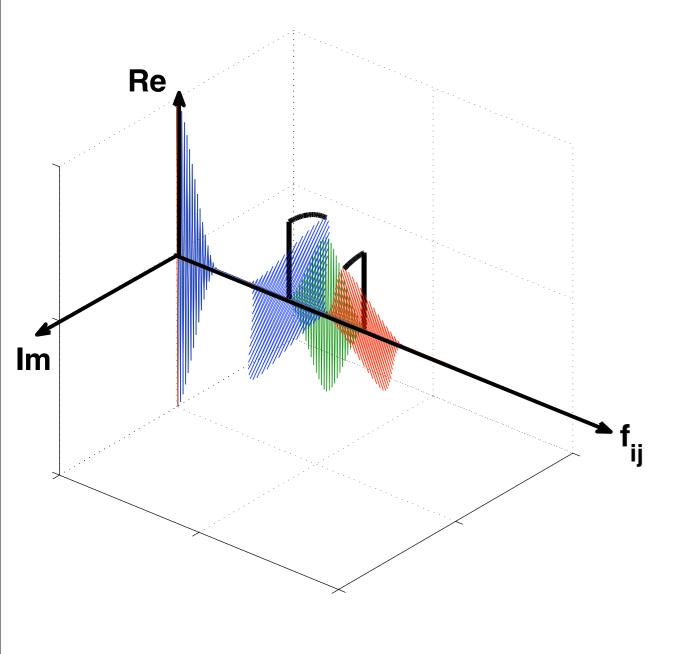


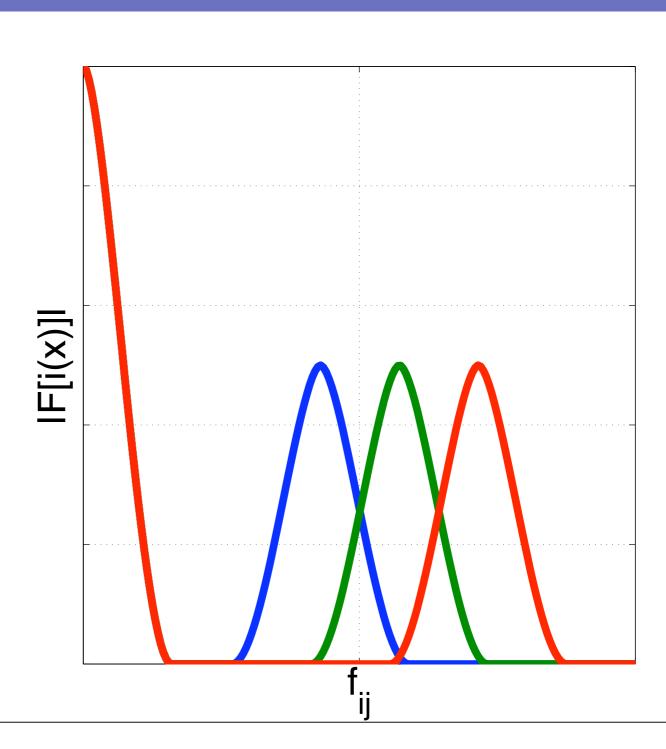


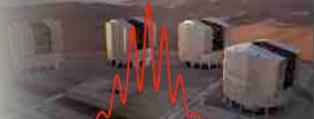




 Fourieranalysis is difficult because of fringepeak overlap







The equation of the AMBER interferogram

$$I_k = \sum_{i}^{N_{\text{tel}}} a_k^i F^i + \sum_{i < j}^{N_{\text{tel}}} \sqrt{a_k^i a_k^j} C_B^{ij} \text{Re}[F_c^{ij} \cdot e^{i(2\pi\alpha_k f^{ij} + \phi_s^{ij} + \phi_B^{ij})}]$$

with the coherent flux:

$$F_c^{ij} = 2N\sqrt{t^i t^j} V^{ij} e^{i(\phi^{ij} + \phi_p^{ij})}$$

can be rewritten in terms of so called "carrier waves"

$$I_k = \sum_{i}^{N_{\text{tel}}} a_k^i F^i + \sum_{i < j}^{N_{\text{tel}}} [c_k^{ij} R^{ij} + d_k^{ij} I^{ij}]$$

$$m_k$$

 $c_k^{ij} = C_B^{ij} \frac{\sqrt{a_k^i a_k^j}}{\sqrt{\sum_k a_k^i a_k^j}} \cos(2\pi\alpha_k f^{ij} + \phi_s^{ij} + \phi_B^{ij})$

$$d_k^{ij} = C_B^{ij} \frac{\sqrt{a_k^i a_k^j}}{\sqrt{\sum_k a_k^i a_k^j}} \sin(2\pi\alpha_k f^{ij} + \phi_s^{ij} + \phi_B^{ij})$$

$$R^{ij} = \sqrt{\sum_{k} a_k^i a_k^j} \operatorname{Re}[F_c^{ij}]$$

$$I^{ij} = \sqrt{\sum_k a_k^i a_k^j} \operatorname{Im}[F_c^{ij}]$$

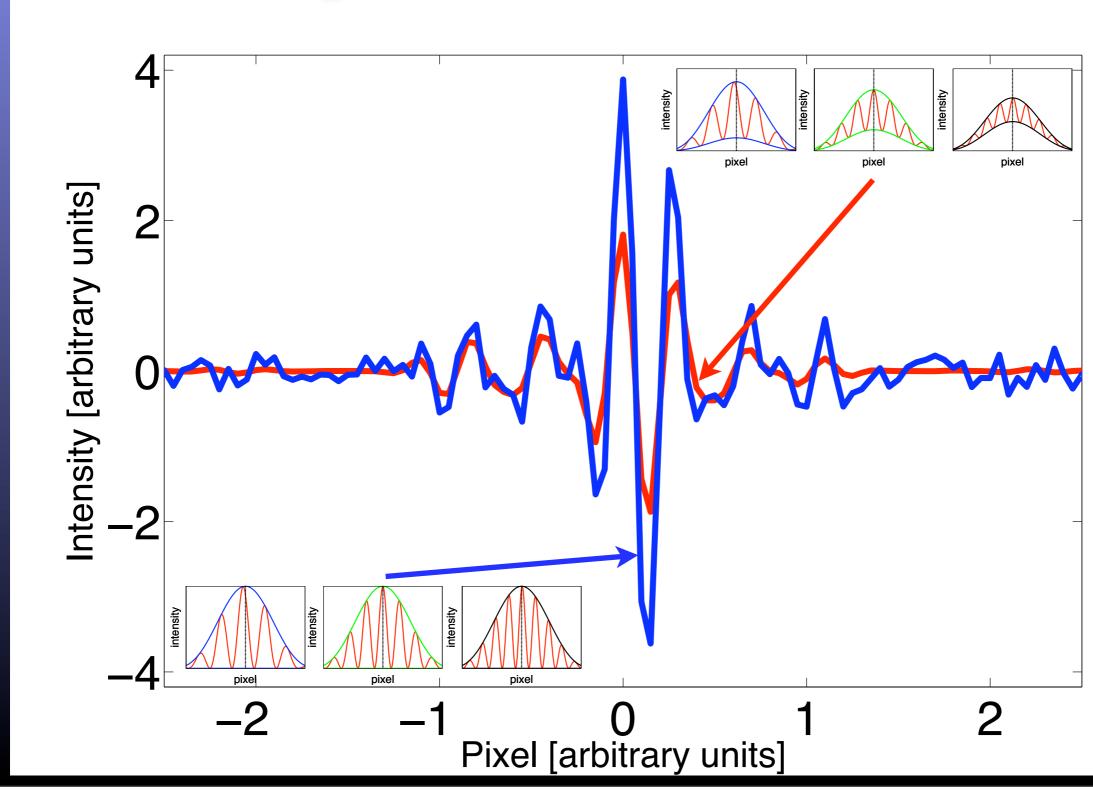
in matrix form:

$$\begin{pmatrix} m_1 \\ \vdots \\ m_k \end{pmatrix} = V2PM \cdot \begin{pmatrix} \vdots \\ R^{ij} \\ \vdots \\ I^{ij} \\ \vdots \end{pmatrix}$$

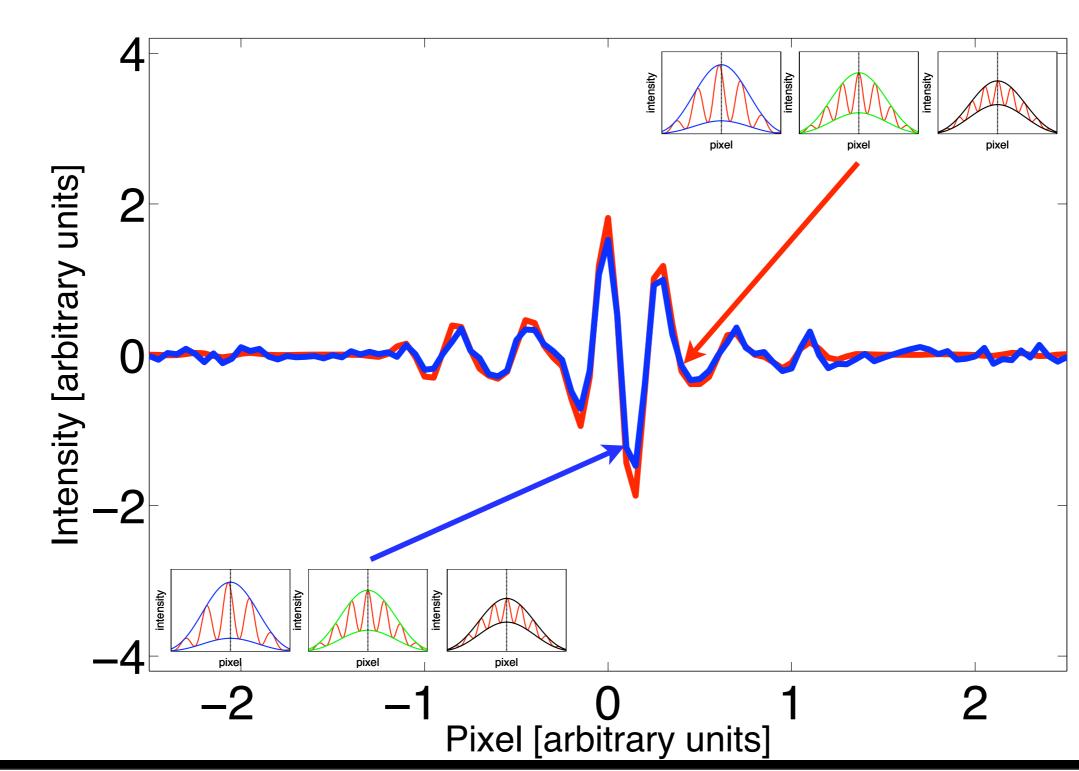
with the "Visibility to Pixel Matrix", containing the carrier waves a and d



• alternative algorithm has to be used

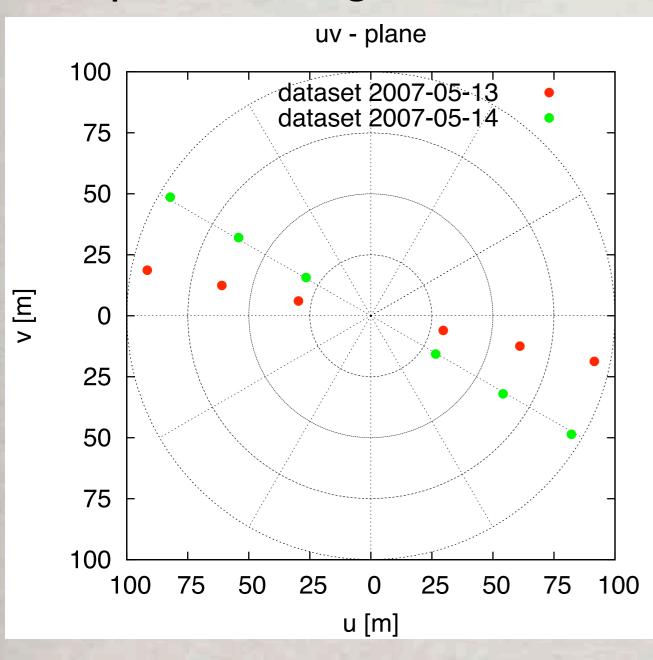


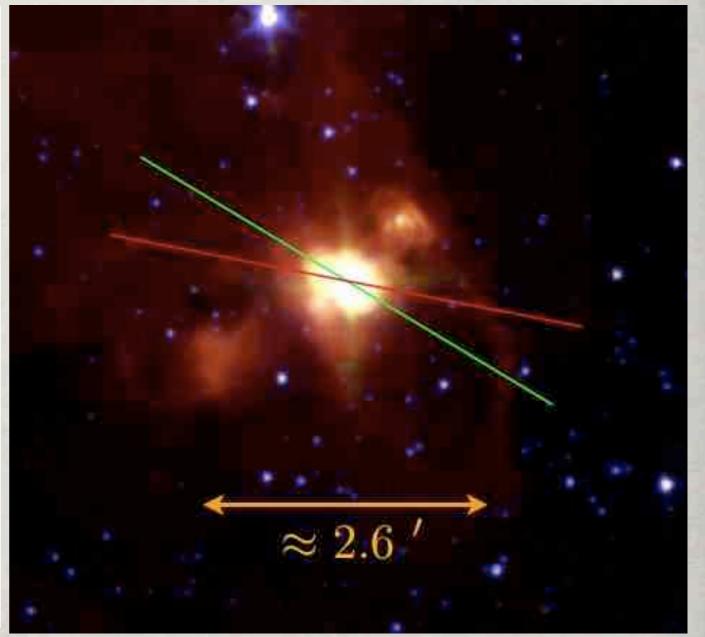






uv - plane coverage





B2 = 62 m

B3 = 93 m

2007.05.13: $\Theta_{pos} = 79^{\circ}$

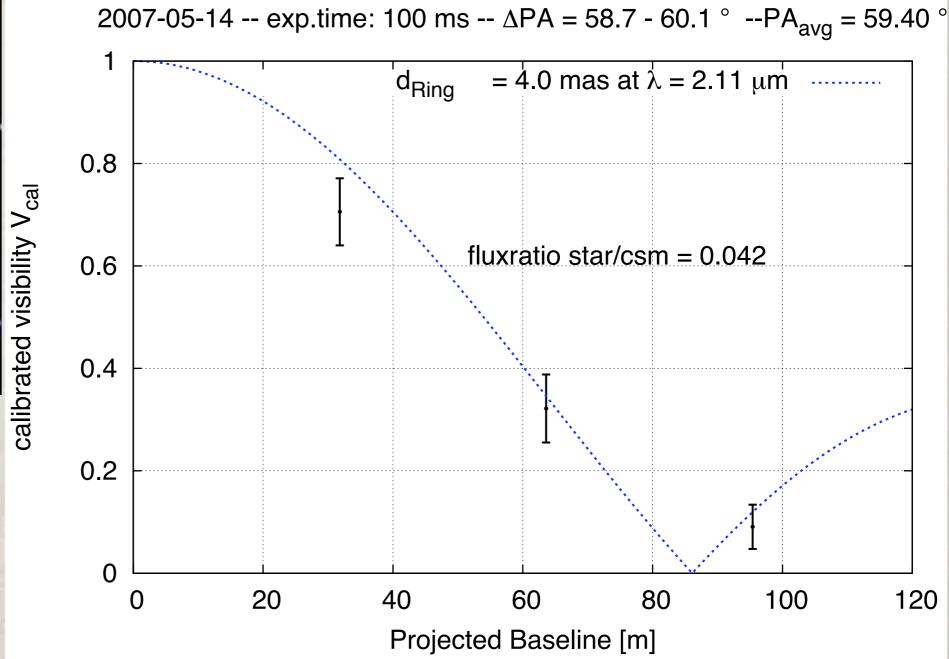
2007.05.14: $\Theta_{\rm pos} = 59^{\circ}$

• The coverage in position angle of ~20° could not be used to analyse possible asymmetries in the source structure





$$\Theta_{\text{pos}} = 59^{\circ}$$



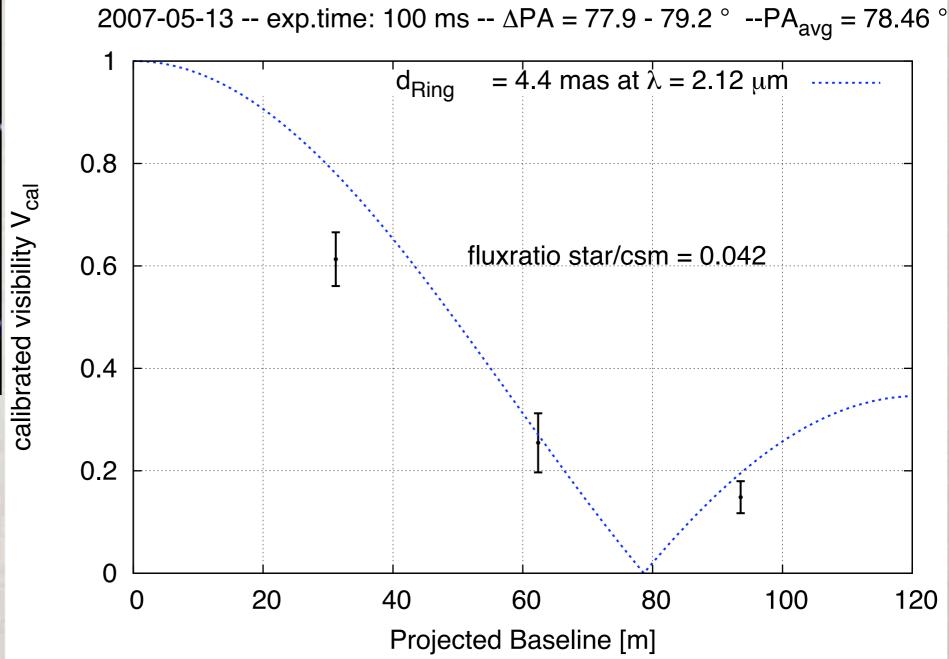


$$d_{\rm ring} = 4.0 \pm 0.2 \; {\rm mas}$$





$$\Theta_{\rm pos} = 79^{\circ}$$





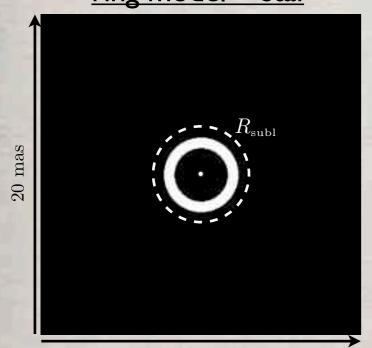
$$d_{\rm ring} = 4.4 \pm 0.4 \text{ mas}$$



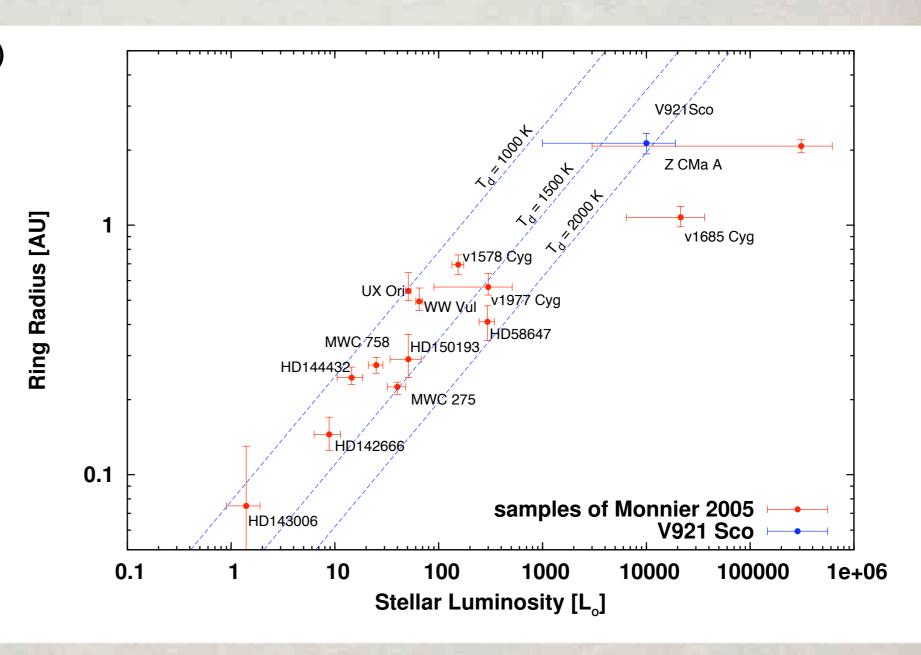
Size-Luminosity relation

(Monnier & Millan-Gabet 2002)

•To interprete the nature of the near-infrared emitting region, the fitted ring-radius is compared to the expected dust sublimation radius ring model + star



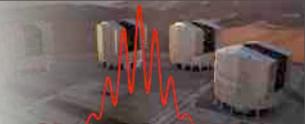
20 mas



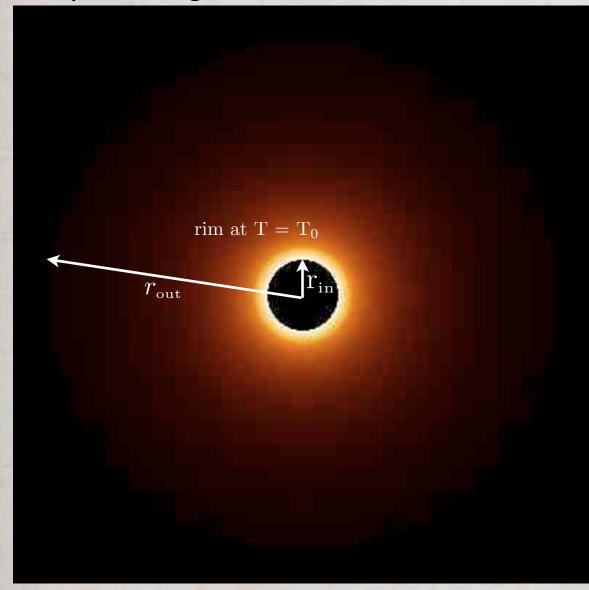
Dust sublimation radius: $R_s = 1.1\sqrt{\epsilon} \left(\frac{L_\star}{1000L_\odot}\right)^{\frac{1}{2}} \left(\frac{T_s}{1500\mathrm{K}}\right)^{-2}$

with the ratio of the dust absorption efficiencies:

$$\epsilon = rac{Q_{
m abs}(T_{\star})}{Q_{
m abs}(T_{
m subl})}$$



Temperature-gradient model



 To get a first more physical approach a temperature-gradient model was used to reconstruct the visibility which was already successfully applied to YSO's (e.g. Bertout et al. 1988, Malbet et al. 1995) Temperature profile:

$$T(r) = T_0 \cdot \left(\frac{r}{r_{\rm in}}\right)^{-q}$$

 $\Gamma_{\rm in}$: inner disk radius

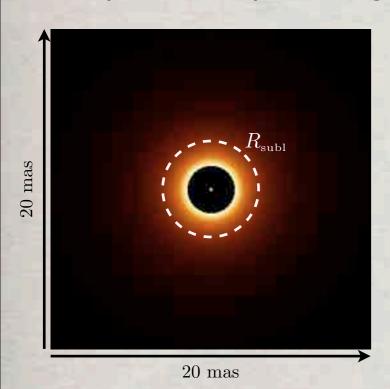
q :exponent

 T_0 :Temperature at $r=r_{
m in}$

$$F_{\lambda} = \frac{2\pi}{d^2} \cdot \cos(\phi) \cdot \int_{r_{\text{in}}}^{r_{\text{out}}} B_{\lambda}(T(r)) r dr$$



2-component temperature-gradient model (disk+star):



$$q = 0.55$$

 $d = 1.15 \text{ kpc}$
 $r_{in} = 1.7 \text{ AU}$
 $r_{out} = 13.2 \text{ AU}$
 $T_0 = 1500 \text{ K}$

$$R_{\star} = 17.3 \ R_{\odot}$$

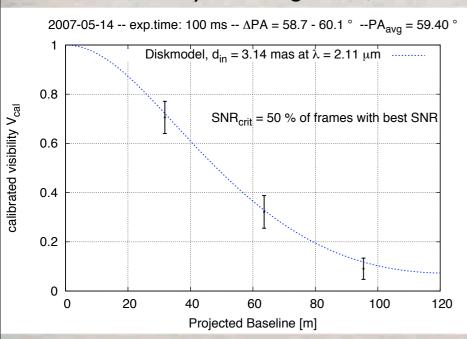
 $T_{\star} = 13225 \ K$

This model is able to reproduce both the observed SED and observed multiwavelength visibilities

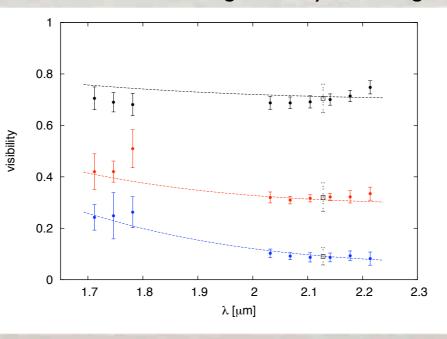
Problem:

The inner dust-disk radius is smaller then the dust sublimation radius

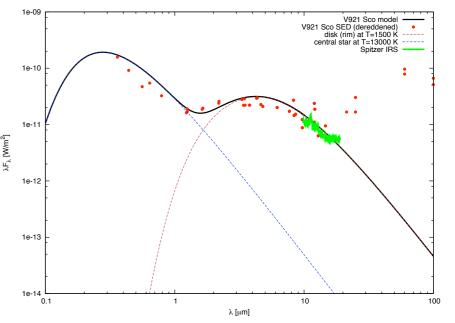
visibility modelling at 2.1 µm

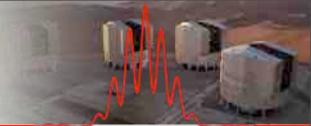


multiwavelength visibiliy modelling

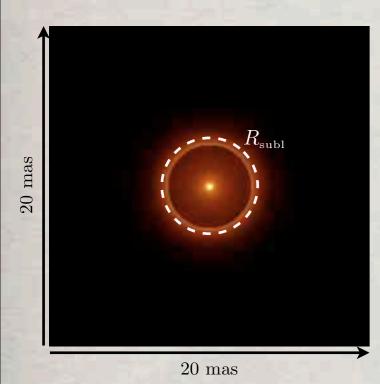


SED modelling





3-component temperature-gradient model (gas disk + dust disk + star):



$$q = 1.3$$
 $d = 1.15 \text{ kpc}$
 $r_{\text{in}} = 2.9 \text{ AU}$
 $r_{\text{out}} = 14.5 \text{ AU}$
 $T_0 = 1500 \text{ K}$
 $q = 0.2$
 $d = 1.15 \text{ kpc}$
 $r_{\text{in}} = 0.12 \text{ AU}$
 $r_{\text{out}} = 2.9 \text{ AU}$
 $r_{\text{out}} = 2.9 \text{ AU}$
 $r_{\text{out}} = 2000 \text{ K}$

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$$R_{\star} = 17.3 \ R_{\odot}$$

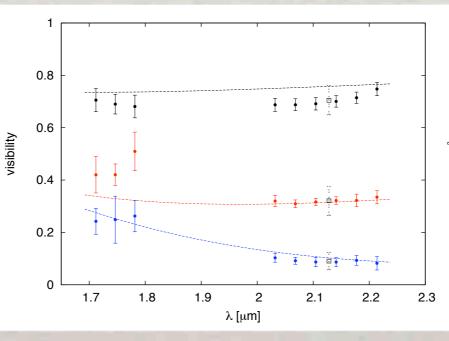
 $T_{\star} = 13225 \ K$

This model is able to reproduce both the observed SED and observed multiwavelength visibilities

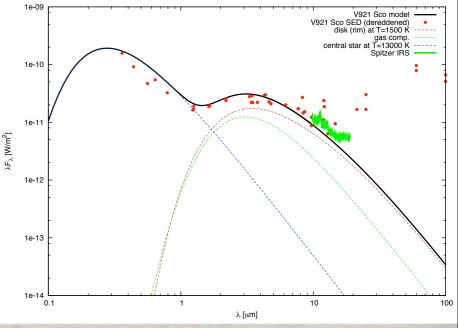
visibility modelling at 2.1 µm

2007-05-14 -- exp.time: 100 ms -- Δ PA = 58.7 - 60.1 ° -- PA_{avq} = 59.40 ° Diskmodel, $d_{in} = 5.2$ mas at $\lambda = 2.10 \mu m$ 0.8 calibrated visibility V_{cal} SNR_{crit} = 50 % of frames with best SNR 0.6 0.4 0.2 20 100 Projected Baseline [m]

multiwavelength visibiliy modelling

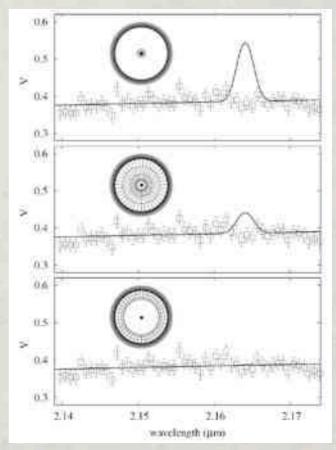


SED modelling



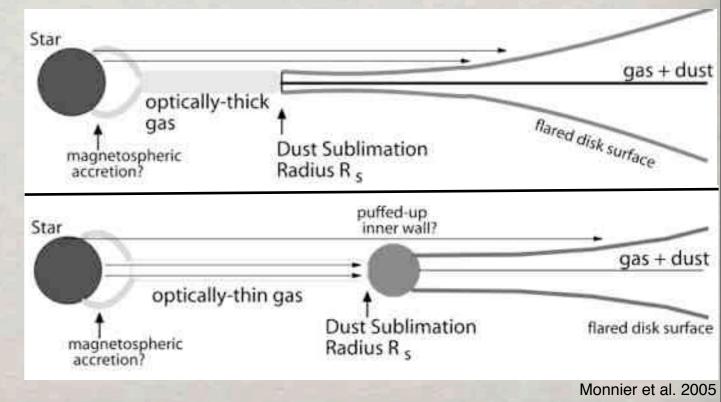
32

- For the given stellar parameters the measured ring radius is more compact than expected
 - One reason might be that the stellar luminosity could be overestimated
 - The dust sublimation radius is not compact in contrast to the expected one



Tatulli 2007 et al.

- An optically-thin inner gas disk could contribute to the total near-infrared emission
 - Such inner gaseous disks where already successfully observed in YSO's e.g. MWC 147 (Kraus et al. 2007)
 MWC 748 (Isella et al. 2008)

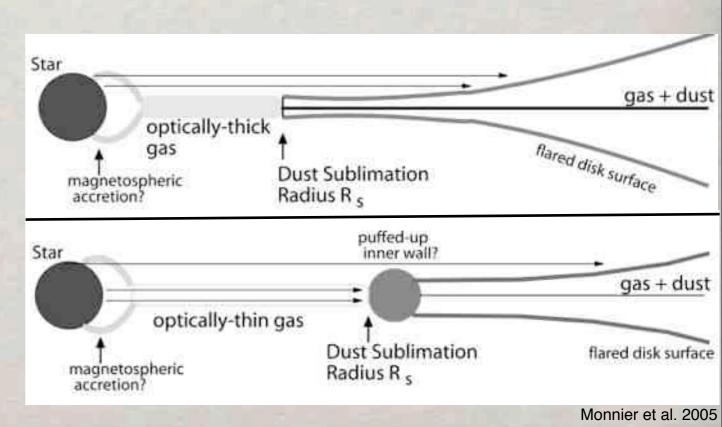


Tatulli 2007 et al.

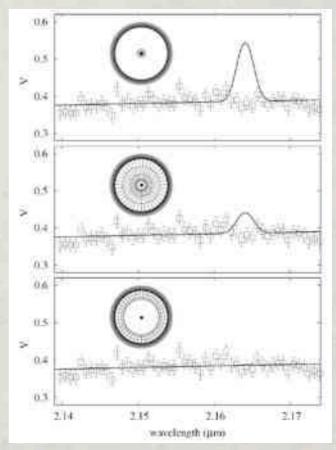
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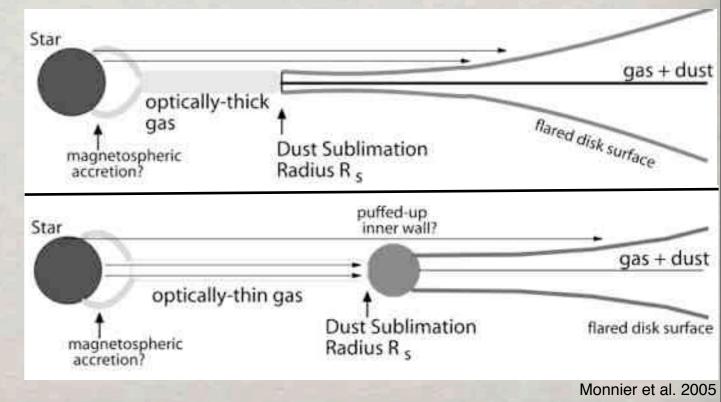


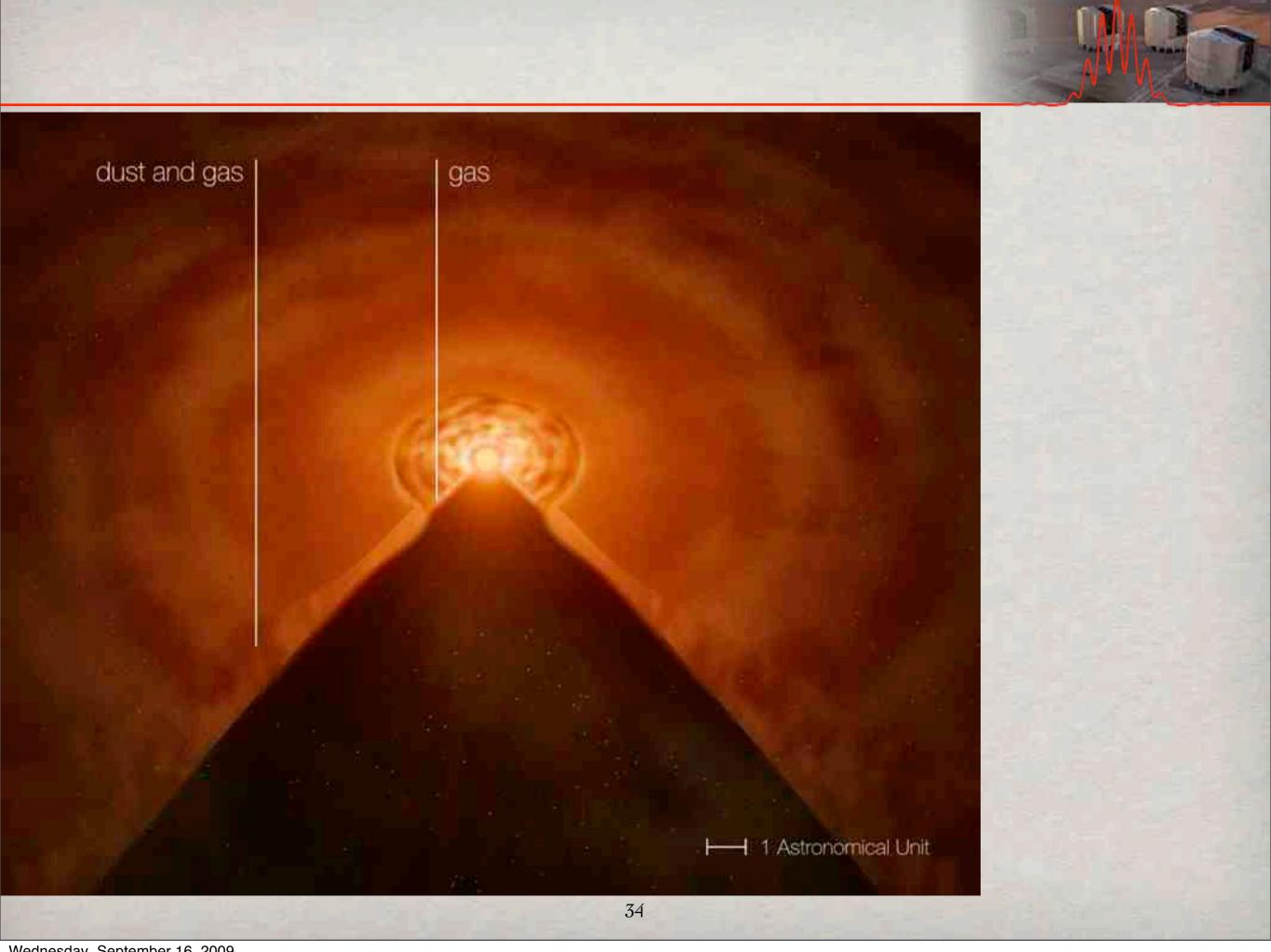
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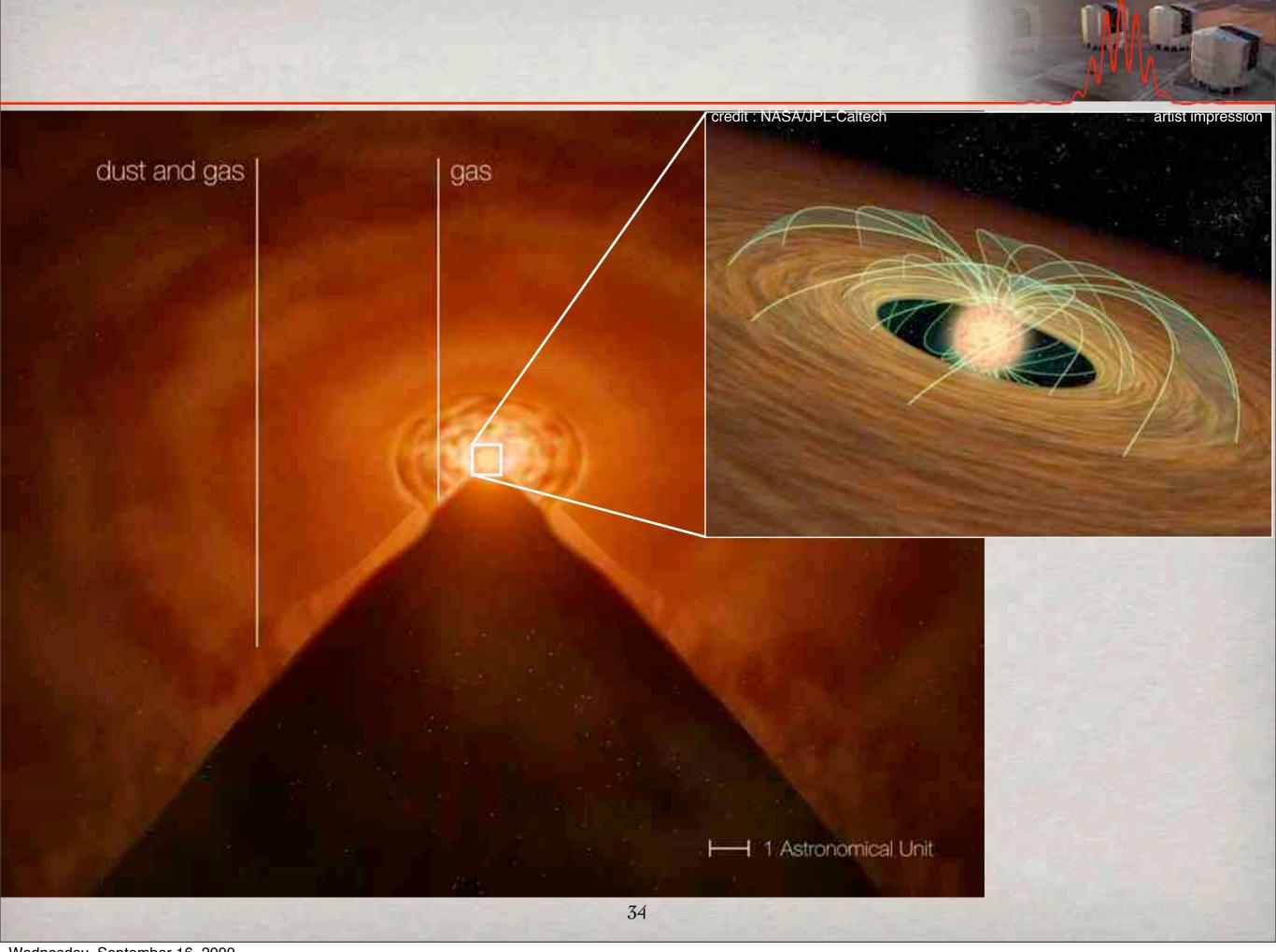


Tatulli 2007 et al.

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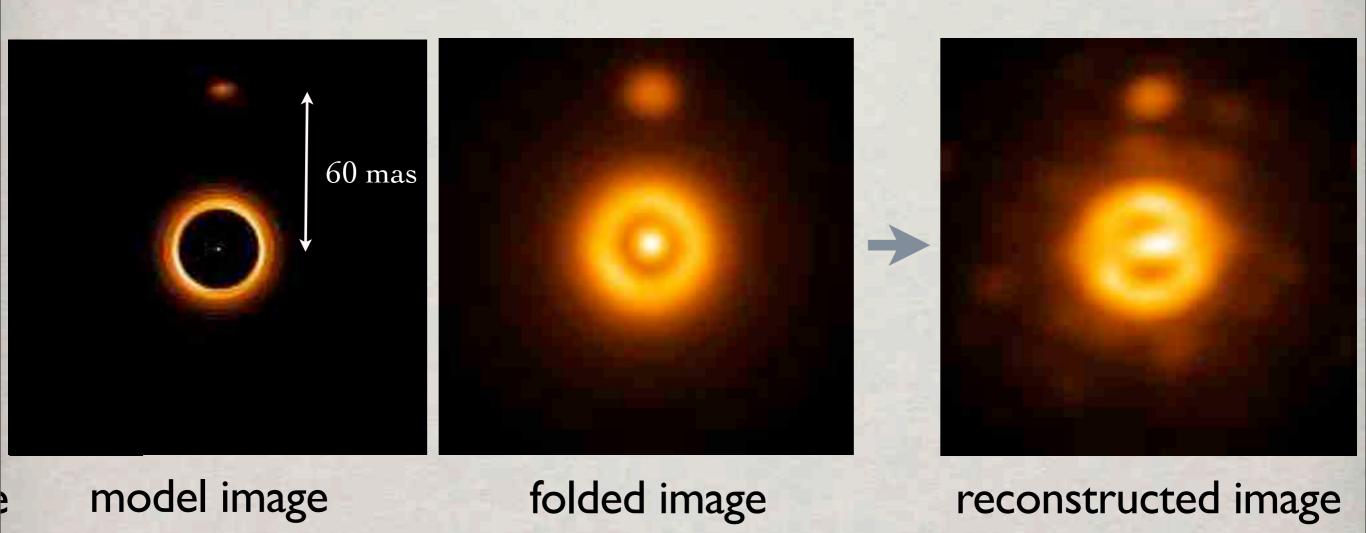
Outline

- Overview: circumstellar disk:
- Disk models
- I he inner rim
- Observational techniques: V921 Scc
- Future Instruments
- Summary

Future Instruments



MATISSE (Multi AperTure mid-Infrared SpectroScopic Experiment)

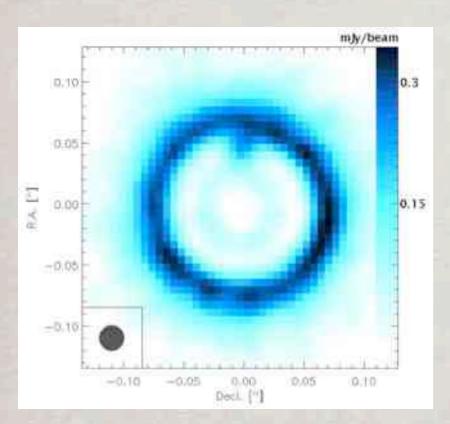


• planet 200 times fainter than central star

Future Instruments



ALMA (Atacama Large Millimeter/submillimeter Array)





Extract of ALMA Science Objectives:

"Image the gas kinematics in protoplanetary disks around young sun-like stars with a resolution of a few astronomical units out to a distance of 150 pc (roughly the distance to the star forming clouds in Ophiuchus or Corona Australis), enabling the study of their physical, chemical and magnetic field structures and detection of the tidal gaps created by planets undergoing formation in the disks."

Outline

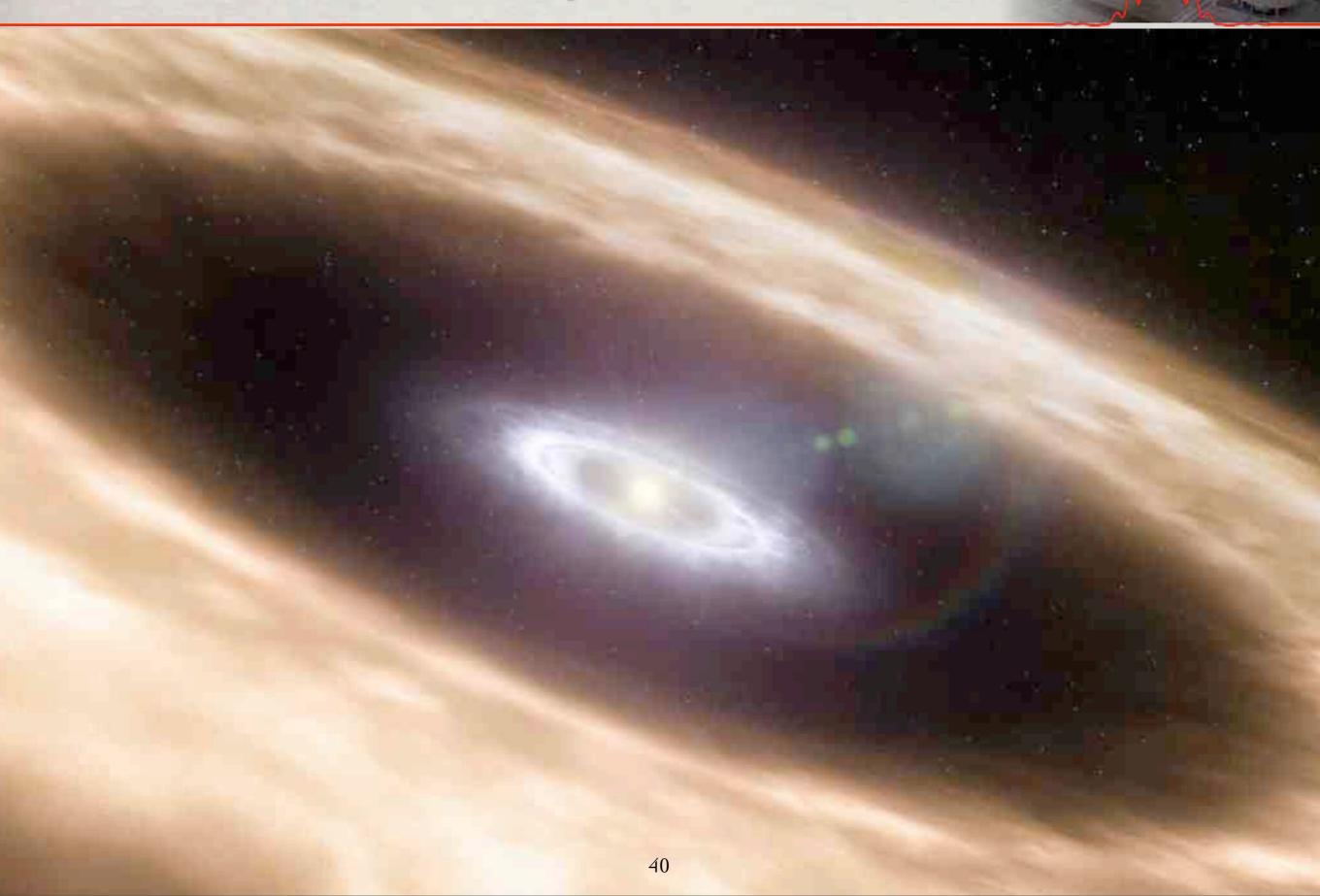
- Overview: circumstellar disk:
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- The inner rim
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Summary



- The investigation of circumstellar disks, especially around intermediate mass stars, are important to understand the formation of high mass stars. \longrightarrow stars with $M_{\star} > 10 M_{\odot}$ are embedded during their whole pre-main sequence life.
- and since we are combining at least three telescopes at the same time, we get closure phase information which reveal information about the rim structure
- with future instruments like ALMA and MATISSE we will be able to investigate circumstellar disks in more detail
 - constraints on disk mass, dust and gas composition etc.
 - detect finally planetary gaps / self shadowed disks directly

Thanks for your attention



Overview of star formation

IMPRS talk 14.09.2009

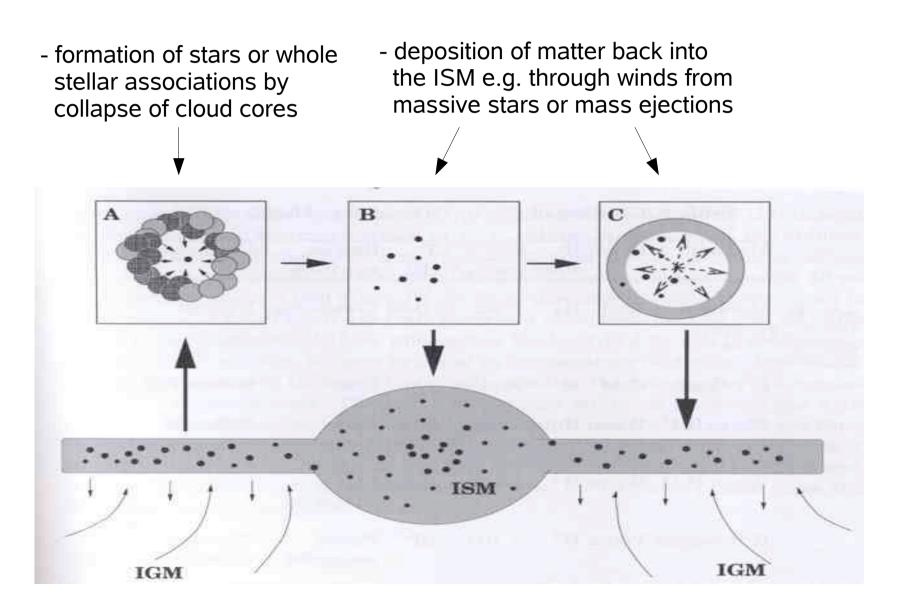
Outline

- The Interstellar medium: composition and different phases
- Initial conditions and stages of star formation
- Interstellar molecules
- Conditions of molecular clouds:
 - equilibrium and stability
 - instabilities
- Cloud collapse
- Models of star formation

The Interstellar Medium

- first observational evidence by the discovery of Ca II lines in spectra of the binary star δ Orionis by J.Hartmann in 1904
- investigation by E. Hubble in 1922: scattering of light of nearby cool stars by dust clouds (reflection nebulae) and excitation of the gas by hot stars (emission nebulae)
- The ISM is an extremely teneous gas consisting of :
- Hydrogen (H₂, H I, HII, e⁻) (90%)
- Helium (He I, He II)
- other elements (e.g. C, O, Ne, Mg, Fe)
- Molecules (e.g. CO, CS)
- Dust
- Cosmic ray particles
- Magnetic fields
- radiation fields

Interactions within the ISM



Processes in the ISM from G. Knapp, Sky & Telescope 2001

Energy transfer in the ISM

Heating mechanisms:

- Photoionization of neutral particles
- Cosmic ray ionization of H₂
- Photoeffect on dust particles
- Photodissociation of molecules
- Excitation of H₂ by UV radiation and collisional deexcitation
- Chemical heating
- Dissipation of turbulence and shocks
- Potential energy released by the gravitational collapse of a molecular cloud

Energy transfer in the ISM

Cooling mechanisms:

- Free-free emission of electrons in HII regions
- Recombination of ionized particles
- Collisional excitation with emission of radiation
- Collisions of gas particles with dust

Different phases of the ISM

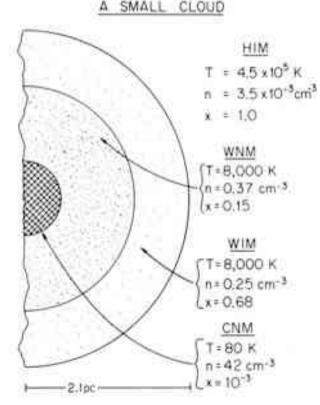
- •The balance of heating and cooling processes determine the temperature and thus the phase of the ISM
- different phases coexist in pressure equilibrium

p = nkT

with the pressure p, the number density n, Boltzmann's constant n and temperature T

three phases:

- a hot phase (shocked gas from supernova explosions, coronal gas)
- a warm phase (atomic hydrogen and ionized hydrogen gas)
- a cold phase (molecular and atomic hydrogen gas and dust)



different phases of the ISM from McKee & Ostriker 1977

Star formation

- Two categories: low-mass (M<8 M_{\odot}) star formation
 - high-mass star formation
- problems for the investigation of massive star forming regions:
 - larger distance and smaller number,

 - heavily extincted,
 short evolution time scales,
 dynamic and complex environments

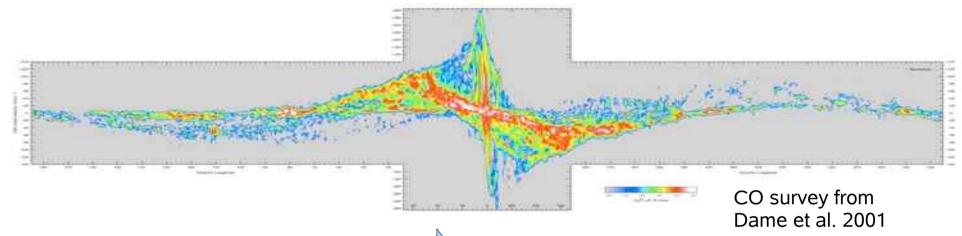
Initial conditions of star formation

Low-mass stars:

- fragmentation of clumps in dark clouds into prestellar cores, identified as Bok Globules in the optical (Bok & Reilly 1947)
- diffuse, cold clouds with low mass and column density (Lombardi & Alves 2001)
- formation of protostars by contraction of dense, compact cores with (Myers & Benson 1983)
 - temperatures of ~ 10 K
 - sizes of ~ 0.05 pc
 - masses of $0.5-5\,M_\odot$
 - densities of 10⁵-10⁶ cm⁻³

High-mass star formation

Giant molecular clouds (GMCs)



- large scale CO surveys formation of massive stars in GMCs
- diameters of 10-100 pc, masses of $10^{5-6.5} M_{\odot}$, mean densities of several 100 cm⁻³ (Stutzki & Guesten 1990)
- possess substructures:
 - clumps \longrightarrow overdense structures, which could form whole clusters, radii about 3-5 pc and masses of 10^3 - $10^4 M_{\odot}$
 - cores could form individual stars or multiple systems

Initial stages of massive star formation

- early known stages:
- hot cores: compact, infrared-bright regions with densities of ~ $10^7 \, \text{cm}^{-3}$, temperatures of $\geq 100 \, \text{K}$, a diameter of ~ 0.1 pc and total mass of several hundred M_{\odot}
- HII regions: ionization of the remaining molecular cloud surrounding a massive protostar, diameters of ≥ 10^{18} cm and densities of ≤ 10^{4} cm⁻³, associated with free-free continuum observed in cm surveys (Palla et al. 1991)
- young stellar objects < 10⁵ years can be traced by water and methanol maser surveys (Walsh et al. 1997, 1998, 2003)

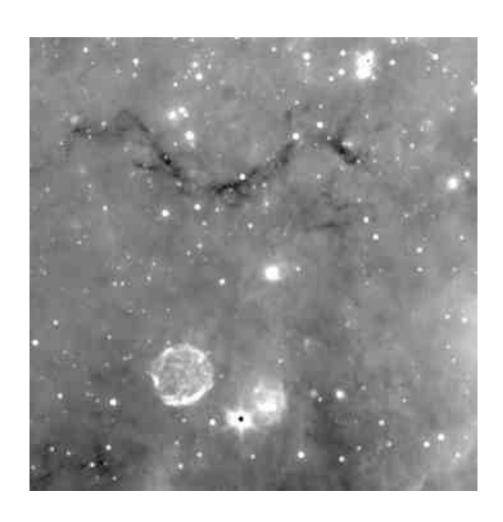
Initial stages of massive star formation

- still unknown: youngest massive protostars
 - (sub)mm dust continuum
 - high-density molecular tracer
- lack of temperature and velocity
 spectral line emission is necessary
- obtaining: linewidth,
 velocity kinematic distances
 mass & luminosity

Infrared Dark Clouds (IRDCs)

- earliest, cold phases are deeply embedded not probed in the mid-infrared
- extinction features against mid-IR background
- first detection by ISO and MSX (Perault et al. 1996, Egan et al.1998)
- Largest 1.2 mm-dust continuum survey of IRDCs by Rathborne et al. (2006)

IRDC11-00



Interstellar molecules

- beginning of molecular astrophysics in 1930s: discovery of CH, CH⁺ and CN in diffuse clouds
- detection by absorption of optical light from background stars
- extension to more complex species, many found in dense cores, in shock-heated regions of Orion, Sagittarius B2 at the Galactic center and in envelopes of evolved, giant stars
- in 1960s: discovery of OH, NH₃, H₂CO and H₂O
- in 1970s: H₂ and CO were identified
- to date over 100 molecules have been found

Abundances and properties of some molecules

- H_2 : the major constituent of cold interstellar clouds as well as hotter environments, e.g. clouds irradiated by a luminous star or shocked by a stellar wind, abundance X=1
- CO : $X = 8 \cdot 10^{-5}$, best observed at 2.6mm, low density tracer ($n\sim 10^3$ cm⁻³)
- OH : $X = 3 \cdot 10^{-7}$, detected at 18 cm, magnetic field probe
- NH₃ : $X = 2 \cdot 10^{-8}$, inversion transitions at 1.3 cm, low temperature probe at high densities (n~10⁵ cm⁻³)
- H_2 CO: X= 2•10⁻⁸, detected at 2.1 mm, high density probe (n~10⁶ cm⁻³)
- CS : $X = 1 \cdot 10^{-8}$, transition at 3.1 mm, high density probe $(n\sim 10^5 \text{ cm}^{-3})$

Conditions of molecular clouds

Cloud equilibrium and stability

- Theoretical model for a molecular cloud:
- uniform-temperature sphere supported by internal pressure against self-gravity with a maximum possible mass, the Jeans value
- Clouds with masses exceeding this limit gravitational collapse
- all observed clouds larger than dense cores
 masses exceeding the Jeans limit, but not collapsing
- assuming all clouds are gravitationally instable, one would expect a star forming rate of $\sim 25~M_{\odot}$ year⁻¹ in our Galaxy, but the observed rate is $\sim 5M_{\odot}$ year⁻¹



most clouds not instable, a stabilizing support

Conditions of molecular clouds

Fragmentation of large- and small-scale structures

- spiral arms of the Galaxy of 10 kpc
- giant molecular clouds of 1 kpc
- molecular clouds of 10 pc
- molecular cores of 0.1 pc
- protostars of 100 AU
- large-scale structures: from spiral arms to molecular clouds, stabilized by thermal, rotational, turbulent and magnetic support
- small-scale structures: molecular cores and protostars, supported by thermal and magnetic pressure

Cloud equilibrium and stability

- kinetic energy of each gas particle, $\frac{3}{2}$ kT with temperature T and Boltzmann constant k, produces a gas pressure which opposes gravitational contraction
- virial theorem for a gravitationally bound cloud:

$$2T + 2U + W + M = 0$$

with the total kinetic energy $T=\frac{1}{2}\,\text{mv}^2$, the energy contained in random, thermal motion $U=\frac{3}{2}\,\text{PV}_{cl}$ with cloud volume V_{cl} , the gravitational energy $W\sim\frac{-M^2}{R}$,

the magnetic energy $M \sim B^2 V_{cl}$

Cloud Support by Rotation

- angular momentum of molecular clouds originates from the ISM and the rotation of the Galaxy, coupling by magnetic fields and shocks
- some angular momentum is lost by magnetic breaking:
- the magnetic field in the Galaxy penetrates molecular clouds
- it will be winded up by the rotation of a contracting cloud with increasing angular velocity

streched magnetic field lines produce opposite angular momentum and reduce the angular velocity of the cloud which remains nearly constant

• assumption of solid rotation of a very dense contracting cloud due to friction at high viscosity constant angular velocity

$$F_z = m \omega^2 R$$
 and $F_G = \frac{GmM}{R^2}$

- the collapse cannot be prevented by rotation within the radius, where centrifugal force F_z equals gravitational force F_G
- outside this radius: collapse proceeds only partially is disk formation

Cloud Support by Turbulence

- the average thermal velocity of molecules is 1-10 km s⁻¹, while observed velocities of interstellar clouds are 10-100 km s⁻¹
- the motion of interstellar gas is influenced by turbulence and compression in gerenal
- the decay time of turbulence can be smaller than the free-fall time during stellar collapse
- follow-up shocks will disperse the clump before it can form protostellar cores
- Theoretically, turbulences should be dissipative. However, observations show well ordered magnetic fields over the dimensions of the clouds which prevents turbulence from dominating over magnetic fields.

Cloud Support by magnetic fields

- molecular clouds are partially ionized the gas is a very good conductor, the magnetic field lines tethered to the gas
- the contraction of the cloud brings together adjacent field lines and results in a larger field strength, as
 B ~ R⁻²
- the increase of B with density is called flux freezing
- the field tension and the magnetic pressure gradient rise

these forces together with an increased gradient in the thermal pressure can oppose self-gravity

Instabilities in the interstellar gas

• non-equilibrium processes in the IS gas transform that gas from the low interstellar density (~ 10⁻²³ g cm⁻³) to high stellar density (~ 10² g cm⁻³)

Gravitational instability ("Jeans instability")

Two forces on a volume element of 1 cm³ in a spherically symmetric mass distribution:

- The inwards directed gravitational force $F_g = G \rho M R^{-2}$ with the density ρ , the constant of gravitation G and the mass M within the distance R
- The outward directed force due to the pressure gradient $F_p = \frac{dP}{dr}$ with $P = \rho T \frac{R_g}{\mu}$ (μ mean molecular weight, R_g gas constant):

Gravitational instability ("Jeans instability")

$$F_{p} = \frac{d}{dr} (T \rho R_{g} \mu^{-1}) = TR_{g} \mu^{-1} \frac{d \rho}{dr}$$

Then, the equation of motion is

$$\frac{d^2r}{dt^2} = -\frac{GM}{R^2} - \frac{R_gT}{\mu} \frac{1}{\rho} \frac{d\rho}{dr}$$

The gas will start to contract for negative acceleration

$$\frac{GM}{R^2} > \frac{R_g T}{\mu} \frac{1}{\rho} \frac{d\rho}{dr}$$

using the approximation $\frac{d\rho}{dr} = \frac{\rho}{R}$ and $R = (\frac{3}{4\pi} \frac{M}{\rho})^{\frac{1}{3}}$

$$M_{Jeans} = \left(\frac{3}{4\pi}\right)^{\frac{1}{2}} \left(\frac{R_g T}{\mu G}\right)^{\frac{3}{2}} \left(\frac{1}{\rho}\right)^{\frac{1}{2}}$$

is the Jeans mass, the critical mass of instability for contraction or the minimum mass of contraction for the ambient values of T, ρ and μ

- for IS clouds with neutral hydrogen : $M_{leans} \sim 10^5 M_{\odot}$
- for dense molecular clouds: $M_{leans} \sim 25 M_{\odot}$

Thermal instabilities

Energy balance in the ISM is determined by

- processes of energy input and output
- proceeses of heating and cooling (radiation)

Increase of density ρ of a gas volume element by random or superimposed fluctuations to ρ +d ρ .

- effective cooling decreases the temperature T by an amount dT the pressure will decrease with respect to the surroundings compression of the volume element
- effective cooling: fast emission of energy gain from contraction increase of density and formation of instability
- thermal instability: cooling is more efficient than heating, when

$$t_c < t_h$$

with the cooling time t_{c} and heating time t_{h} .

• exponential increase of density fluctuations with the cooling time scale

Ambipolar diffusion

- magnetic pressure as a major support of molecular clouds, but much smaller magnetic energy per unit mass of a star than in the ISM
- ambipolar diffusion \implies explanation of reduced influence of the magnetic field
- co-existence of ions, electrons and neutral particles in a molecular cloud with ratio of charged to neutral particles ~ 10⁻⁷
- coupling of the magnetic field to the charged particles by electromagnetic forces, coupling of charged particles to the neutral component by viscous forces
- movement of the molecular cloud relative to the magnetic field separation of charged particles and decoupling of the magnetic field from the neutral gas

formation of a cloud core consisting of neutral gas without magnetic forces

problems: - poorly known degree of ionization or dependence from density
 - support of clouds by magnetic forces perpendicular to magnetic lines contraction of plasma along the magnetic lines and formation of a disk with efficient cooling further contraction

Cloud collapse

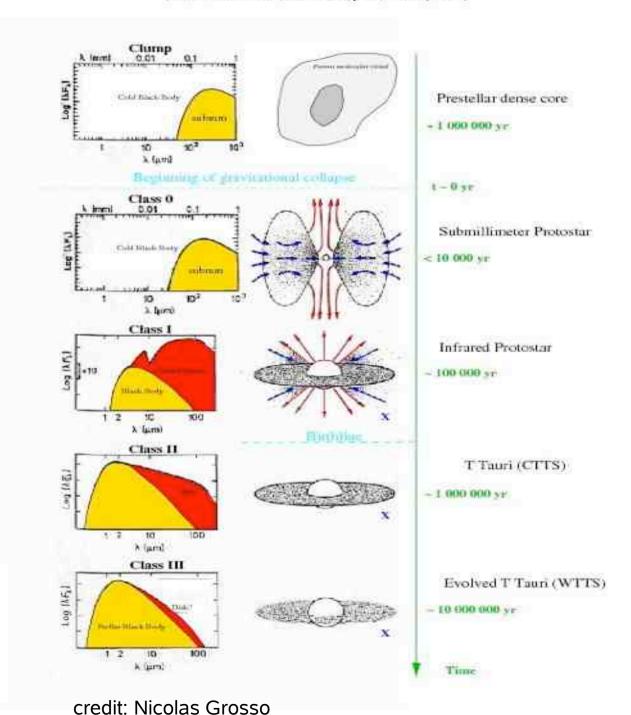
- star formation in the densest parts of molecular clouds high extinction by associated dust avoids observations process described only theoretically
- gravitational force dominates that of thermal and magnetic pressure
- beginning of contraction, increase of density towards the centre
- free-fall collapse time proportional to $(G\rho)^{-1/2}$ \Longrightarrow smaller in the interior
- inside-out-collapse: interior begins to collapse before the outer regions
- observations of dense cores in CO and at higher densities in NH₃
- end of collapse in a protostar, which pulls in cloud material by its gravitational attraction

Infrared/Submillimeter Young Stellar Object Classification

(Lada 1987 + André, Ward-Thompson, Barsony 1993)

Low-mass star formation

- compact cores in diffuse cold dark clouds
- deeply embedded protostars, strong accretion, collimated outflows
- emerging protostars (I.R.) accretion, increase of mass, heating, outflows
- young stellar objects, less embedded, thick disk
- pre-main sequence or young main sequence stars
- thin disk

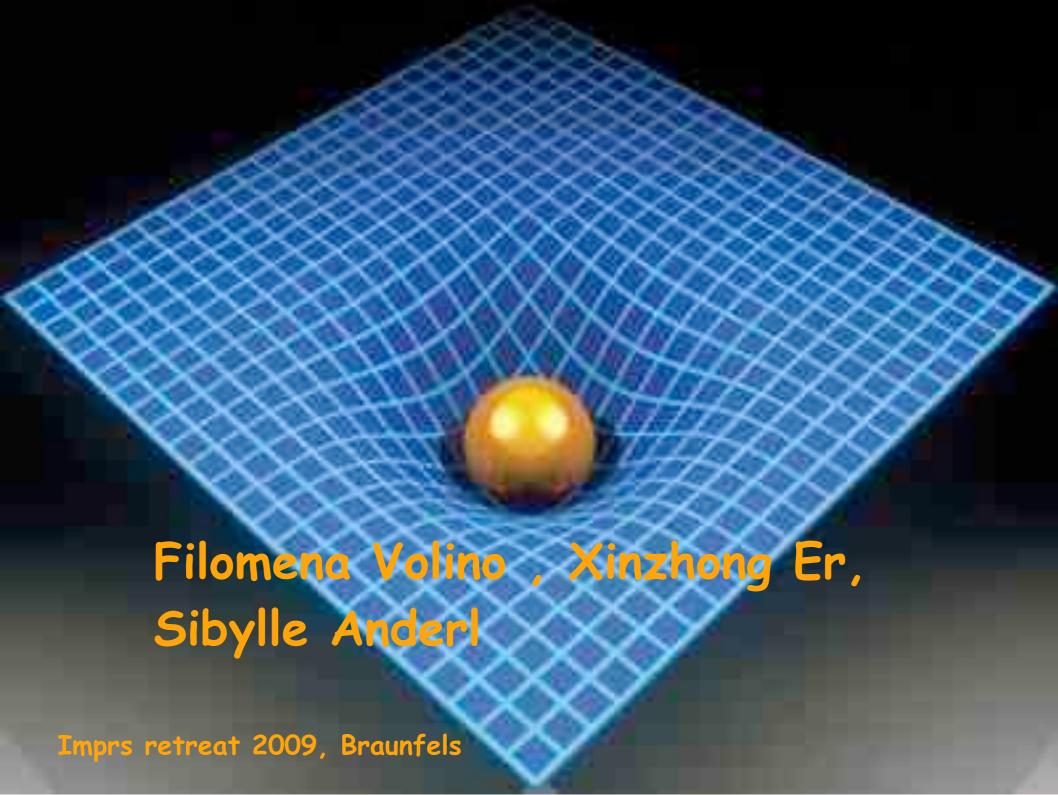


High-mass star formation

- theoretical problems compared to low-mass s.f.: radiation pressure halts infall
- two different main models:
 - high accretion rates through disks (Padoan & Nordlund 2002)
 - merging to high-mass star in the centre of star clusters (Bonnell et al. 1998)
- observational evidence of
 - model I: strongly collimated molecular outflows indicating high accretion rates through disks (Beuther et al. 2002)
 - model II: concentration of most massive stars in regions of young stellar clusters (Zinnecker & Bate 2002)

Conclusion

- molecular clouds form out of the ISM and fragment into substructures such as clumps and cores
- some well known initial phases of star formation
- still unknown earliest phases of MSF
- most clouds in energetic equilibrium
- instabilities in the ISM can lead to cloud collapse
- better understanding of low-mass than high-mass star formation



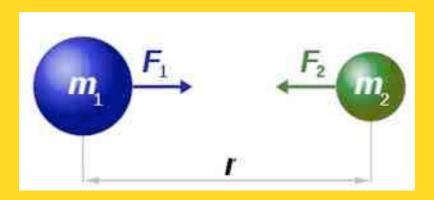
Outline

- · Gravity, from Newton to Einstein
- Framework of GR
- Cosmological principle
- Relativistic cosmology

Newtonian gravity

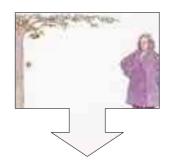
$$F_{1}=m_{1}x_{1}=G\frac{m_{1}m_{2}}{|x_{1}-x_{2}|^{2}}\frac{x_{2}-x_{1}}{|x_{1}-x_{2}|}$$

$$F_{2}=m_{1}x_{2}=G\frac{m_{1}m_{2}}{|x_{1}-x_{2}|^{2}}\frac{x_{1}-x_{2}}{|x_{1}-x_{2}|}=-F_{1}$$



why do we need new theory of gravity??

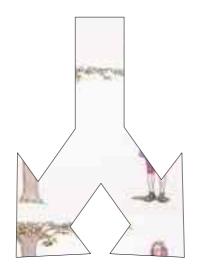
- 1865 J.C. Maxwell, electromagnetism
- •search for 'ether', *luminis feris*
- •contraction of length and slow down of a clock when moving through ether!! (Lorentz, Fitzgerald, Poincare', 1895)



hypothesis not verifiable!!

why do we need new theory of gravity??

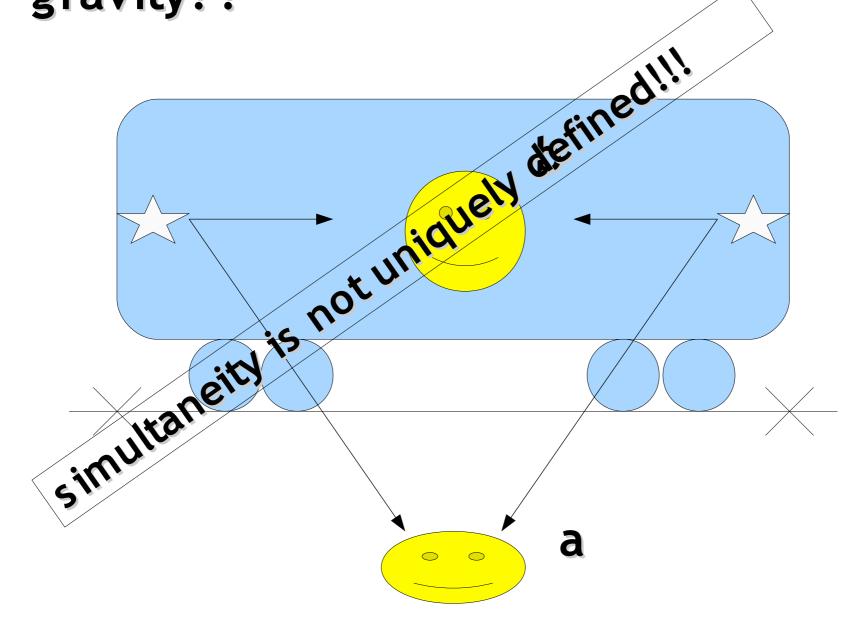
special relativity (Einstein, 1905)



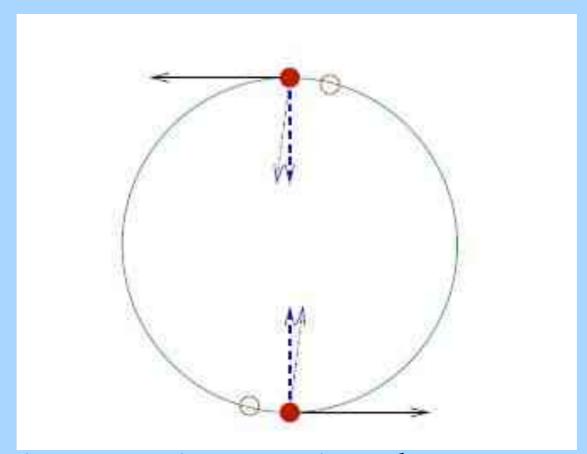
all observers are equivalent as far as dynamical experiments

constancy of velocity of light (quite heuristic statement for the time!!)

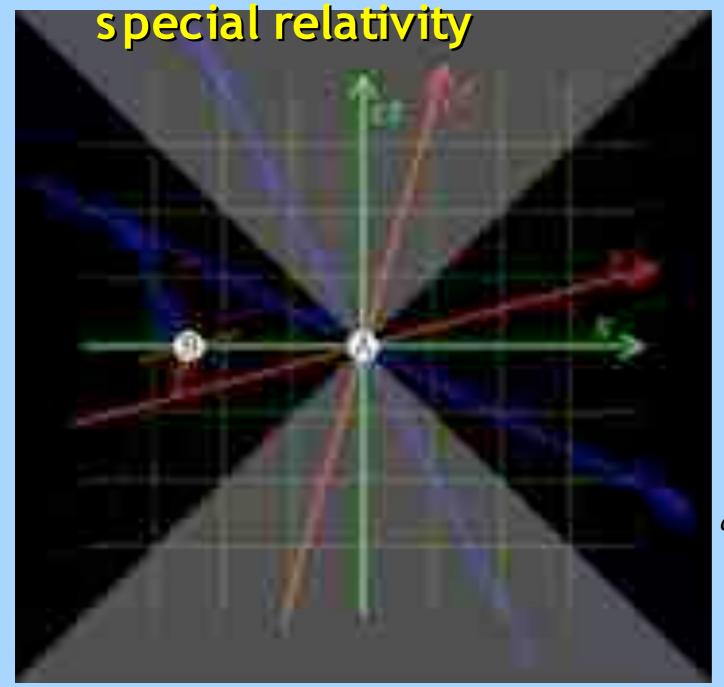
•why do we need new theory of gravity??



•why do we need new theory of gravity??



inconsistencies between Newtonian gravity and SR



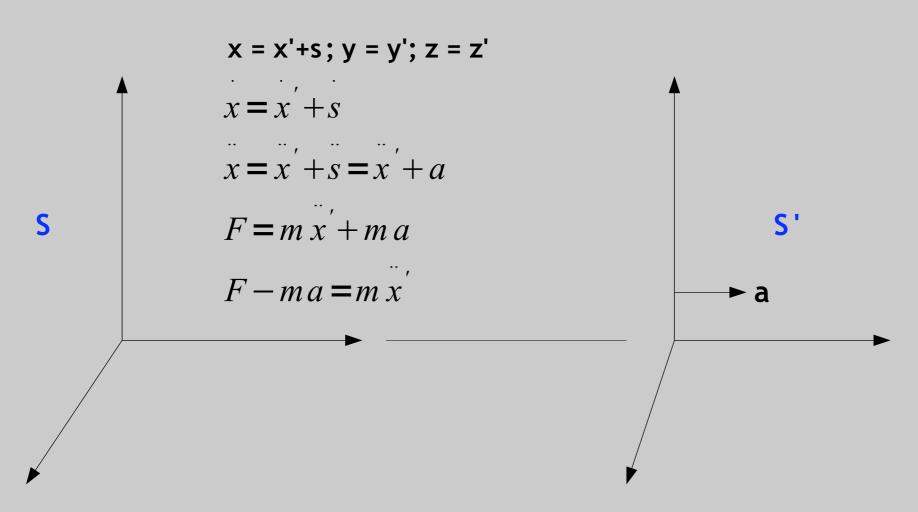
- space and time merge together and form a four continuum spacetime
- the interval
 between 2 events
 P(t,x,y,z) and
 P'(t+dt,x+dx,y+dy,z+dz) is

$$ds^2 = dt^2 - dx^2 - dy^2 - dz^2$$

•Minkowsky spacetime

general relativity

(or, investigating Newton's second law in a non inertial frame)



in S' the body experiences the 'additional' inertial force

- · How do we detect an inertial frame?
- Observer in absolute acceleration respect the absolute space
- *No meaning to the notion of 'motion', only to the notion of 'relative motion'
- •A body in an empty space cannot be said in motion

Mass to define an inertial frame!

general relativity

(or gravity as inertial effect!)

- •All inertial forces in Newtonian theory are proportional to the mass of the body experiencing them
- •If we drop 2 bodies in the Earth's gravitational field, then they experience m₁g and m₂g.
- Gravity arises when using a non inertial frame



The principle of equivalence

A frame linearly accelerated relative to an inertial frame in special relativity is locally identical to a frame at rest in a gravitational field (Gedankenexperiment)

- The motion of a gravitational test particle in a gravitational field is independent of its mass and composition
- The gravitational field is coupled to everyhting

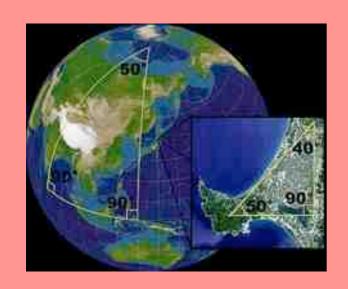
theory	position	veocity	Time	Acceleration
newtonian	relative	relative	absolute	absolute
SR	relative	relative	relative	absolute
GR	relative	relative	relative	relative

•<u>All</u> reference systems are equivalent!!(or all physical laws can formulated in a way which is equivalent for all r.f. or coordinates)

- 1st summary Special relativity vs GR
- ·All inertial reference frames are equivalent
- Mass energy equivalence
- Linearly accelerated field relative to an inertial frame is equivalent to a frame at rest in gravitational field
- ·Gravity and acceleration are locally equivalent

all observers are equivalent (all observers must be capable to discovery law of physics) or all physical law should have a tensorial form

Mathematical framework of GR



in Newtonian theory
it is used the
formalism of
vectors, in GR it is
used the formalism
of tensors

A sphere is a 2-dim manifold: it can be represented by collection of 2-dim maps

Space-time is 4-dim manifold

$$x^{\mu} = (x^{0}, x^{1}, x^{2}, x^{3})$$

Mathematical framework of GR

Many physical quantities are regarded as correspondences between sets of vectors (input vector- tensor - output vector)

Tensors as expression of relationship between vectors:

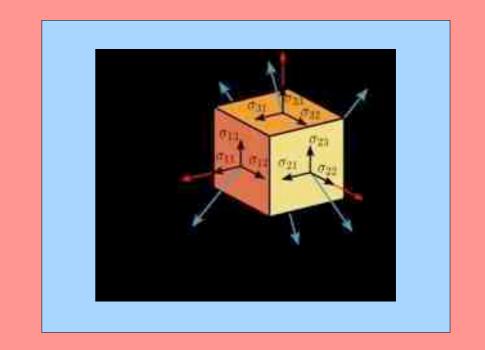
Independent on the coordinate system!!

$$\sigma_{11} \quad \sigma_{12} \quad \sigma_{13}$$

$$\sigma = \sigma_{12} \quad \sigma_{22} \quad \sigma_{23}$$

$$\sigma_{13} \quad \sigma_{23} \quad \sigma_{33}$$

$$\sigma = T^{(e_1)} \quad T^{(e_2)} \quad T^{(e_3)}$$



Tensor metric

$$a^2 := g_{\mu\nu} dx^{\mu} dx^{\nu}$$

Length of a vector

$$ds^2 = g_{\mu\nu} dx^{\mu} dx^{\nu}$$

Interval between 2 neighbouring points

For polar coordinates:
$$ds^2 = dr^2 + r^2 d\phi^2$$
 $g = \begin{bmatrix} 1 & 0 \\ 0 & r^2 \end{bmatrix}$

$$g = \begin{cases} 1 & 0 \\ 0 & r^2 \end{cases}$$

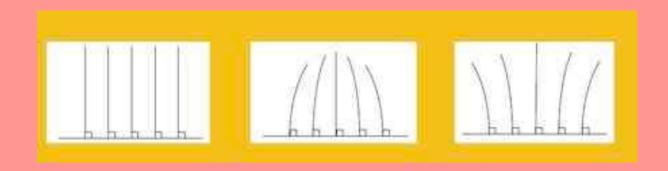
Minkowsky space:

$$ds^{2} = dt^{2} - dx^{2} - dy^{2} - dz^{2} \quad g = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$$

$$g = \begin{pmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix}$$

Geodesic equation

- •Shortest curve connecting 2 fixed points (straight line as closely as possible in local inertial frame)
- Trajectory of freely falling particles



How does it change the distance between 2 neighbouring points??

Geodesic equation

In a curved space time, particles moving along geodesics will accelerate towards or away from each other



Curvature tensor describes gradient of gravitational accelerations, the so called 'tidal forces'

^{2nd} summary Geodesic equation

In Newtonian theory gravitational field (gradient of potential) is source of acceleration
In GR curvature is source of tidal effect, thus acceleration

Curvature (metric) as potential

What's the source of gravity??

•Equivalence mass-energy

$$T^{\mu\nu}(x^{\alpha}) = \rho_0(x^{\alpha}) < U^{\mu}U^{\nu} > (x^{\alpha})$$

(transport of µ momentum in the direction v)

 $T^{\mu\nu}$ as source of gravity!!

$$G^{\alpha\beta} = k T^{\alpha\beta}$$

Die größte Eselei

 empty Minkowsky space-time as the only possible solution for a static Universe

$$G^{\alpha\beta} + \Lambda g^{\alpha\beta} = k T^{\alpha\beta}$$

expansion of the Universe

$$G_{\alpha\beta} = -\Lambda g_{\alpha\beta} + k T_{\alpha\beta}$$

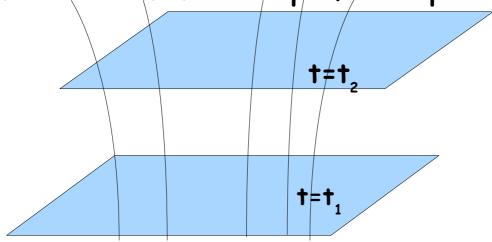
(dark energy)

The cosmological principle

- Copernican principle, 'the Earth does not occupy a special place in the Universe
- S moothed on large scale the Universe appears is otropic and homogeneus
- Existence of <u>foundamental</u> observers at rest respect the mean motion of nearby matter (Weil's postulate,1923)

cosmological principle, it leads to the RW metric by simple symmetry considerations:

1 set of observers on the first hypersurface; not to violate the assumption of homogeneity all the observers must reach the 2nd hypersurface in the same time; also their velocity must be orthogonal in order to keep the homogeneity at cosmic time t (otherwise there would be a prefered spatial direction).



$$c^2 d\tau^2 = (cdt)^2 - d\Sigma^2(t)$$

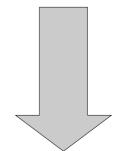
$$c^2 d\tau^2 = (cdt)^2 - d\Sigma^2(t)$$

$$\Delta \Sigma^2 = \gamma_{ij}(x^k) \Delta x^i \Delta x^j$$

$$\gamma_{ij}(t, x^k) = a^2(t)\sigma_{ij}(x^k)$$



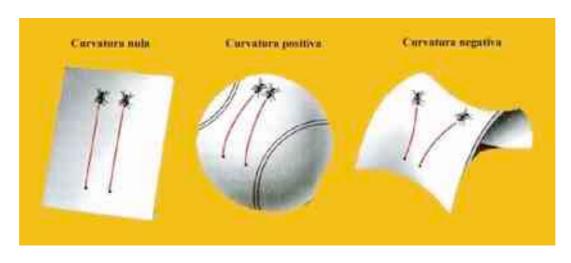
The ratio of distances at later time must be independent of x^k and Δx^k !! (not to violate homogenity)



The time evolution of threedimensional metric is uniform in space

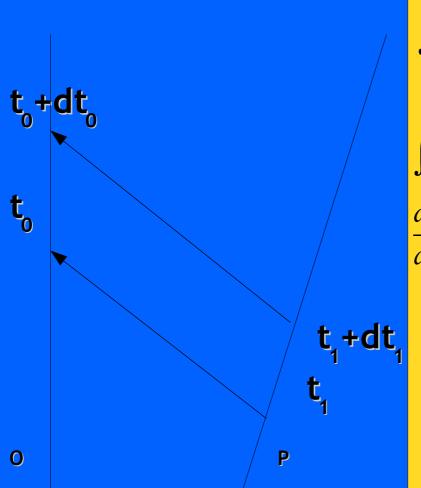
$$c^{2}d\tau^{2} = (cdt)^{2} - a^{2}(t)\sigma_{ij}(x^{k})dx^{i}dx^{j}$$

$$d\sigma^{2} = \frac{dr^{2}}{1 - k r^{2}/R^{2}} + r^{2}(d\theta^{2} + \sin^{2}(\theta)d\phi^{2}) = \frac{dr^{2}}{1 - k r^{2}/R^{2}} + r^{2}d\Omega^{2}$$



$$K = 0$$
 $K = 1$ $K = 1$

Propagation of light



$$\int_{t_1+dt_1}^{t_0+dt_0} \frac{dt}{a(t)} = \int_{t_1}^{t_0} \frac{dt}{a(t)}$$

$$\int_{t_1+dt_1}^{t_0+dt_0} \frac{dt}{a(t)} - \int_{t_1}^{t_0} \frac{dt}{a(t)} = \int_{t_0}^{t_0+dt_0} \frac{dt}{a(t)} - \int_{t_1}^{t_1+dt_1} \frac{dt}{a(t)} = 0$$

$$\frac{dt_0}{a(t_0)} = \frac{dt_1}{a(t_1)}$$

$$t_0 > t_1 \rightarrow a(t_0) > a(t_1)$$

 $1 + z = v_1/v_0 = a(t_0)/a(t_1)$

Propagation of light

for small distances:

$$\begin{aligned} &t_0 \! \approx \! t_1 \! + \! dt \\ &1 \! + \! z \! = \! \frac{a(t_0)}{a(t_0 \! - \! dt)} \! \simeq \! \frac{a(t_0)}{a(t_0) \! - \! a(t_0) dt} \! \simeq \! 1 \! + \! \frac{a(t_0)}{a(t_0)} dt \\ &z \! \simeq \! a(t) r \end{aligned}$$

Interpreting z as veleocity of recession

redshift proportional to distance r!!

Relativistic cosmology

- cosmological principle ====>> Robertson-Walker metric (metric of space-time)
- ·Weyl's postulate (existence of perfect fluid)
- ·General relativity with cosmological term

$$\frac{-k + a^2 + 2aa}{a^2} + \Lambda = 8\pi p; 3\frac{k + a^2}{a^2} - \Lambda = 8\pi \rho$$

By homogeneity, density and pressure can only be function of time!!

Relativistic cosmology

$$8\pi \frac{d(\rho a^3)}{dt} = -3a^2a8\pi p$$
 Conservation of energy!!

Friedmann's equations are consistent with conservation of energy (field equation were actually designed to be consistent with this!!)

Relativistic cosmology

$$\frac{-k+a^2+2aa}{a^2} + \Lambda = 8\pi p; 3\frac{k+a^2}{a^2} - \Lambda = 8\pi \rho$$

$$H^{2} = \frac{a^{2}}{a^{2}} = \frac{8\pi\rho}{3} + \frac{\Lambda}{3} - \frac{k}{a^{2}}$$

$$\rho_c = \frac{3}{8\pi} H^2$$

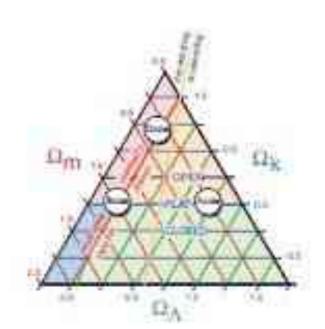
$$\Omega_M = \frac{\rho}{\rho_c}$$

$$\Omega_{\Lambda} = \frac{\Lambda}{3H^2} \Omega_M + \Omega_{\Lambda} + \Omega_k = 1$$

$$\Omega_M + \Omega_\Lambda < 1 \leftarrow k = -1$$

$$\Omega_M + \Omega_\Lambda = 1 \leftarrow k = 0$$

$$\Omega_M + \Omega_\Lambda > 1 \leftarrow k = 1$$



3rd summary Relativistic cosmology

RW metric describes pattern of galaxies (foundamental particles) redshift, Hubble's law

RW metric in Einstein's field equations: Freedman's equations, different cosmological models

Bilbiography

- •Introducing Einstein's relativity,
 - R. D'Inverno
- ·Chandra, Nasa

Olber's paradox (1826)
Why is the sky dark?
assuming:
the space is Euclidean and infinite

the average number of stars per unit of valume and the average luminosity of each star is constant throughout space and time (provided that these averages are taken over sufficiently large area)

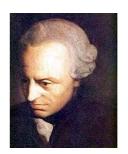
the Universe has been existing for an infinite time and it is static on large scale

The total luminosity would be infite!!!

$$\frac{(4\pi r^2 dr)l}{4\pi r^2} = l dr$$

Too young Universe or expanding Universe

Immanuel Kant, born in 22 April 1724, Koenigsberg, Prussia. Kant was the last influential philosopher of modern philosophy in the classic sequence of the theory of knowledge during the Enlightenment beginning with thinkers John Locke, George Berkeley and David Hume.



Immanuel Kant, wikipedia

(following relates to the point 1 and 2 of the other one)

One of Kant's most prominent works is the **Critique of Pure Reason**, an investigation into the limitations and structure of reason itself. He suggested that by understanding the sources and limits of human knowledge we can ask fruitful metaphysical questions. He asked if an object can be known to have certain properties prior to the experience of sensation of that object. He concluded that all objects about which the mind can think must conform to its manner of thought. For example, if you always wore blue spectacles, you could be sure of seeing everything blue. However, it is possible that there are objects not blue, or with such nature which the mind cannot know, so the principle in the "blue world" cannot be applied outside of experience.

Empiricists and Rationalists The empiricists believed that knowledge is acquired through experience alone, but the rationalists maintained that such knowledge is open to Cartesian doubt and that reason alone provides us with knowledge. Kant argues, however, that using reason without applying it to experience will lead to illusions, while experience will be purely subjective without first being subsumed under pure reason.

'a priori' and empirical An 'empirical' proposition is one which we cannot know except by the help of sense-perception, either our own or that of someone else whose testimony we accept. An 'a priori' proposition is one which though it may be elicited by experience, is seen, when known, to have a basis other than experience.

Space and time (point 4) According to Kant, the outer world causes only the matter of sensation, but our own mental apparatus orders this matter in space and time, so that anything would be impossible if space and time were not kinds of pure 'a priori' intuitions.(think about the geometry and mathematics)

After applying the space and time to things that are not experienced, Kant maintains, we find ourselves troubled by 'antinomies' –that is to say, by mutually contradictory propositions each of which can apparently be proved.

Antinomies (point 5 and 6)

- is it infinite of both space and time?
- every composite substance both is, and is not, made up of simple parts?
- two kinds of causality, one according to the laws of nature, the other that of freedom?
- there is, and is not, an absolutely necessary Being?

Snapshots from the life of an AGN

A.3 Equations...

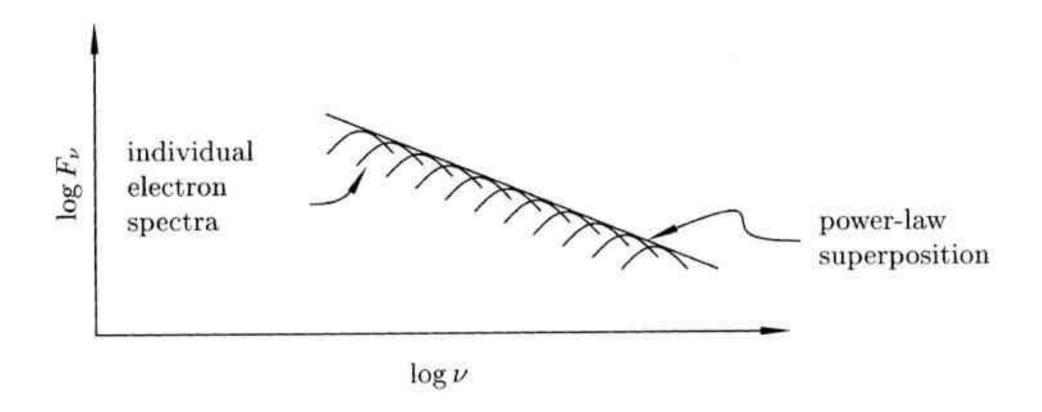
"Synchrotron Emission"

(A.1) Rusen Lu
(A.2) Marios Karouzos

(A.3) Chin-Shin Chang

IMPRS Retreat - 2009, Braunfels

15th September 2009



Snapshots from the life of an AGN

B.2 Milestone in....

"The accretion disk"

(B.1) Marios Karouzos (B.2) Chin-Shin Chang

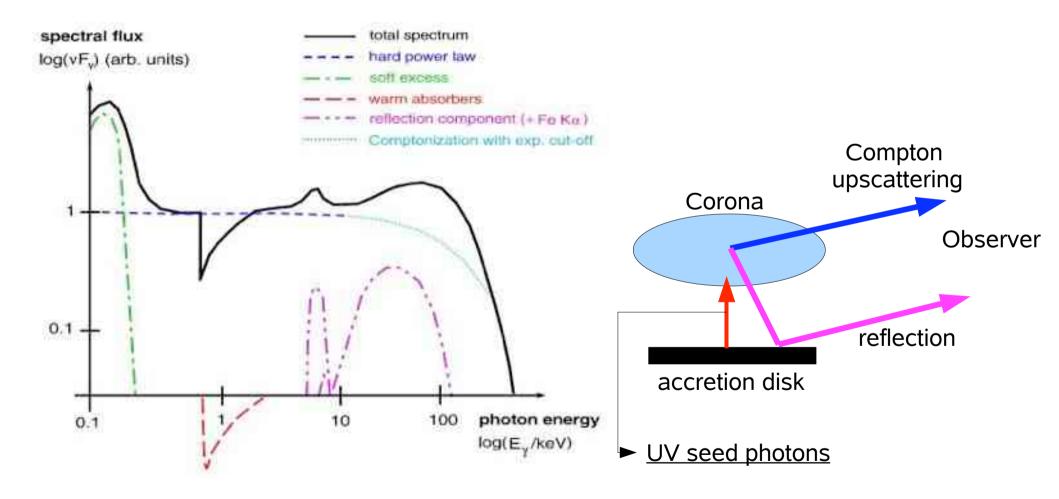
(B.3) Rusen Lu

IMPRS Retreat – 2009, Braunfels

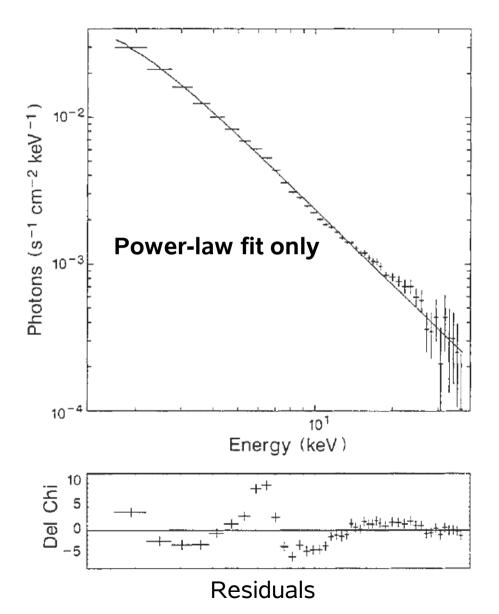
15th September 2009

X-ray observational evidence of AGN accretion disk

X-Ray: spectra and mechanism



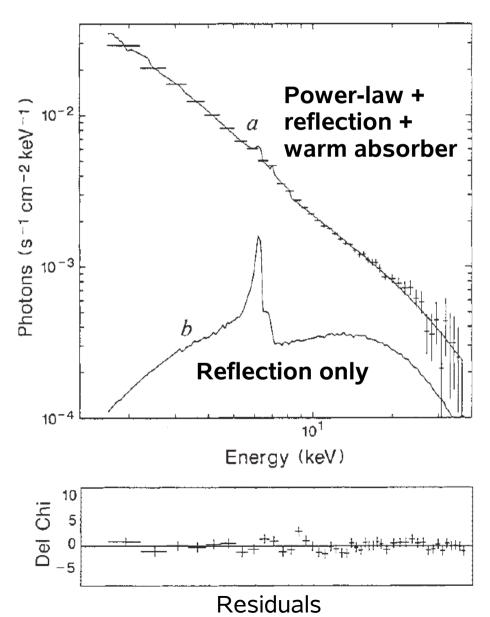
First evidence of accretion disk



- Exosat & Ginga satellites observations
- Power-law fit residuals show an excess around 6-7 kev
- Possible iron line

Pounds et al., 1990, Nature, 344,132

First evidence of accretion disk

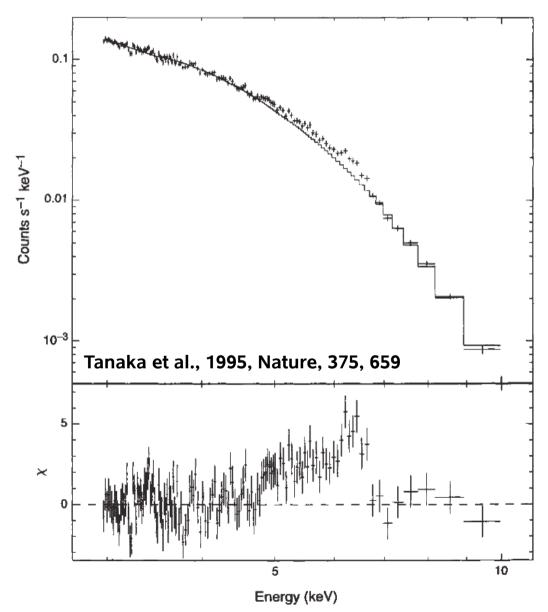


- Fit greatly improved by adding reflection component (+ Iron K-α line)
- Reveal cold, dense matter within 1000 gravitational radii
- Quantitative evidence for the reflected continuum component from this cold matter

Pounds et al., 1990, Nature, 344, 132

2009/09/15

Further evidence of accretion disk

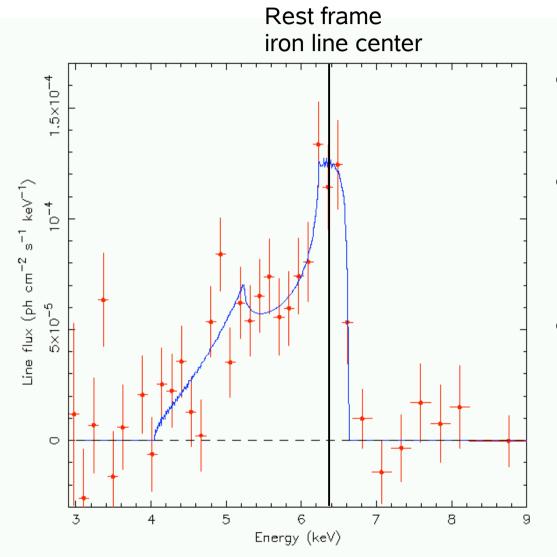


- ASKA observation of MCG-6-30-15
- Power-law +
 continuum reflection
 model: residual
 showed iron-line
 broadening

2009/09/15

Chin-Shin Chang

Iron line broadening



Tanaka et al., 1995, Nature, 375, 659

- The broad iron K-α line shows extensive red wing
- Suggests a Doppler and gravitational shifts close to a central black hole
- Best-fit line model: an externally-illuminated accretion disk orbiting a Schwarzschild black hole (Fabian et al., 1989, MNRAS, 238, 729)







Chin-Shin Chang IMPRS Retreat 2009 Braunfels

Snapshots from the life of an AGN

C.1 Introduction

"Superluminal motion"

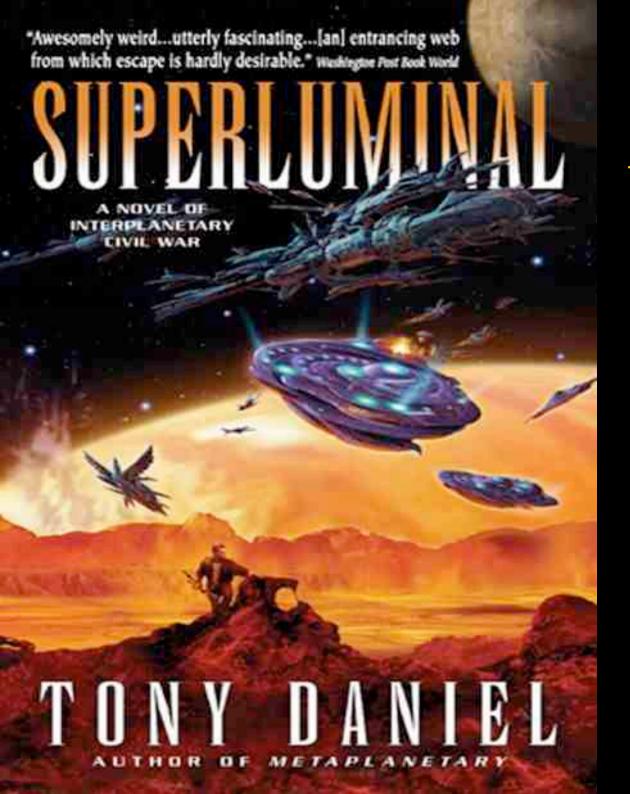
(C.1) Chin-Shin Chang

(C.2) Rusen Lu

(C.3) Marios Karouzos

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15th September 2009

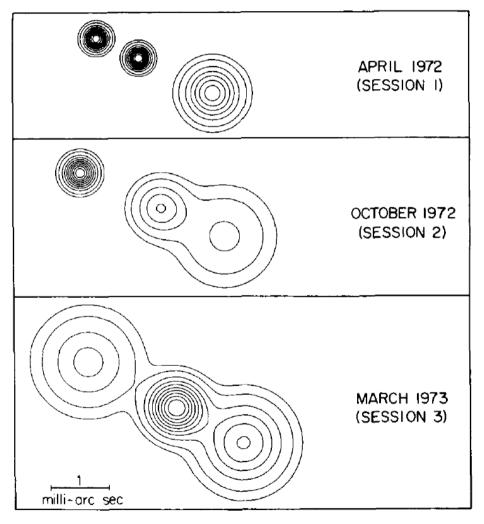


MOTION

Introduction

3C 273

- Very Long Baseline Interferometry (VLBI) observations starting from the 70s
- compact extragalactic sources made up of two or more components, which have speed faster than light ~ 2 - 4c



Cohen 1975

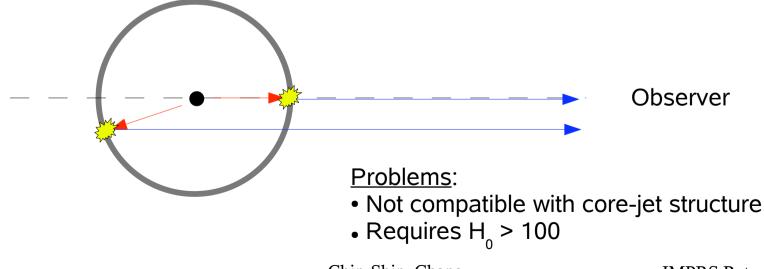
People were very excited and started to figure out why...

Let's take a look at some models on debate back then

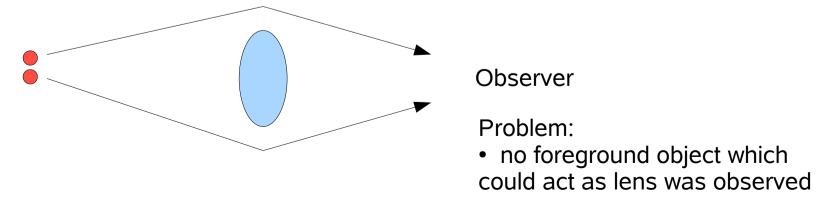
- Overestimate of distance
- Random fluctuations (Dent 1972)
 - Christmas tree model

<u>Problem</u>: expansions/contractions should be 50-50% statistically

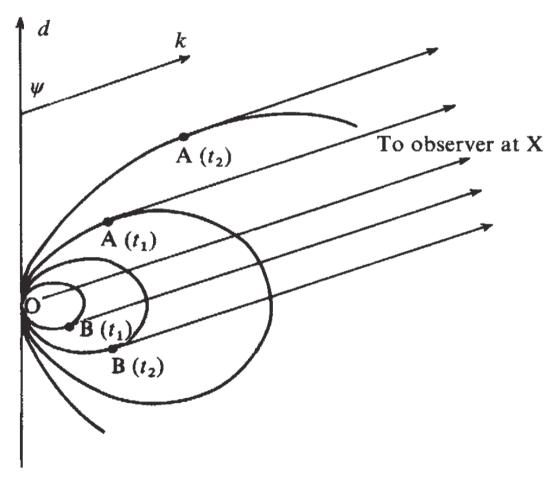
• Light-echo model (Lynden-Bell 1977):



- Phase effects
 - non-constant expansion velocities
 - frequency-dependent structure
- Gravitational lens
 - a subluminally moving source with a foreground galaxy could result in superluminal motion (Chitre&Narlikar 1979)



- Dipole field model
 - a burst of charged particles move along the field lines, forming a shell, which expands with relativistic velocities
- Opposite sides of the magnetic field tend to cancel out – in agreement with observation (weak circular polarization



 $H_0 < 60 \text{ km/s/Mpc}$

Milgrom 1978, Nature 274, 349

Relativistic bulk motions

Relativistic free expansion (Vitello & Salvati 1976)

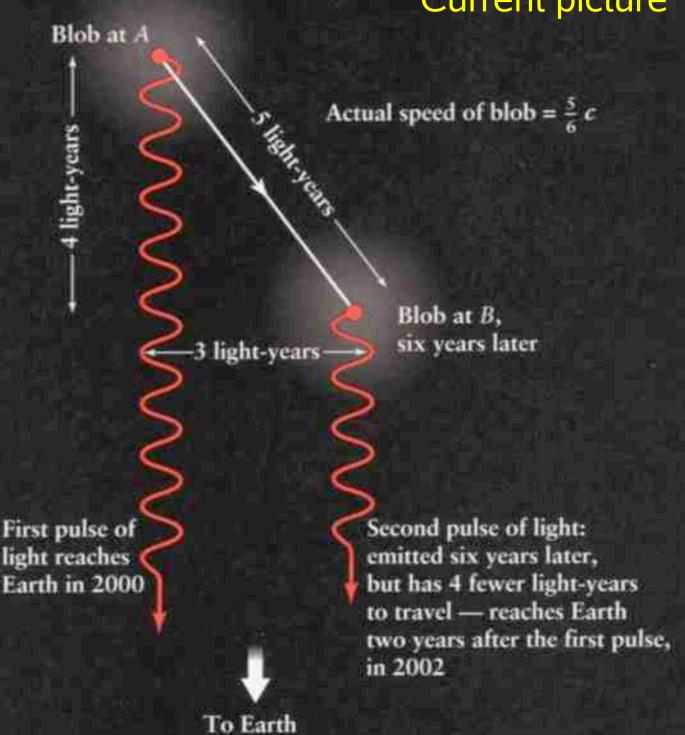
expansions constrained along one dimention can produce superluminal motion.

Problem: difficult to obtain two comparable components

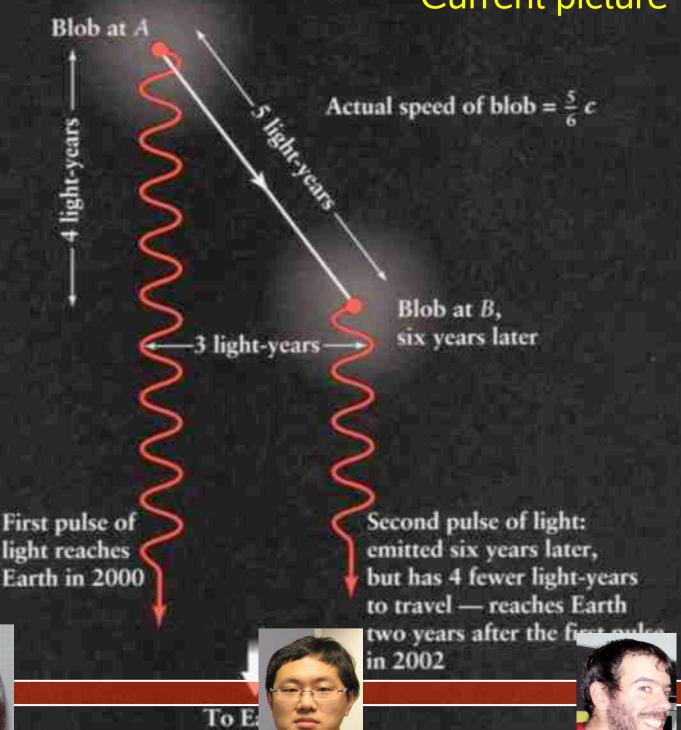
- Relativistic blast-waves
 - a large energy release in an ambient medium could leat to a relativistic blast-wave
 - Marscher (1978) and Shapiro (1979): isotropic explosion in a disk-confined ambient medium -> two superluminal radio components could be produced

<u>Problem</u>: blast waves should decelerate/accelerate, contradicts 3C 345 observation

Current picture

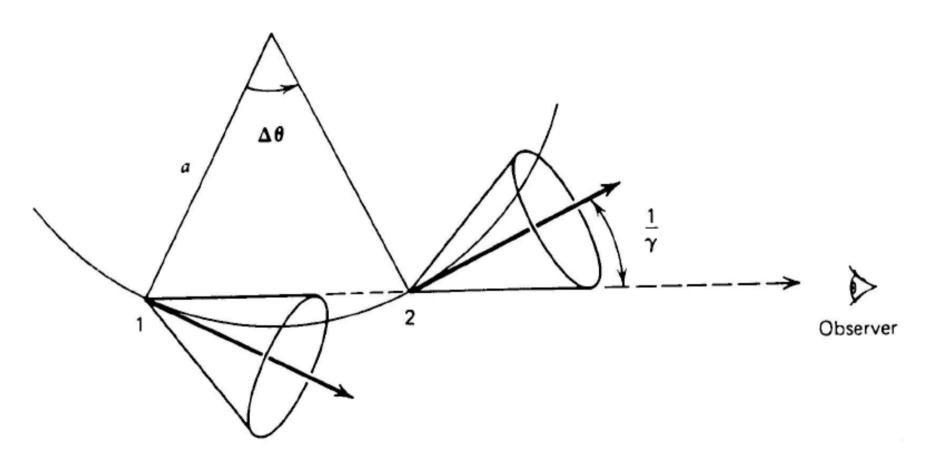


Current picture



References

- Marscher & Scott, 1980, PASP, 92, 127
- Milgrom & Bahcall, 1978, Nature, 274, 349



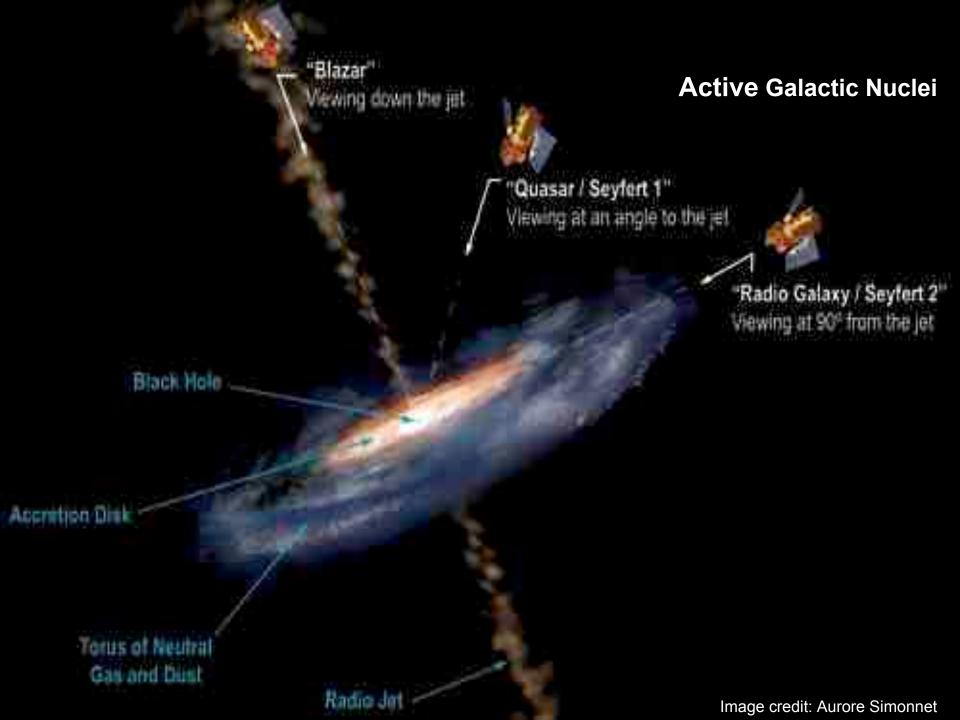
Rybicki & Lightman, Fig. 6.2

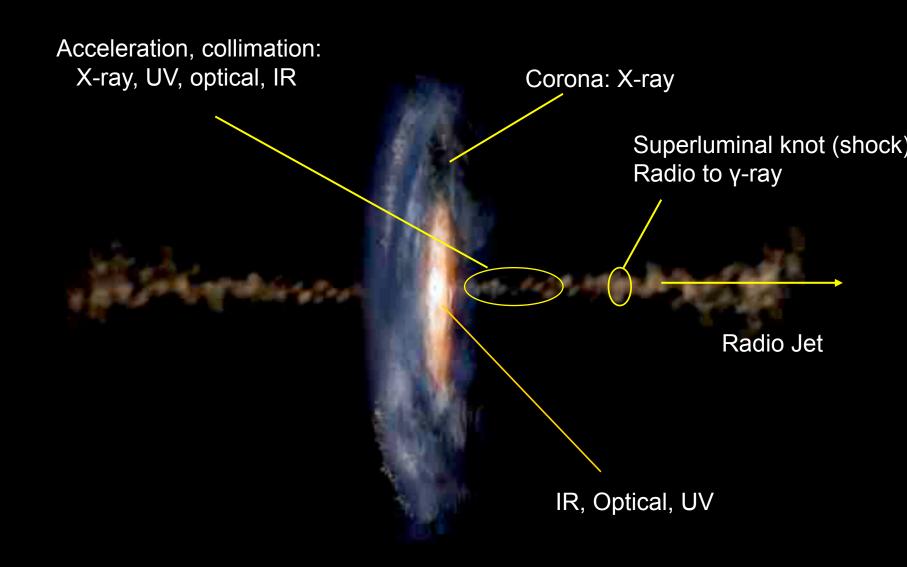


(A.1) Rusen Lu

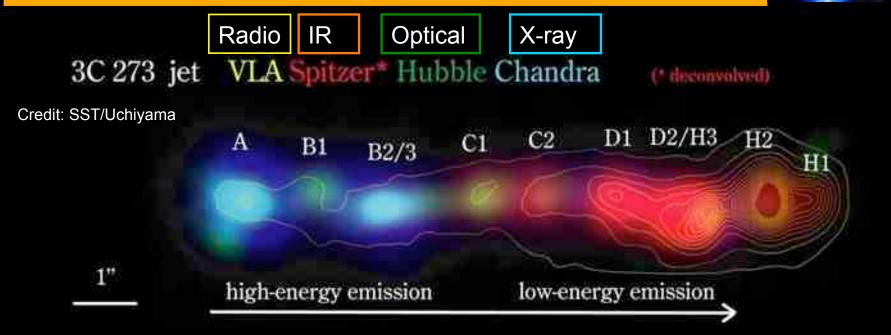
(A.2) Marios Karouzos

(A.3) Chin Shin Chang





AGN across the spectrum



Radio & mm: Jet

IR: jet base

Optical: jet base + BH region

UV: jet base

X-ray: jet +BH region

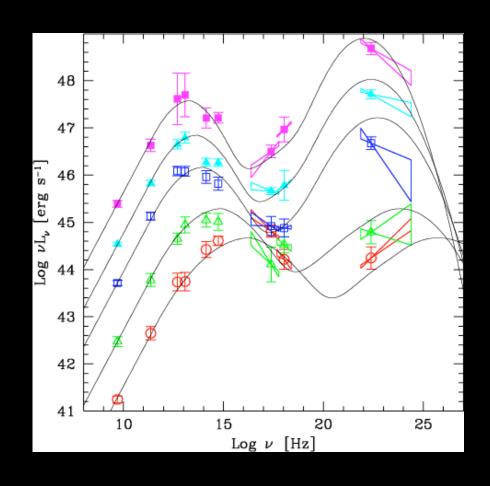
Gamma-ray: BH region + jet shocks

Emission mechanism of Blazars

SED: 2 peaks in μ -F(μ) plot

The first peaks in the UV-X-ray band for the HBL or in the NIR-optical band for the LBL and FSRQs.

The second peaks in the TeV band for the HBL and in the GeV band for the LBL.



Synchrotron and IC

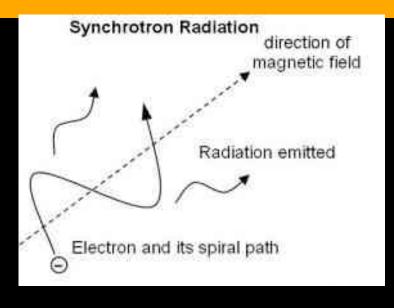
Named after its discovery in a synchrotron accelerator build in 1946_

Two of its characteristics include:

- (1) Non-thermal power-law spectrum
 - (2) Polarization.

Energy loss:

$$P_{
m syn} = rac{4}{3} \sigma_{
m T} c eta^2 \gamma^2 U_{
m B}$$

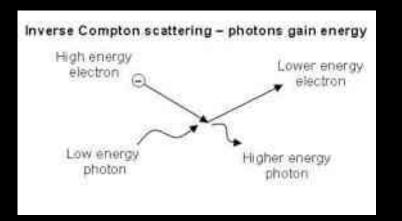


Average frequency of the up-scattered photo:

$$rac{\langle
u
angle}{
u_0} = rac{4}{3} \gamma^2$$

Energy loss:

$$P_{
m IC} = rac{4}{3} \sigma_{
m T} c eta^2 \gamma^2 U_{
m rad}$$



Synchrotron and IC

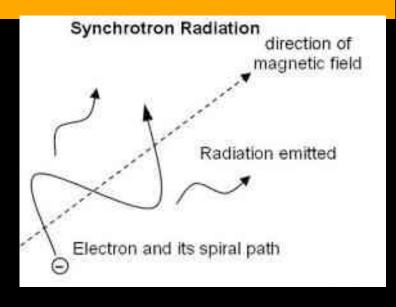
Named after its discovery in a synchrotron accelerator build in 1946_

Two of its characteristics include:

- (1) Non-thermal power-law spectrum
 - (2) Polarization.

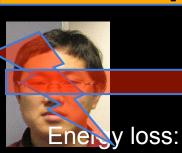
Energy loss:

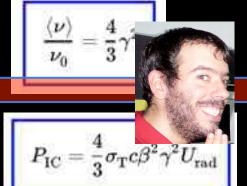
$$P_{
m syn} = rac{4}{3} \sigma_{
m T} c eta^2 \gamma^2 U_{
m B}$$

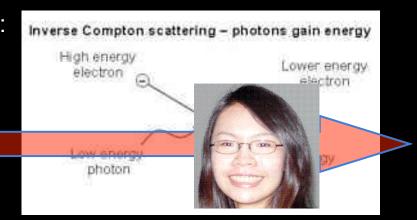


Road map:

y of the up-scattered photo:







Snapshots from the life of an AGN

A.2 Milestone in...

"Superluminal motion"

(C.1) Chin Shin Chang

(C.2) Rusen Lu

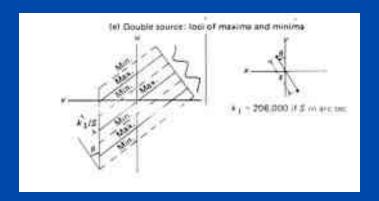
(C.3) Marios Karouzos

Discovery of superluminal motion in 3C 279 (Whitney et al. Science, 1971)

Single baseline observations:

(Goldstone-Haystack)

Freq.: 7.8 GHz



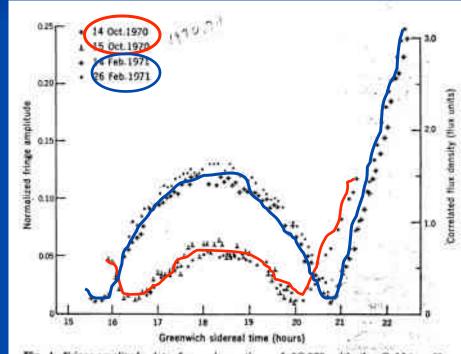
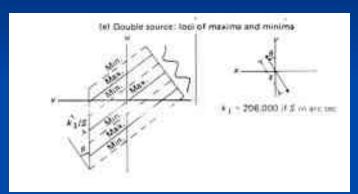
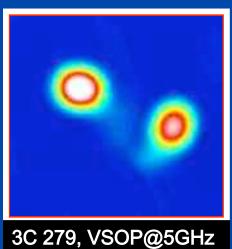


Fig. 1. Fringe-amplitude data from observations of 3C 279 with the Goldstone-Haystack interferometer. Each point is based on 110 seconds of integration.





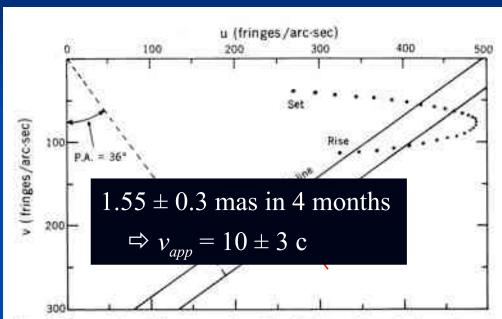


Fig. 4. The u-v plane (1) representation of the Goldstone-Hayatack observations of 3C 279. The dotted curve shows the interferometer resolution at 15-minute intervals from 15 hours 30 minutes to 22 hours 30 minutes Greenwich sidereal time. The solid lines connect the times at which nulls were observed in October 1970 and in February 1971. The distances from the origin to the solid lines are inversely proportional to the separations of the components of the putative double source at the two times of observation. [The position angle (P.A.) was assumed to remain constant.]

227

1970s:

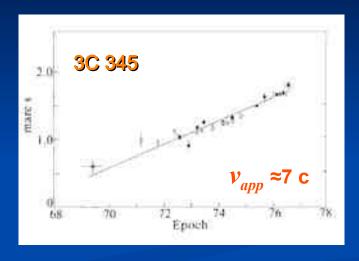
A few strong sources have repeated observations (3C120,3C273, 3C 279, and 3C 345).

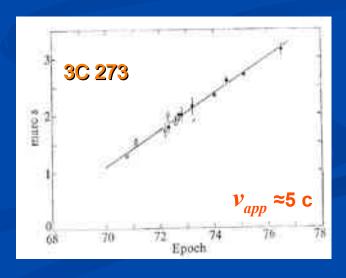
'superluminal motion' by comparing the amplitude patterns.

Late 70s:

Map-making was in a stage of rapid development

"hybrid mapping technique"





(3c 273)

Vare = (9.6±0.8) a

Fig. 4.E. Yi. H. mays as a frequency of Mathematic of the ground Nr. 277 in = 0.235; made or fire Military specific, sharing appearant logisthamism? (i.e., factor than light), expansion of the names (from Pressure of al. 1885). Figure contrary of 1.2 frequent and the Collection Institute of Technology Reproduced by permission from Factor, Vol. 286, no. 1815–267. Copyright 1861 bilanchina framesis (Lanch).

Development of "hybrid mapping' technique allows to map the brightness distribution!

=> First direct and unambiguous evidence!

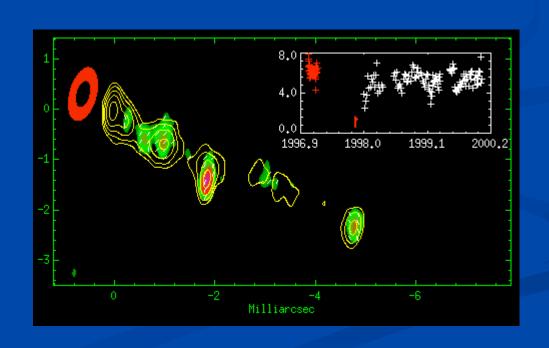
The innermost part of the jet in 3C273:

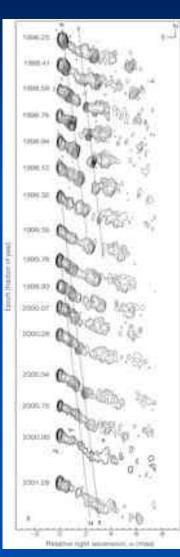
The brightest (leftmost) one corresponds to the object at the center of the quasar.

the rightmost knot looks to have moved about 30 light years in only three years. It moves at 10 times the speed of light

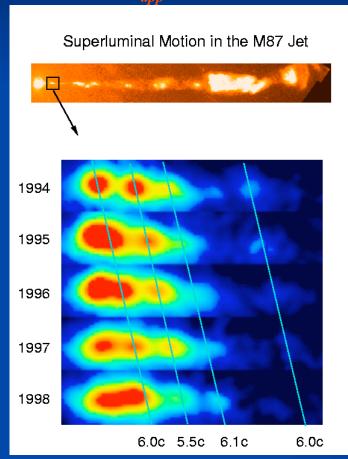
(3c 120)

16 epochs VLBA observations @7mm





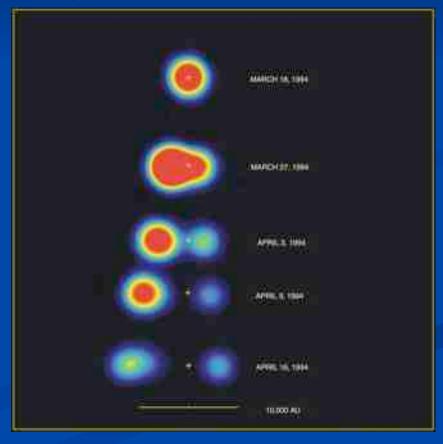
Optical superluminal motion



Biretta et al. ApJ, 1999

Superluminal motion In the Galaxy (GRS 1915+105)

$$v_a \approx 1.25 \text{ c}; v_r = 0.65 \text{ c}$$



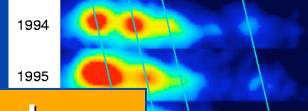
Mirabel and Rodriguez, Nature, 1994

Optical superluminal motion

$$v_{app} \approx 6 \text{ c}$$

Superluminal Motion in the M87 Jet





Road map:

6.0c 5.5c 6.1c

Superluminal motion In the Galaxy (GRS 1915+105)

$$v_a \approx 1.25 \text{ c}; v_r = 0.65 \text{ c}$$



B.1 Accretion disks Marios Karouzos



B.1 Introducing...

"The accretion disk"

(B.1) Marios Karouzos

(B.2) Chin Shin Chang

(B.3) Rusen Lu

B.1 Accretion disks Marios Karouzos

Outline:

(making a long, long, long, long story quite short)

- 1. Introduction to the introduction
- 2. Accreting matter and extracting energy
- 3. Spherical and Bondi accretion
- 4. Non-adiabatic accretion
- 5. Accretion rate and the ADAF model
- 6. Observational evidence





Hunting for the right picture...1

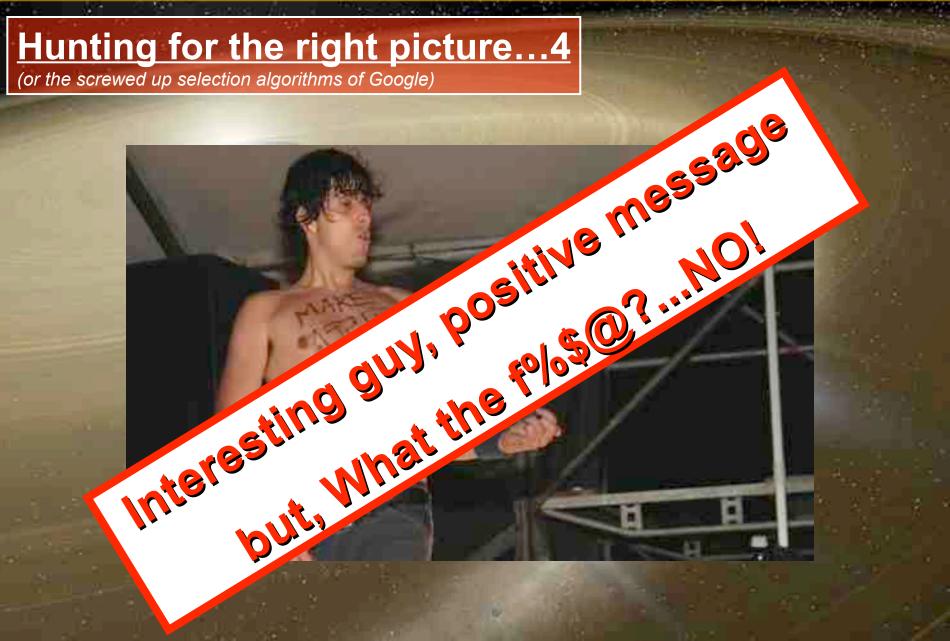


Hunting for the right picture...2



Hunting for the right picture...3

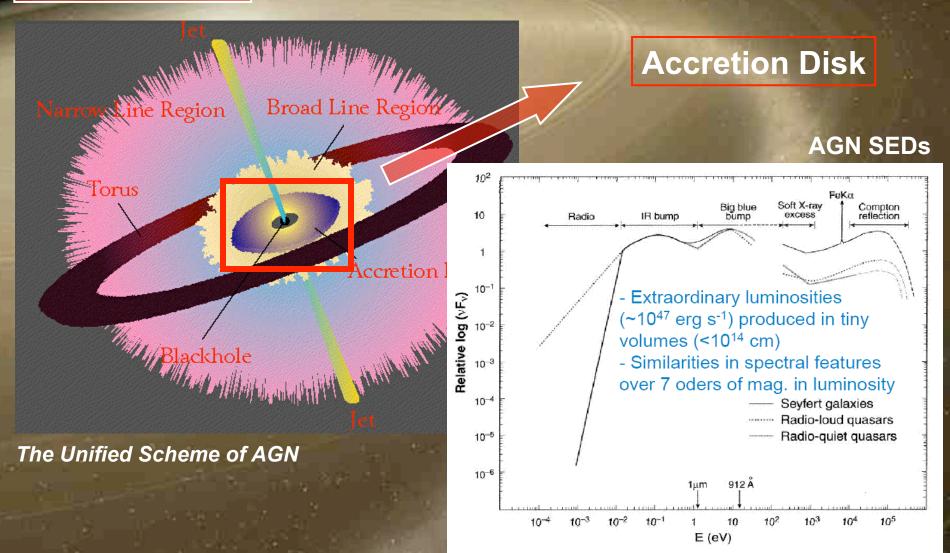




Hunting for the right picture...5







Accreting matter

depending on the spin of the BH

(...and energy interplay)

Powerful energy-producing mechanisms:

- 1. Nuclear fusion (ε ≤ 0.8%)
- 2. Accretion (ε ~ 6 29%)*

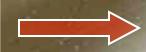
For most galaxies → material has angular momentum (**NOT** free fall)

Mechanisms to extract energy:

- viscosity
- non-axisymmetric gravitational forces
- magnetic forces



Kinetic energy



Thermal energy

Intersection + Equalization of orbits → Accretion Disk

*not the journal...

Spherical and Bondi accretion

(...simplifying Nature*)

Spherical accretion (simplest assumption):

- smooth
- time steady
- spherically symmetric



temperature of accreting gas very high

→ virialized

radiation pressure (trapped photons) high

→ support against gravity

Assumption valid for:

> Eddington luminosity

$$L_E = \frac{4\pi cGM\mu_e}{\sigma_T} = 1.51 \times 10^{38} \frac{M}{M_{sol}} erg s^{-1}$$

(see Rusen's B.3)

Spherical and Bondi accretion (cont.)

(...simplifying Nature*)

Equation of state (energy equation):

→ simplest case (Bondi 1952): adiabatic law

 $p \propto \rho^{\gamma}$

We can derive the accretion rate:

$$\dot{M} = 4\pi\lambda(\gamma) \frac{(GM^2)\rho_{\infty}}{c_s^3}$$

where:

λ(γ) is a function of γ ρ_∞ is the density at infinity c_s the speed of sound at infinity

From the above:

- 1. we have a **scale** for the *accretion rate* (for certain M and f_∞)
- 2. accretion is **regulated** by equation of state (γ)

* for astrophysical plasma $\gamma = 5/3$ (no heating/cooling)

Non-adiabatic accretion

(...now it gets interesting!)

We need to approximate the conditions of the flow:

$$n_e = \frac{\dot{M}}{4\pi r^2 \mu_e u} = 3.8 \times 10^{11} \left(\frac{\dot{M}}{M_{sol} yr^{-1}}\right) M_8^{-2} x^{-3/2} cm^{-3}$$

assuming Newtonian physics + infall at ~ free-fall speed

We can derive the **Thomson** optical depth, in terms of the Eddington accretion rate:

$$\tau_T = \frac{\dot{M}/\dot{M}_E}{x^{1/2}}$$

$$\frac{L}{L_E} \sim 1 \times 10^{-4} \left(\frac{\dot{M}}{\dot{M}_E}\right)^2$$

assuming a certain temperature profile + cooling mechanism (two-body collisions)

L << L_E

Non-adiabatic accretion (cont.)

(...now it gets interesting!)

Even for the more realistic case non-adiabatic accretion:

→ spherical assumption is not valid

photon trapping



ADAF (see next slides) thermal instability



disc disruption

(non-physical result)

Both problems arise from high efficiency ($L \sim L_E$)!

Accretion rate and ADAF

(...lets see what's really happening!)

Even for an initial spherical infall:

- > circular orbits of fixed angular momentum
- > interaction of neighboring orbits
- > mixing of angular momentum
- > co-planar orbits

an accretion disk is formed!

in most cases: thickness << radius



Thin accretion disk

accretion rate regulates the morphology of the disk:

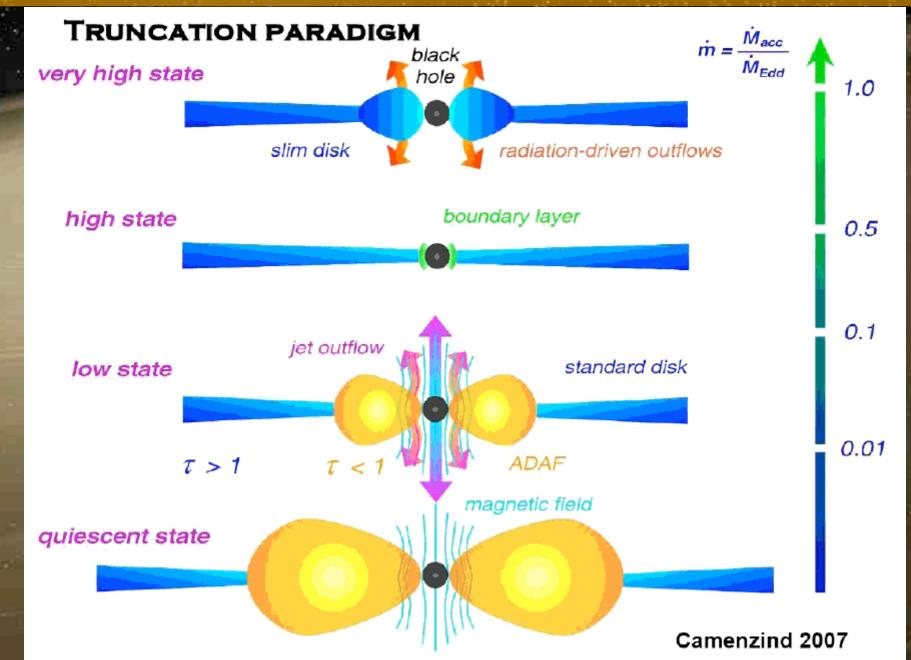
for $dM/dt \rightarrow (dM/dt)_E$



radiation pressure becomes important



thick disk

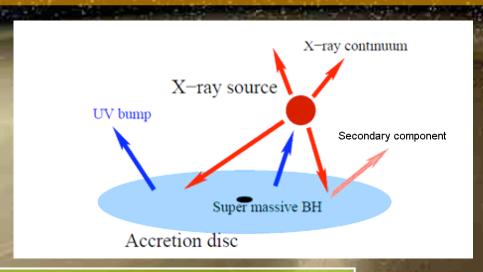


Observational tests

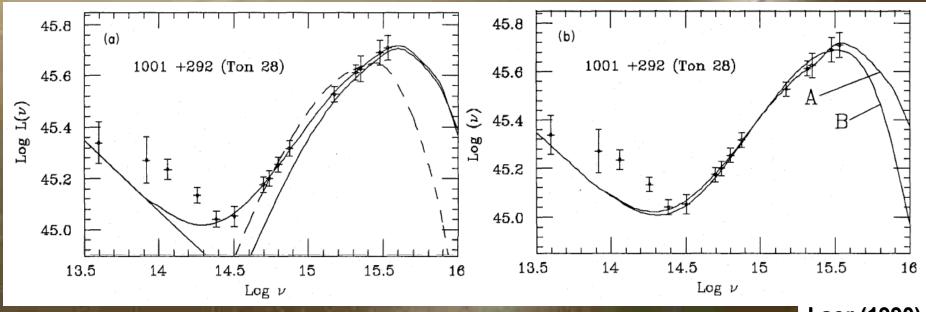
(...lets see!)

Big blue bump:

$$\frac{dF}{d\ln\lambda} \sim 10eV$$



Points toward a thermally emitting surface (no specific geometry needed!)



Laor (1990)

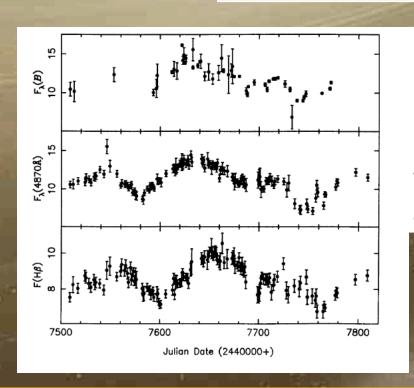
Observational tests (cont.)

(...lets see!)

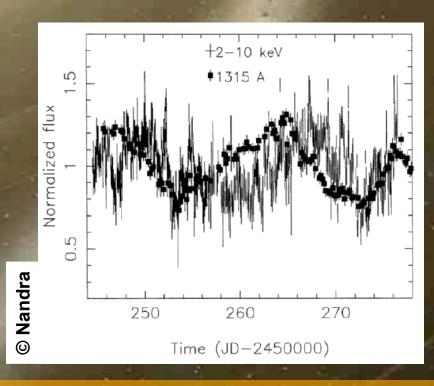
Variability:

timescales → size of emitting regions (light travel time)
→ physical nature of processes

frequency dependency → tracing across the disk



Peterson et al. (1991)

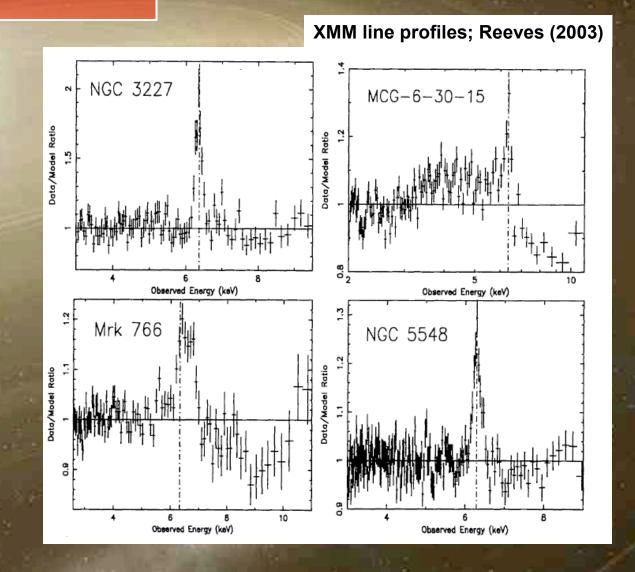


Observational tests (cont.)

(...lets see!)

The iron K line:

(see Chin Shin's B.2)

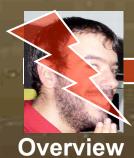


<u>Summary</u>

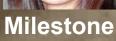
.and passing the torch!)

- Accretion → high enough ε to power AGN
- Spherical accretion → first order approximation
 - > Bondi (adiabatic)
 - > non-adiabatic
- Accretion in disk geometry → most probable
 - > geom. thin disks
 - > geom. thick disks
- Indirect observations
 - > Big Blue Bump
 - > Variability
 - > Iron K line

Road map:









Equations

Snapshots from the life of an AGN

A.2 Milestone in...

"Synchrotron Emission"

(A.1) Rusen Lu

(A.2) Marios Karouzos

(A.3) Chin Shin Chang



THE POLARIZATION OF SYNCHROTRON RADIATION

K. C. WESTFOLD*
California Institute of Technology
Received February 14, 1959

ABSTRACT

The spectral distribution and polarization of radiation from an electron gyrating ultra-relativistically in a magnetic field are calculated. The result is used to calculate the principal emissivities of a distribution of high-energy electrons such as occurs in the Crab Nebula. It is shown that the degree of polarization of the emission increases with frequency, from two-thirds at radio frequencies to unity. The depolarizing factors affecting the intensity of the emergent rays are briefly discussed.

I. INTRODUCTION

The synchrotron process by which radiation is generated has assumed considerable importance since the recent studies by Oort and Walraven (1956), Pikelner (1956), and Woltjer (1958). These have virtually confirmed Shklovsky's (1953) hypothesis that the light from the Crab Nebula is due to radiation from high-energy electrons gyrating in a magnetic field. This process can now be invoked to account for the non-thermal emission from other radio stars and from the galactic halo.

The most useful calculations of the radiation from charged particles moving with velocities close to the velocity of light (ultra-relativistic velocities) are those of Schwinger (1949). His procedure was to calculate the radiant power emitted, via the rate at which the particle does work on the field of which it is the source. The field vectors were not required, so that the polarization of the emission was left undetermined.

On general grounds it is to be expected that radiation so intimately connected with a magnetic field would exhibit polarization. Indeed, it was the discovery of strong polarization in the optical emission from the Crab Nebula by Vashakidze (1954) and Dombrovsky (1954) that sealed the adoption of the synchrotron hypothesis. Woltjer (1957) has

K.C. Westfold, 1959, ApJ

The Motivation

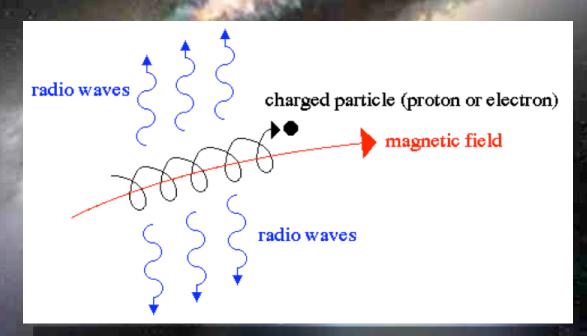
Polarization measurements (photographic plates)

Oort and Walraven (1956); Mean Polarization degree ~ 17%



The Paper

The synchrotron process by which radiation is generated has assumed considerable importance since the recent studies by Oort and Walraven (1956), Pikelner (1956), and Woltjer (1958). These have virtually confirmed Shklovsky's (1953) hypothesis that the light from the Crab Nebula is due to radiation from high-energy electrons gyrating in a magnetic field. This process can now be invoked to account for the non-thermal emission from other radio stars and from the galactic halo.



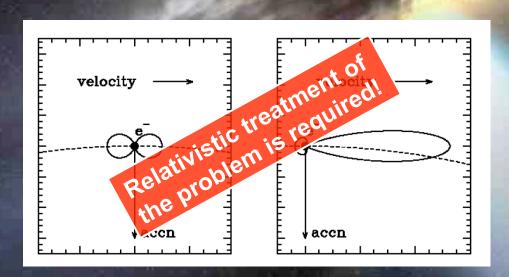
The general idea of the synchrotron process

The gory details

On general grounds it is to be expected that radiation so intimately connected with a magnetic field would exhibit polarization. Indeed, it was the discovery of strong polarization in the optical emission from the Crab Nebula by Vashakidze (1954) and Dombrovsky (1954) that sealed the adoption of the synchrotron hypothesis.

For the proper interpretation of these measures it is essential that the polarization properties of the emission from a single electron should first be known.

We are dealing with relativistic particles, so that:



$$\gamma = \frac{1}{\sqrt{1 - \beta^2}}$$

The position vector

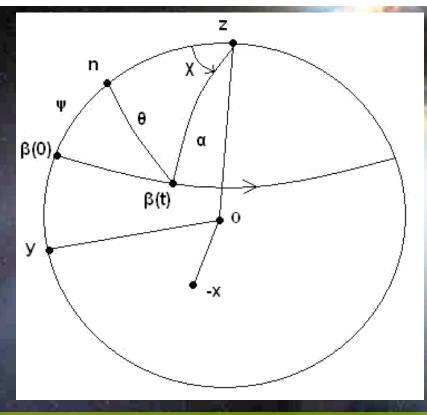
(and other things...)

assuming that γ ~ constant

$$\frac{\vec{r}}{c} = \frac{\beta}{\omega_B} [(\hat{x} \cos \omega_B t + \hat{y} \sin \omega_B t) \sin a + \hat{z} \omega_B t \cos a]$$
(A) (B)

 $\vec{\omega}_B = \frac{e}{m} \sqrt{1 - \beta^2} \vec{B}_0$

gyrofrequency



Index:

z: direction of B0

n: line of sight vector

χ: position angle

α: angle between velocity and B₀

ψ: angle between velocity and n

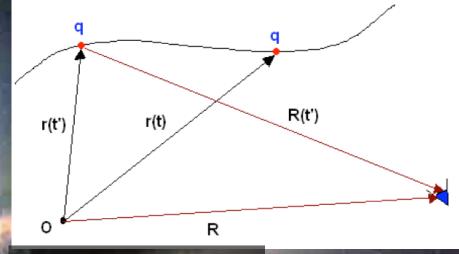
The field equations

(hold onto your seats...)

$$\vec{\mathbf{E}} = \frac{\mu e c}{4\pi R} \frac{\vec{n} \times [(\vec{n} - \vec{\beta}') \times \dot{\vec{\beta}'}]}{(1 - \vec{\beta}' \cdot \vec{n})^3}$$

$$\vec{\mathbf{B}} = \frac{1}{c} \vec{n} \times \vec{\mathbf{E}},$$

$$E_n(\vec{r}) = \frac{\omega_B}{2\pi} \int_0^{2\pi/\omega_B} \vec{E} \exp(in\omega_B t) dt$$



Sketch of retarded * time

$$E_n = A(R, \omega_B) \cdot \int_0^{2\pi/\omega_B} \frac{\vec{n} \times [(\vec{n} - \vec{\beta}') \times \dot{\vec{\beta}'}]}{(1 - \vec{\beta}' \cdot \vec{n})^2} \exp\left[in\omega_B \left(t' - \vec{n} \cdot \frac{\vec{r}}{c}\right)\right] dt'$$

* politically correct term: mentally challenged

Some assumptions

(of course...what else?)

We assume that:

- motion length scale << distance to observer
- $\gamma >> 1 \rightarrow \gamma^{-1} << 1 \rightarrow \beta$ can be expanded
- n is on the plane (B₀,β₀)
- $\theta > \gamma^{-1}$ negligible \rightarrow integration over $\pm \infty$

$$E_n = \frac{\mu e c \omega_B}{4\sqrt{3}\pi^2 r} \exp\left(in\omega_B \frac{r}{c} \frac{n}{\sin\alpha}\right) \cdot \{E_2 \cdot \hat{\mathbf{x}} - E_1 \cdot (\hat{\mathbf{x}} \times \hat{\mathbf{n}})\}$$

$$Q_n = \frac{E_n \cdot \hat{x}}{E_n \cdot \hat{x} \times \hat{n}}$$

complex polarization degree of the nth E harmonic

Calculating the intensity

(and some guys called Stokes parameters...!)

$$I_f = R^2 \frac{c}{2\pi} |E_n|^2 \frac{dn}{df}$$

R: distance to observer n: number of harmonic f: frequency $O(\omega_B)$

$$f = n \cdot \frac{\omega_B}{2\pi}$$

$$I_f^{(1)} = \frac{3}{4\pi^2} \frac{e^3 B_0 \gamma}{mc^2} \left(\frac{f}{f_c}\right)^2 (1 + \gamma^2 \psi^2)^2 K_{2/3}^2(g_f)$$

$$I_f^{(2)} = \frac{3}{4\pi^2} \frac{e^3 B_0 \gamma}{mc^2} \left(\frac{f}{f_c}\right)^2 \gamma^2 \psi^2 (1 + \gamma^2 \psi^2) K_{1/3}^2(g_f)$$

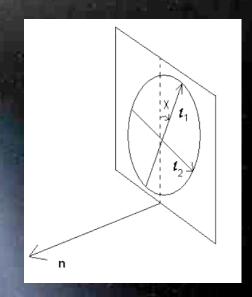
Stokes parameters:

$$I_f = I_f^{(1)} + I_f^{(2)}$$

$$Q_f = [I_f^{(1)} - I_f^{(2)}] \cos 2x$$

$$U_f = [I_f^{(1)} - I_f^{(2)}] \sin 2x$$

$$V_f = [I_f^{(1)} - I_f^{(2)}] \tan 2\beta$$



A population of electrons!

(in a nutshell...)

At a given field point the synchrotron radiation received from a small volume containing a distribution of ultra-relativistically gyrating electrons effectively originates in the group whose velocities have directions within the conical annulus for which α is within an angular distance $0(\xi)$ of θ , the angle between n and n0.

The contributed power depends on:

- the energy of the e⁻: E=E(E₀,γ)
- the angle ψ

$$\eta_f^{(i)}(\vec{n}) = \frac{1}{4\pi} \int_0^\infty N\Big(\frac{E}{E_0}\Big) \Big\langle P_f^{(i)}\Big(\frac{f}{f_c}\Big) \Big\rangle \frac{dE}{E_0},$$

Total emissivity:

Polarized emissivity:

$$\eta_f = \eta_f^{(1)} + \eta_f^{(2)}$$

$$\eta_f^{(p)} = \eta_f^{(2)} - \eta_f^{(1)}$$

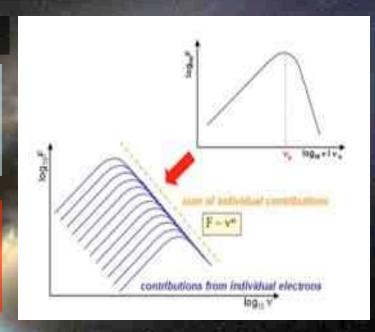
A power law...

(the simplest case!)

We can assume for the population of electrons:

$$N(x) = Ax^{-p} \qquad \text{for} \qquad \frac{E_1}{E_0} \le x \le \frac{E_2}{E_0}$$

$$N(x)=0$$
 for $x<rac{E_1}{E_0}, x>rac{E_2}{E_0}$



$$\eta_f(\vec{n}) = A \frac{\mu e^2 c}{8\sqrt{2}\pi} \left(\frac{3}{2}\right)^{\gamma/2} (f_{B_0} \sin \alpha)^{(p+1)/2} f^{-(p-1)/2} \left[G\left(\frac{f}{f_{c2}}\right) - G\left(\frac{f}{f_{c1}}\right) \right],$$

Direct dependency on: Lorentz factor, frequency, transverse B

Intensity and Stokes parameters

(hung on...almost there!)

Assuming an optically thin medium: (and no depolarization effects)

$$I_f = \int \eta_f ds$$

$$\eta_f^{(1)} + \eta_f^{(2)} = \frac{\sqrt{3}}{16\pi} A \frac{e^3 B \sin \theta}{mc^2} \frac{p + \frac{7}{3}}{p+1} \Gamma \left(\frac{3p-1}{12}\right) \Gamma \left(\frac{3p+7}{12}\right) \left(\frac{3e B \sin \theta}{2\pi mc f}\right)^{\frac{p-1}{2}}$$

$$\eta_f^{(1)} - \eta_f^{(2)} = \frac{p+1}{p+\frac{7}{3}} (\eta_f^{(1)} + \eta_f^{(2)})$$

$$\begin{pmatrix} I_f \\ Q_f \\ U_f \\ V_f \end{pmatrix} = \frac{\varepsilon^{\frac{p}{3}}}{\text{110bserver's framely}} \begin{pmatrix} \frac{p+\frac{7}{3}}{p+1} \\ \cos 2\chi \\ \sin 2\chi \\ 0 \end{pmatrix}$$

This refers to energy per unit length, frequency, time, surface, and solid angle

* from my side!

Summary...

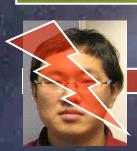
(yeap, it's over*!)

- We calculate Stokes parameters for 1 electron
- Polarization depends on the energy (γ)
- Also on the magnetic field power + structure
- Angle (β, B) is important
- Relativistic effects important
- Generalize for a population of electrons
- Polarization then depends on power law index!

Simple description:

- > constant B field
- > constant energy
- > constant geometry
- > optically thin medium

Road map:







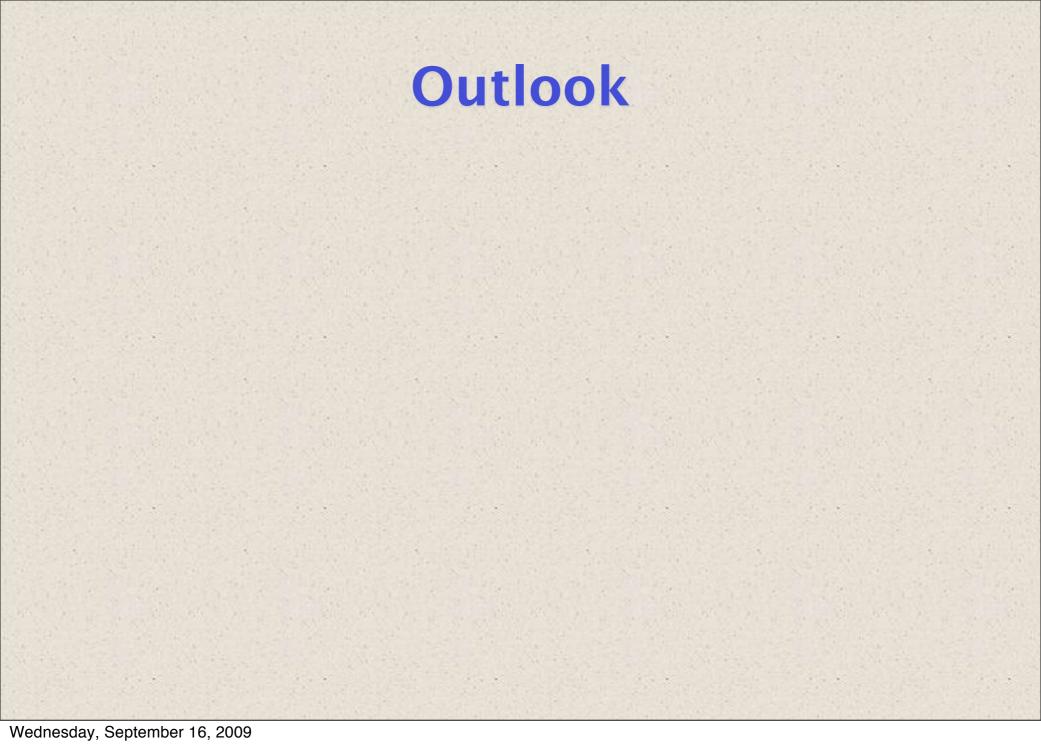


Gamma - Ray Bursts

loannis Nestoras

IMPRS Retreat 15/09/2009

International Max Planck Research School (IMPRS) for Astronomy and Astrophysics.



Outlook

What are gamma-ray bursts, (GRBs)??

Outlook

What are gamma-ray bursts, (GRBs)??

- What are gamma-ray bursts, (GRBs)??
- Type of GRBs

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- Type of GRBs
- Theoretical models for GRBs

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- What are gamma-ray bursts, (GRBs)??
- Type of GRBs
- Theoretical models for GRBs
- Obsarvational data for GRBs

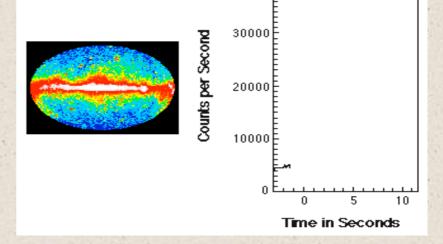
So what are they exactly??

IMAGINE if you could see something that:

Emitted as much energy as nearly the entire universe for few seconds, Allowed you to see billions of years into the past, from your own backyard,

And, of all the world's great observatories looking for this object,

You saw it first...



So what are they exactly??

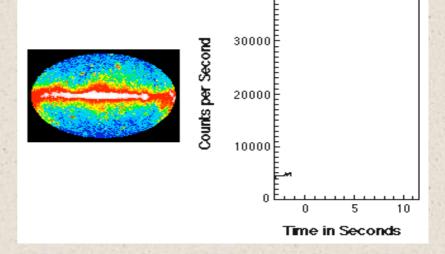
IMAGINE if you could see something that:

Emitted as much energy as nearly the entire universe for few seconds, Allowed you to see billions of years into the past, from your own backyard,

And, of all the world's great observatories looking for this object,

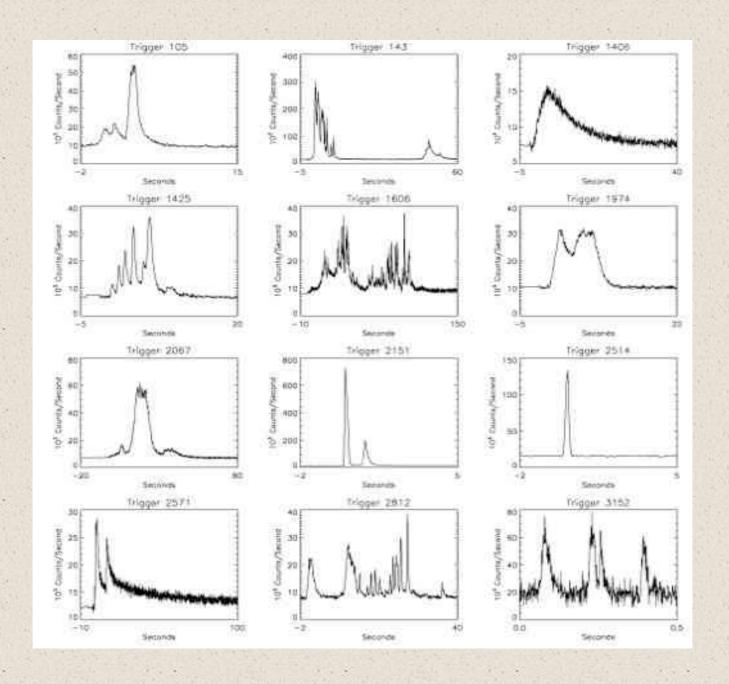
You saw it first...

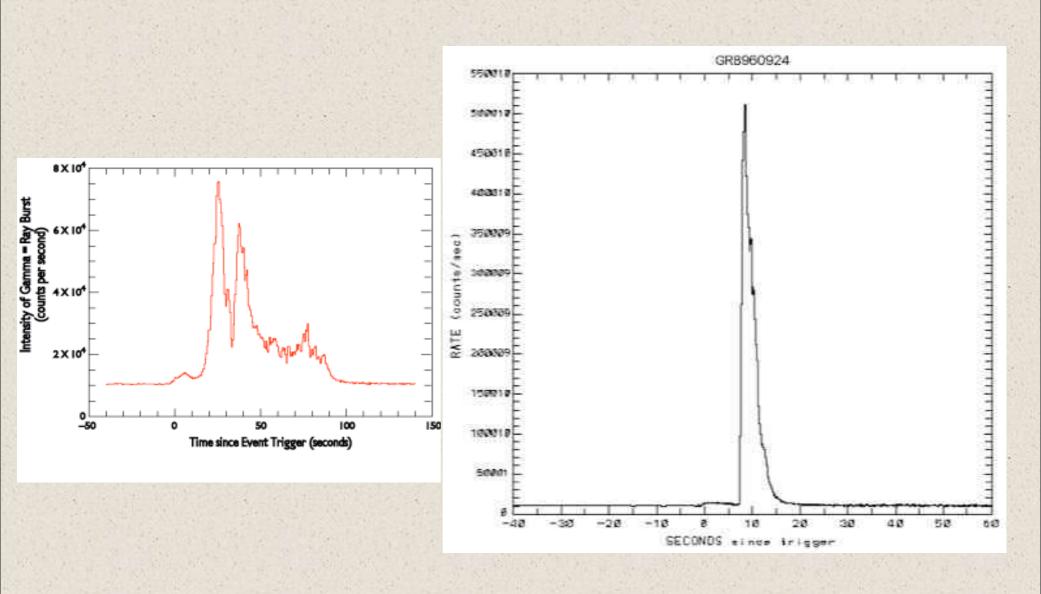
GRBs are objects that produce massive emission of gamma rays for a period of ~ 0.1 to 100 seconds followed, in some cases, by optical, radio, and/or x-ray afterglows

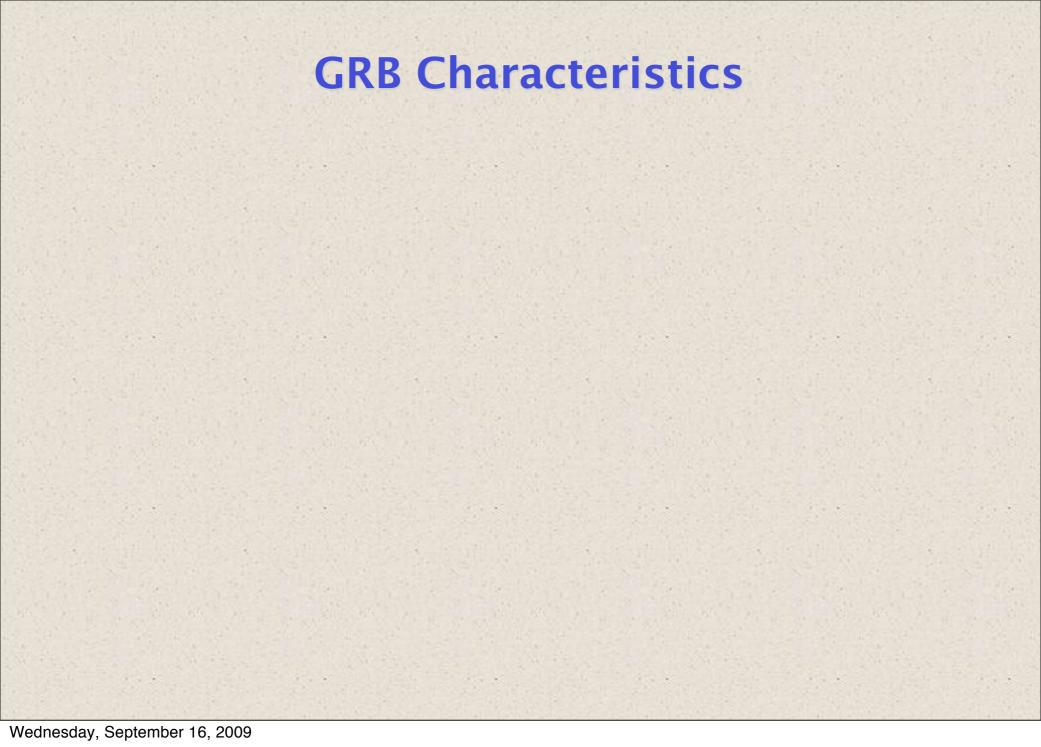


So what are they exactly??









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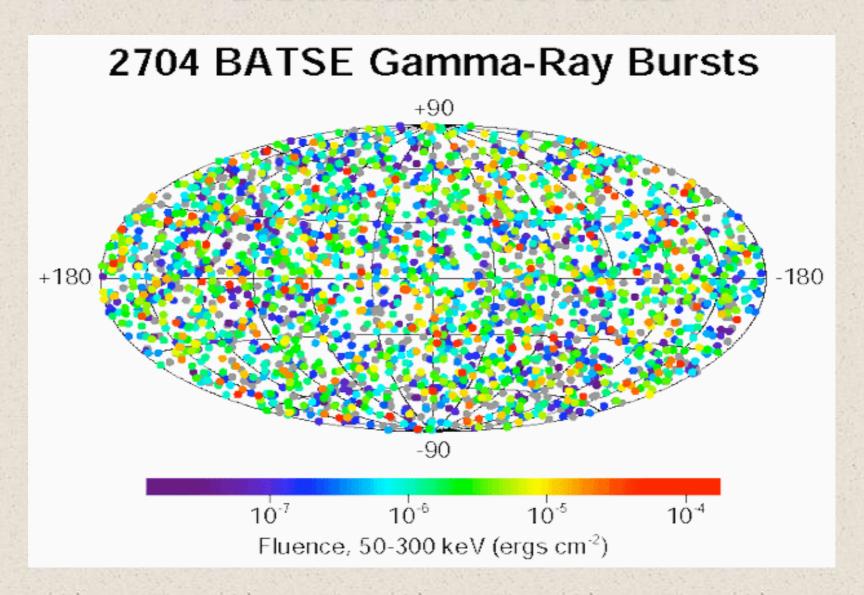
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- > The dimension of the central engine is of the order of $10^5 10^{10}$ m.
- The power of a GRB is $>10^{43}$ watts.

Distribution of GRBs

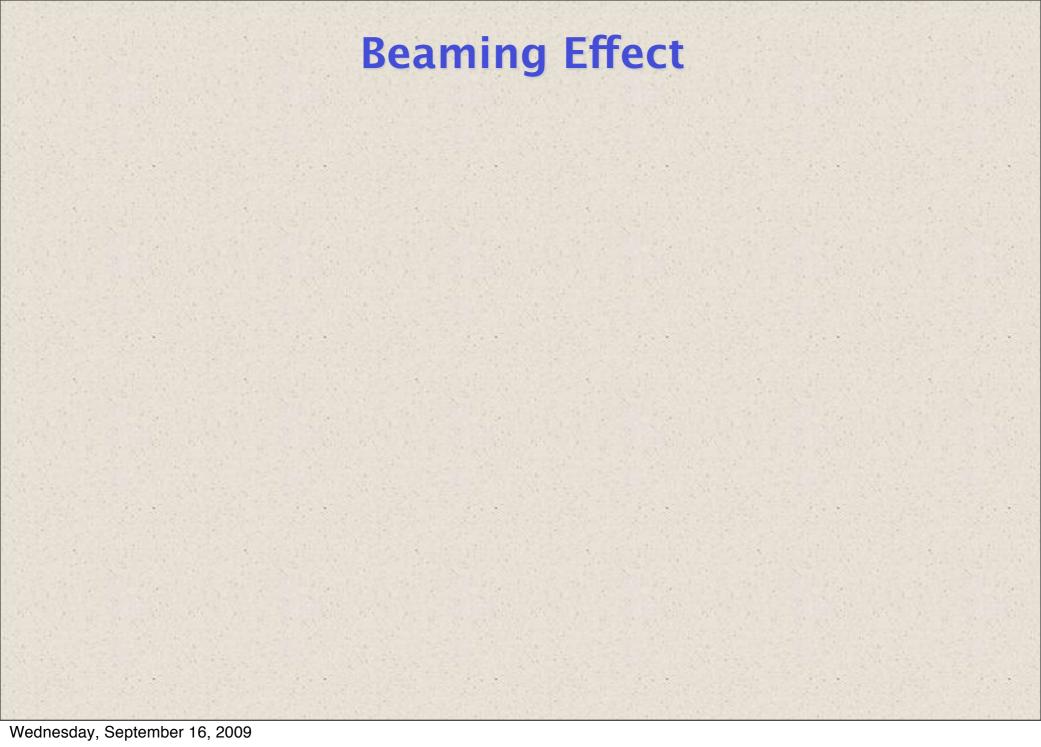


The power of GRBs

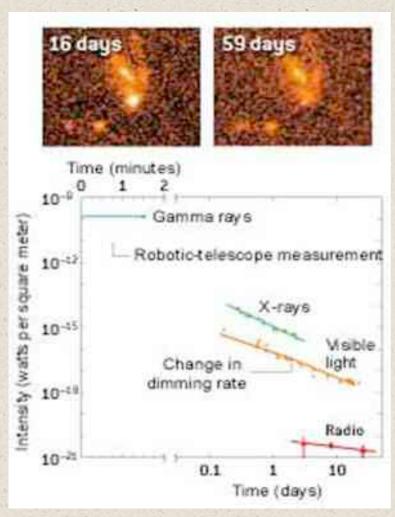
❖Power of a single GRB >10⁴⁰ Joule/sec!!!!!

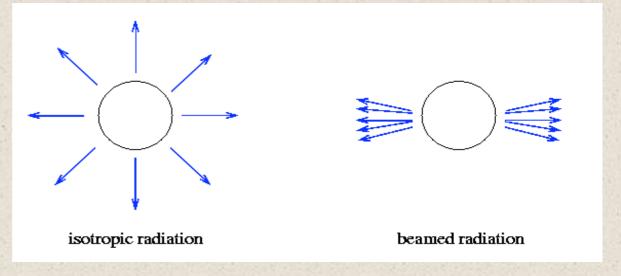
❖ Power of the Sun L_H=3.8·10²⁶ Joule/sec

❖Power of a Galaxy L=10³⁶ Joule/sec!!!

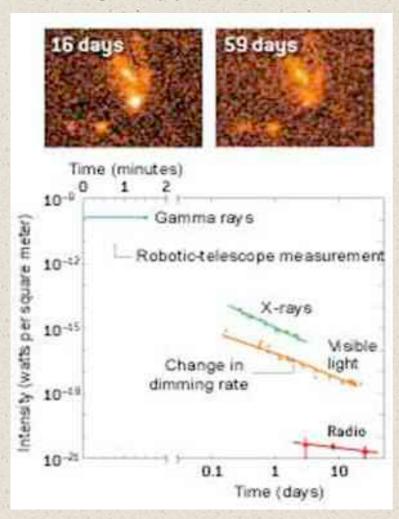


GRB990123

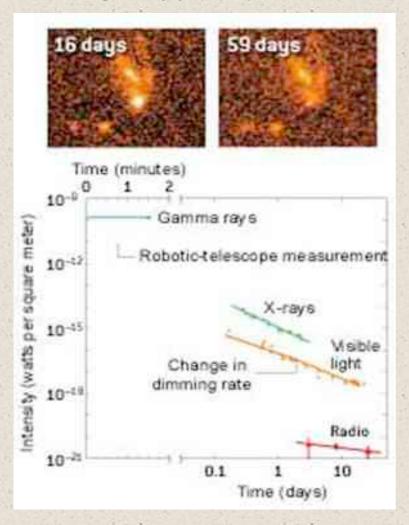


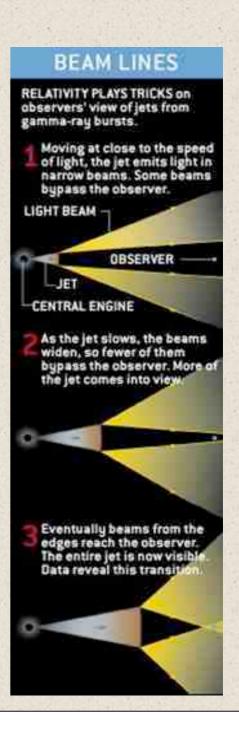


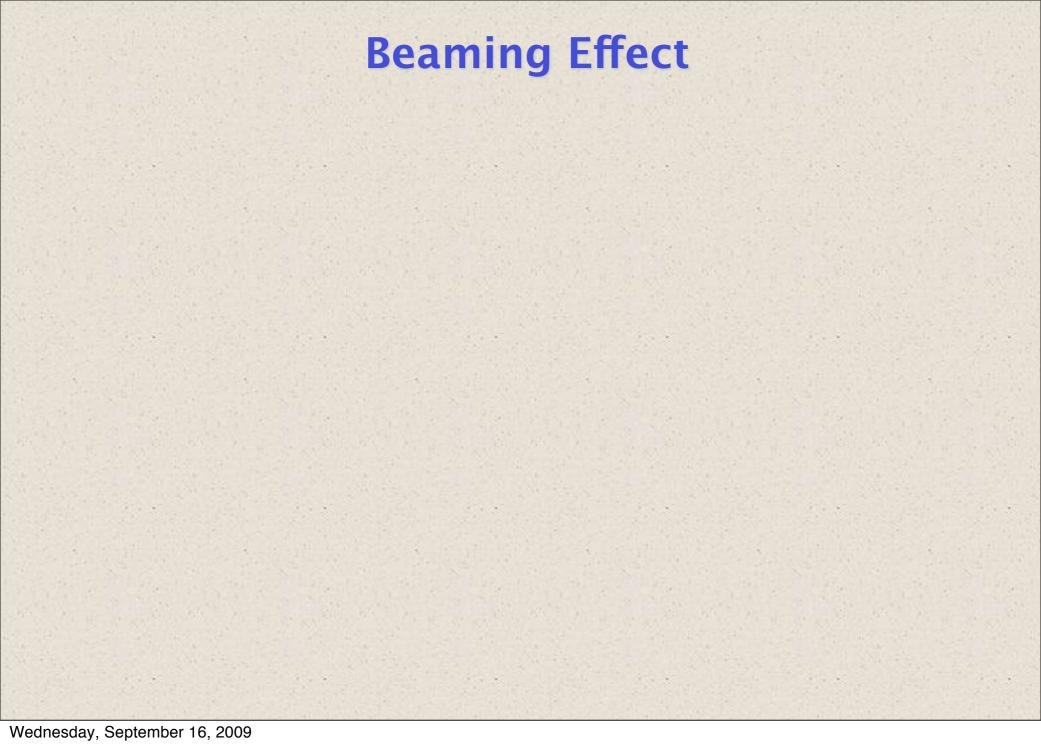
GRB990123

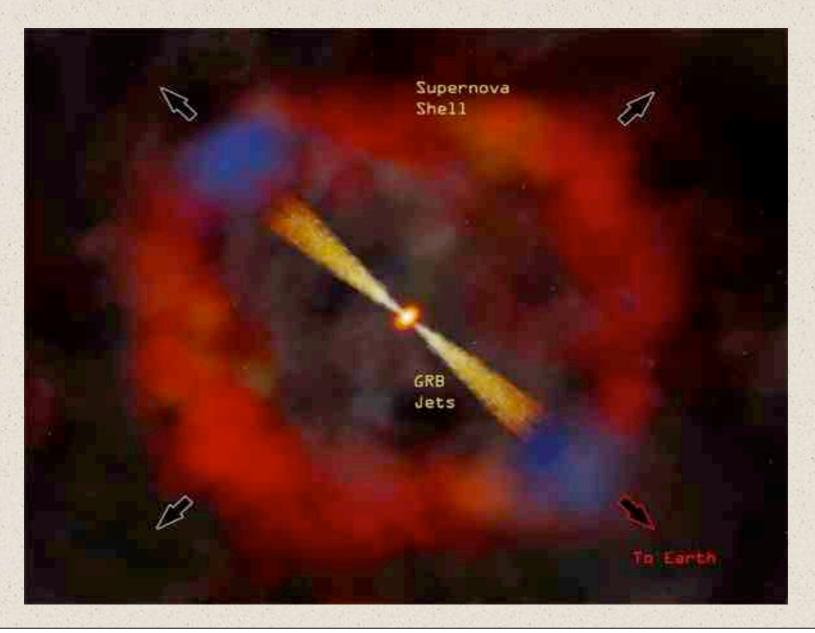


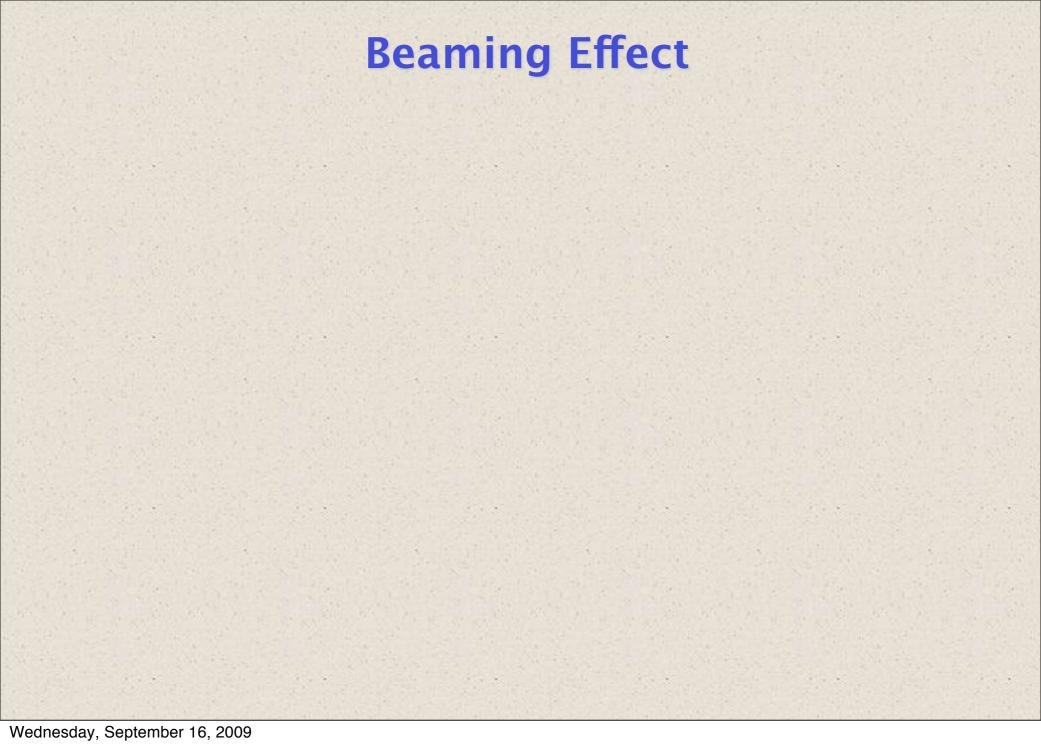
GRB990123











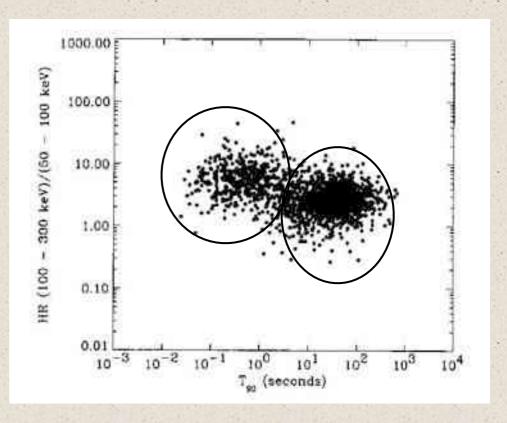


Type of GRBs

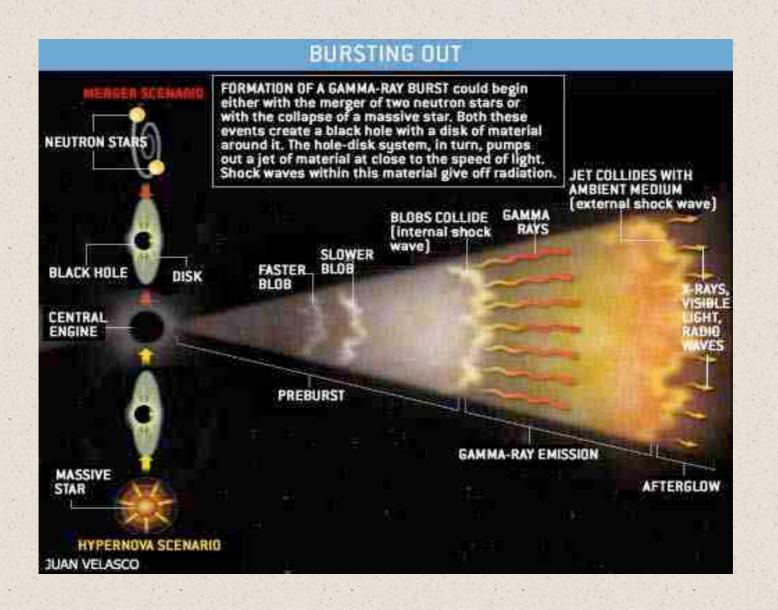
Burst Class (Subclass)	Percentage Of All Bursts	Duration of Initial Emission (sec)	Initial Gamma Ray Emission	X-Ray Emission	Visible Emission	Hypothetical Central Engine
Long (normal)	25	20	✓	✓	1	Energetic explosion of massive star
Long (ghosts)	30	20	✓	✓	X	Energetic explosion of massive star
Long (x-ray flashes)	25	30	X	✓	X	Energetic explosion of massive star
Short	20	0.3	✓	?	?	Merger of pair of compact objects?

Theoretical models of GRBs

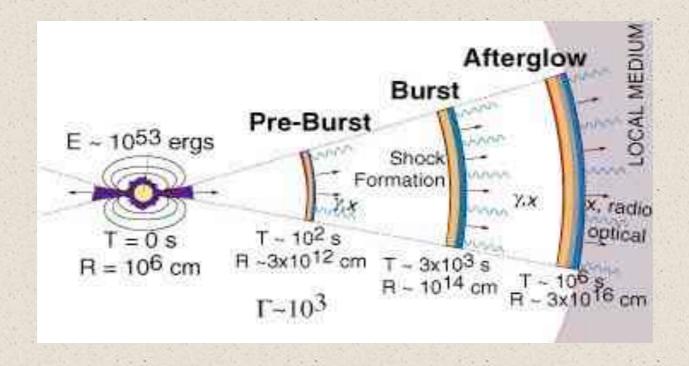
- Plots of "hardness ratio" versus burst duration showed a dumbbell-like distribution.
- Infers there may be two different types of GRB "engines", thus multiple theories of GRB formation may be correct.



Theoretical models of GRBs



Theoretical models of GRBs

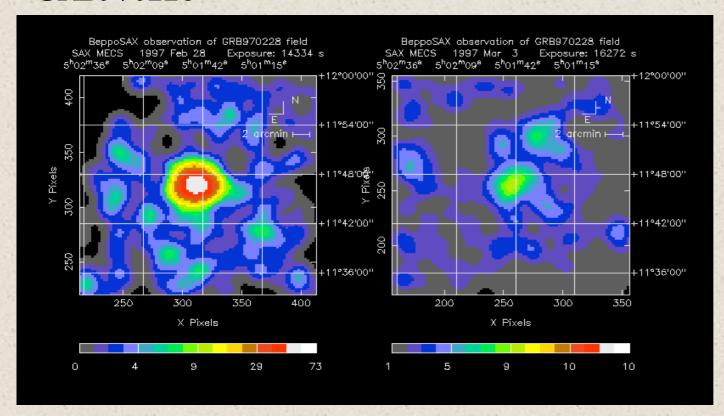






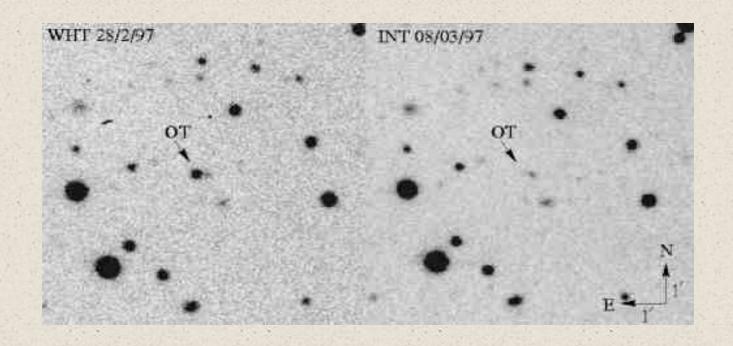
Observational data for GRBs

GRB970228



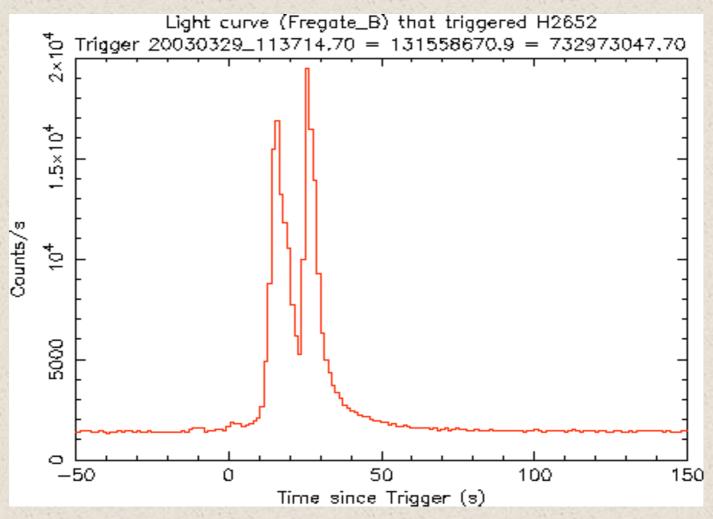
The first obsarvation of an afterglow $\sigma\epsilon$ x-rays

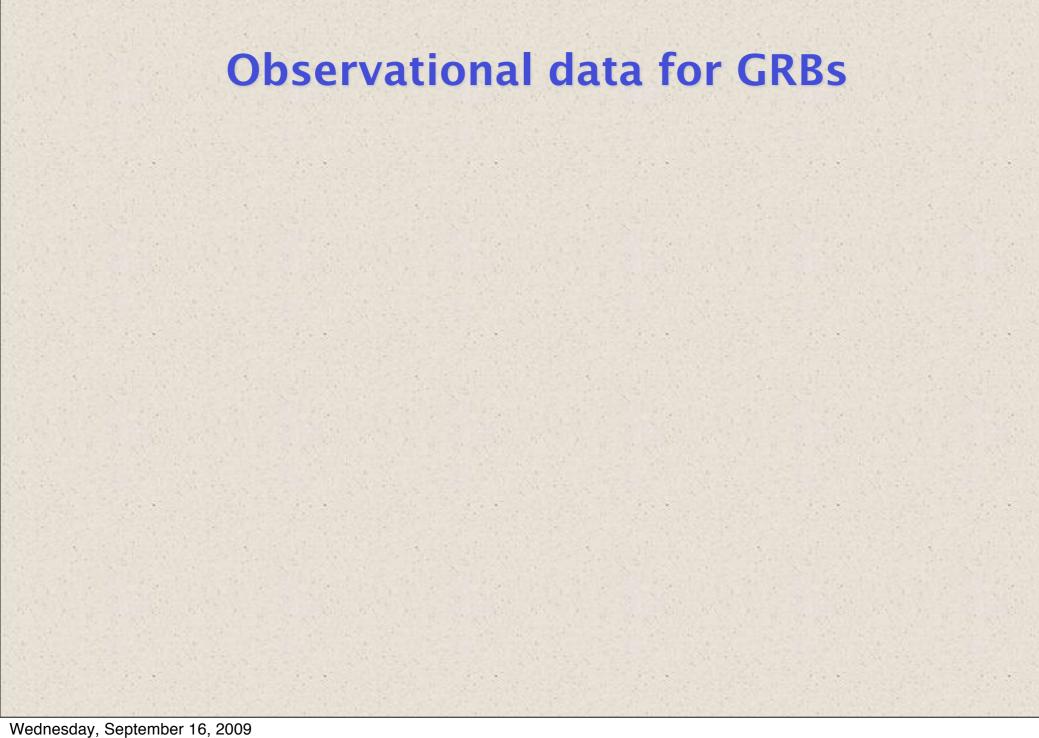




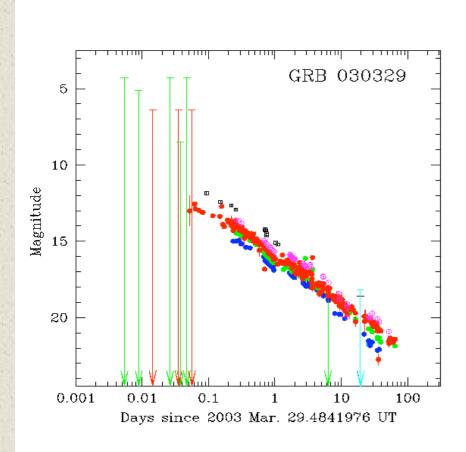
And in Optical...

GRB030329





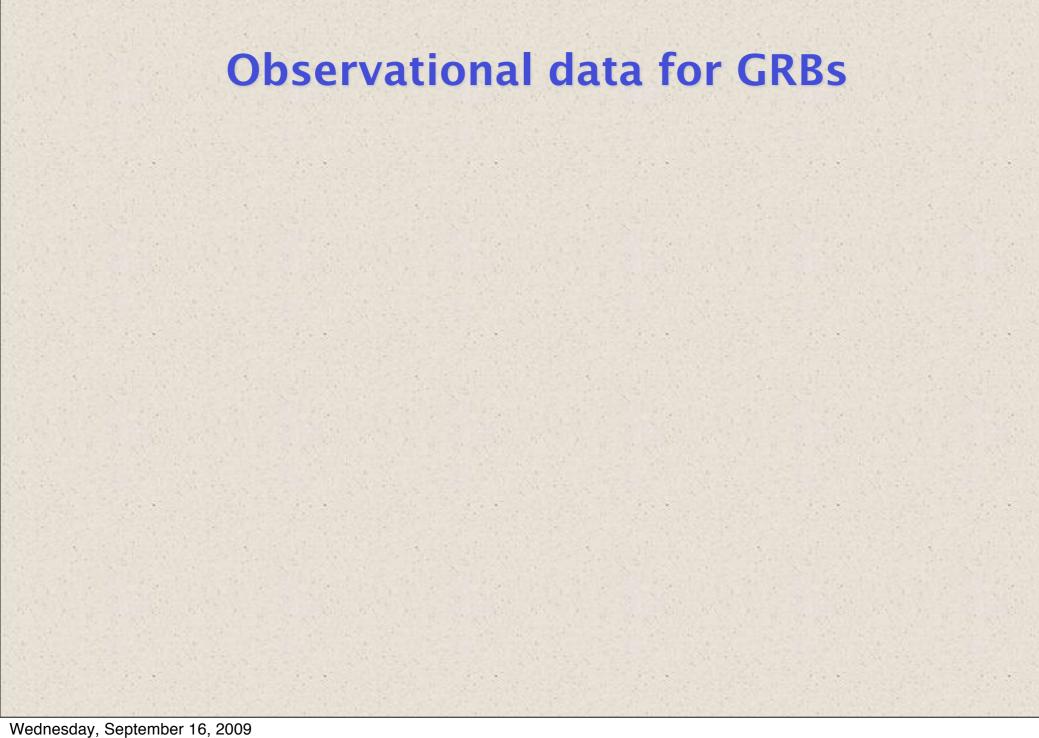
ESO FR Those (Ta.HE (10 9 mc 2005)

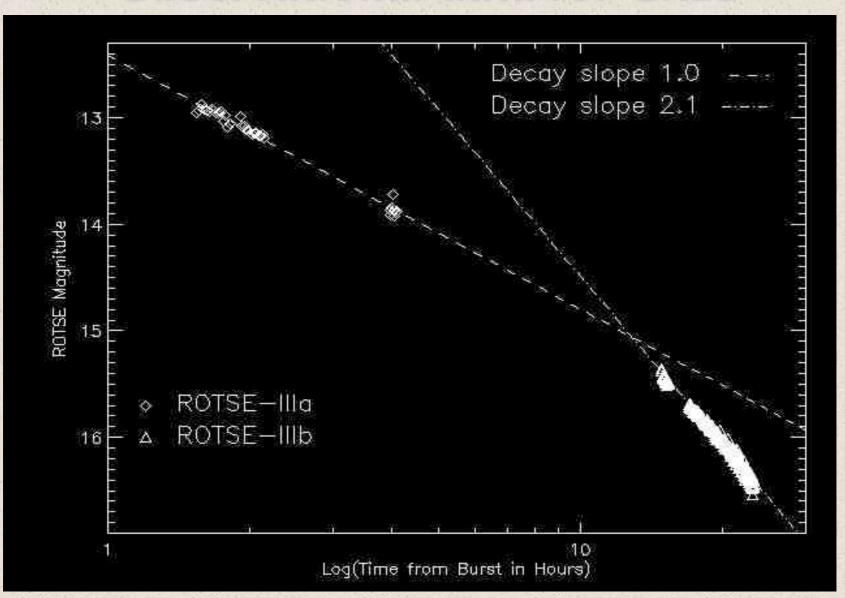




(VLT + FORS)

o European Southern Observator

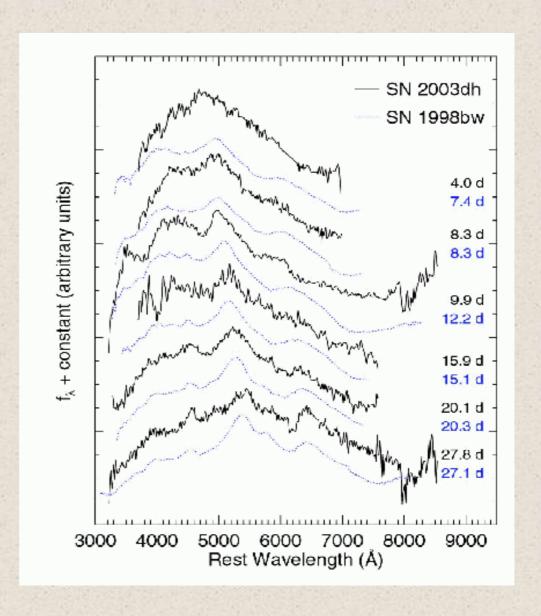




Connection of GRB980425 - SN 1998bw

and

Connection of GRB030329 - SN 2003dh



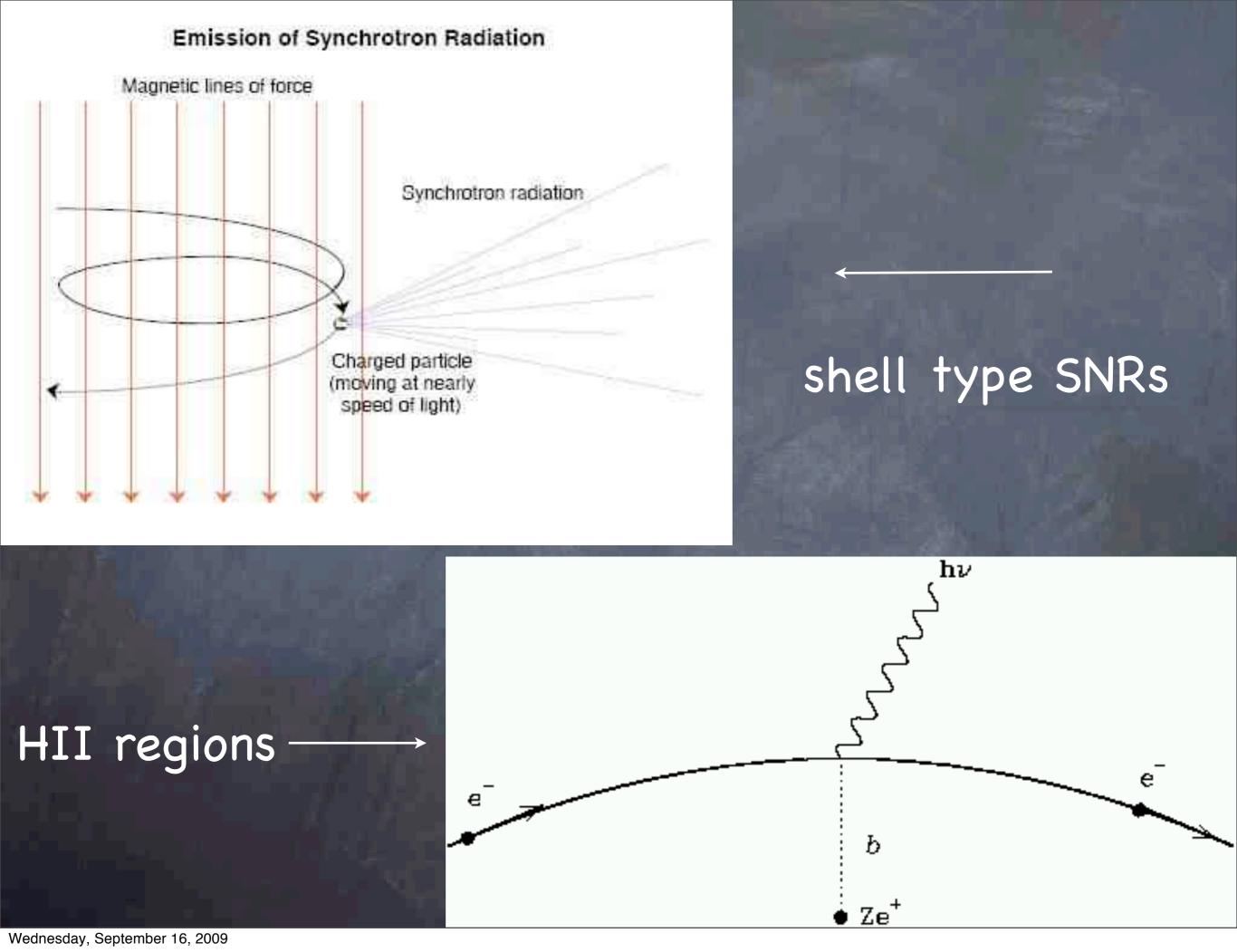
Radio (polarization) surveys of the Galaxy/Galactic plane

Xuyang Gao

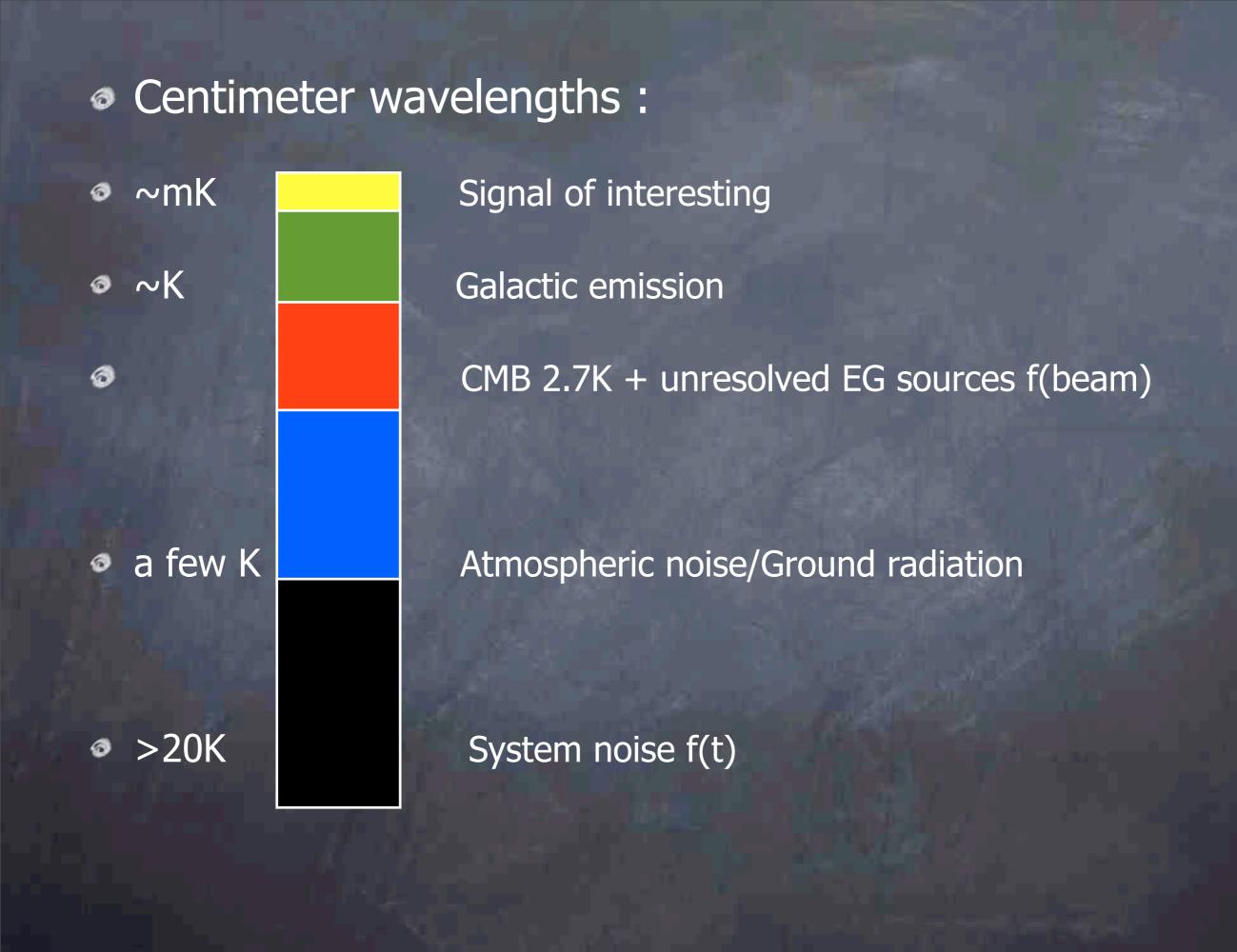
IMPRS retreat 2009, Braunfels 09-16-09

- Radio properties of SNRs, HII regions, FSs, ISM etc
- Foreground of CMB polarization
- Magnetic field in the Galaxy

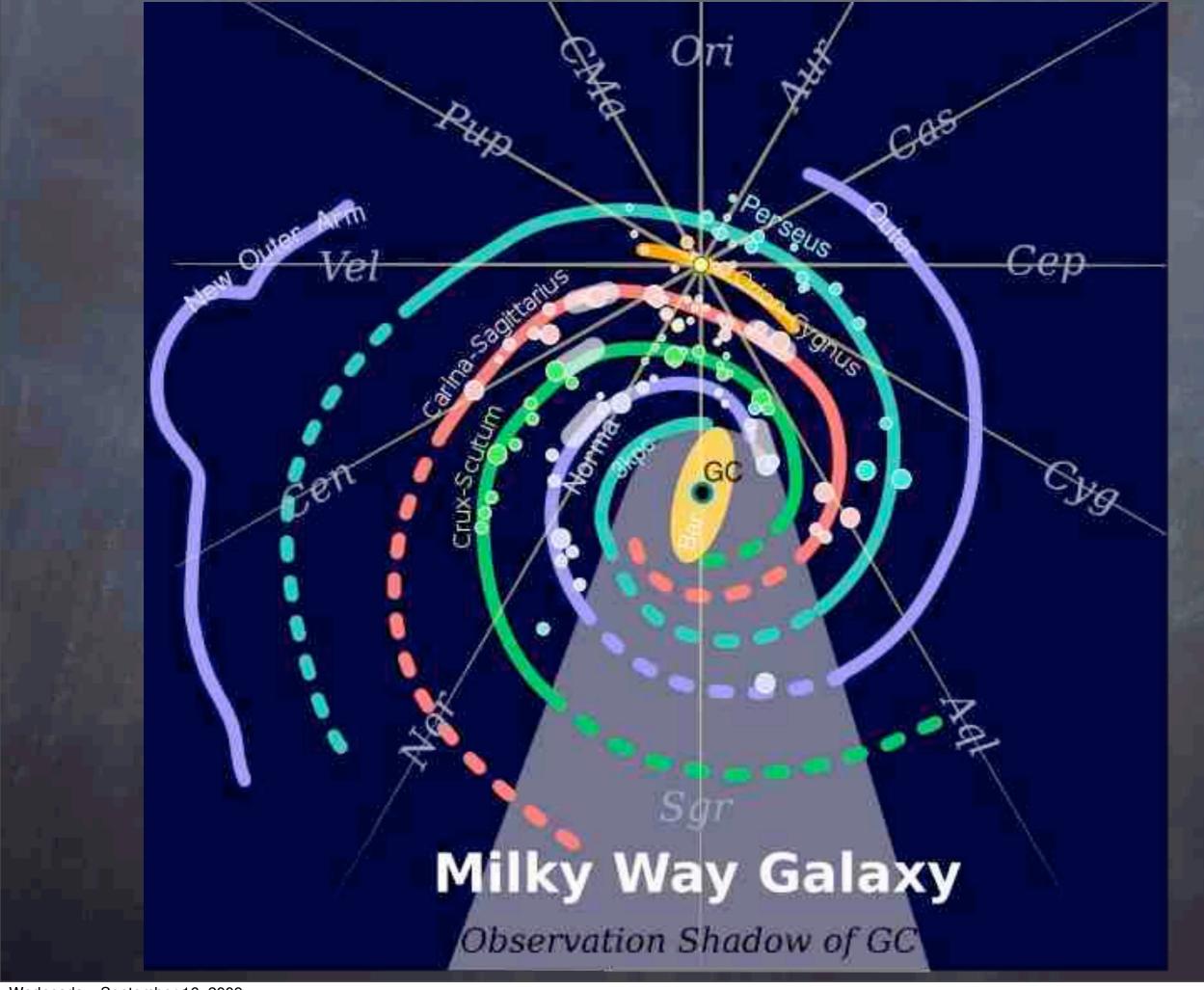
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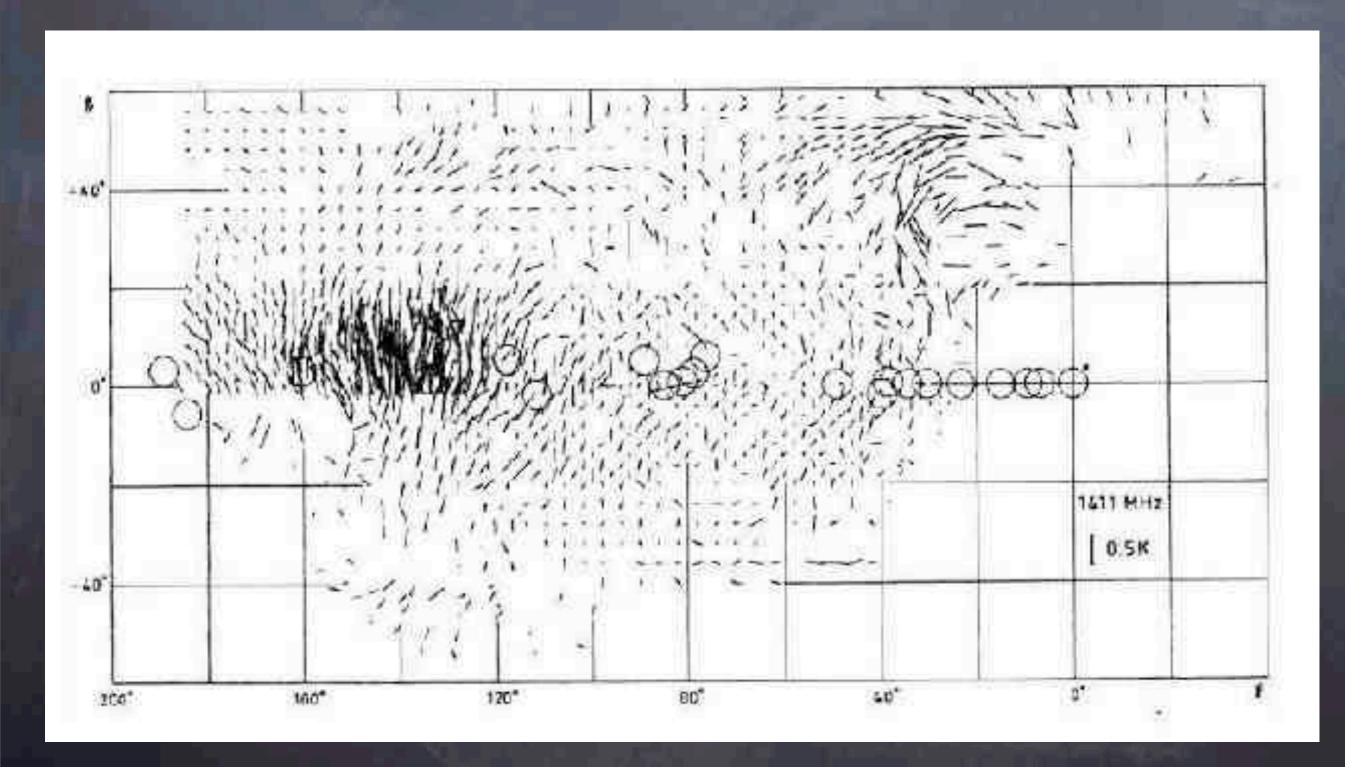
- Radio properties of SNRs, HII regions, FSs, ISM etc
- Foreground of CMB polarization
- Magnetic field in the Galaxy



History of polarization survey

- Cambridge 7.5-m dish 408MHz (Wielebinski et al. 1964)
- Leiden Dwingeloo 25-m telescope 408MHz (Berkhuijisen et al. 1963)
- Parks 64-m telescope 30MHz (Mathewson et al. 1965)
- Dwingeloo 610MHz
- 408MHz and 620MHz in southern sky

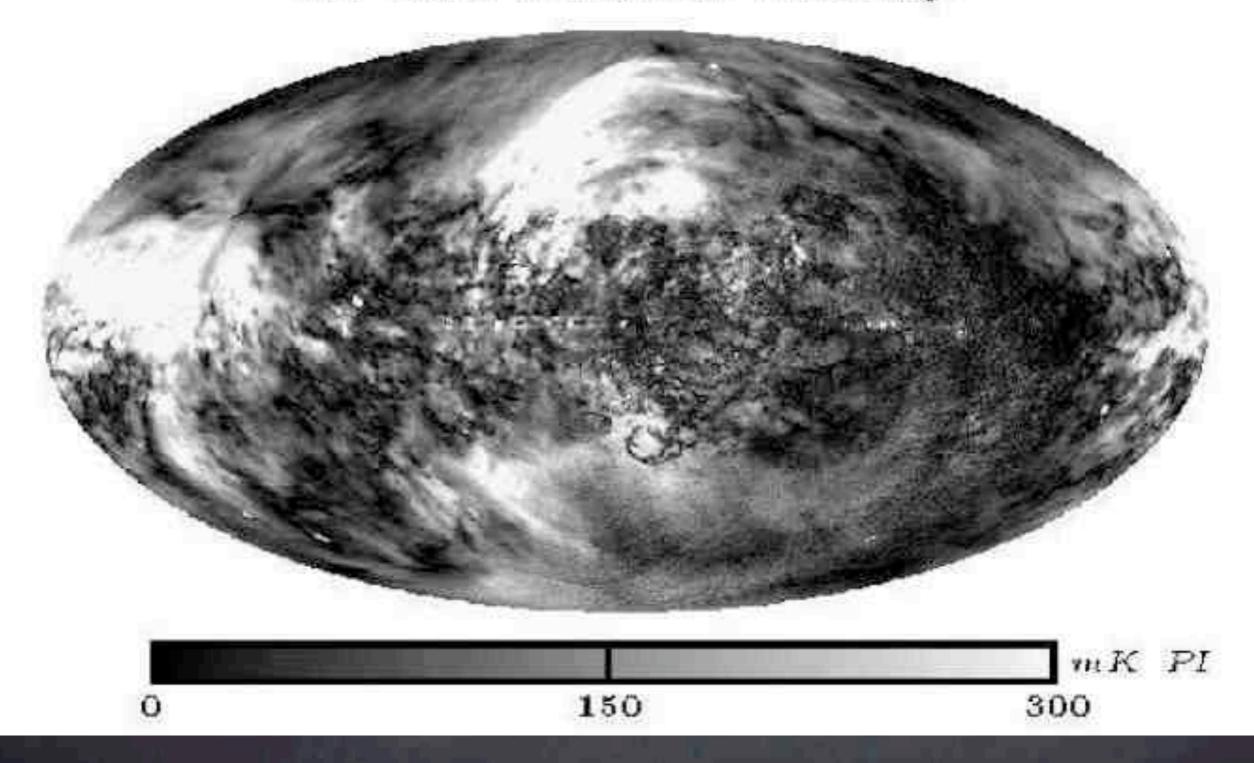
Leiden-Dwingeloo 1.411GHz polarization survey



Nowadays.....

- Effelsberg 1.4GHz, 2.7GHz survey
- © CGPS/SGPS 1.4GHz survey
- © EMLS 1.4GHz survey
- Parks 2.4GHz survey
- Sino-German 4.8GHz survey
- Nobeyama 10GHz survey
- WMAP
- Ø

1.4 GHz Polarized Intensity



Property of synchrotron emission

Tintensity:
$$I_{\nu} \sim N_e B_{\perp}^{\frac{\gamma+1}{2}} \nu^{\frac{-(\gamma-1)}{2}}$$

Polarization percentage: $p = \frac{\gamma + 1}{\gamma + \frac{7}{2}}$

$$p = \frac{\gamma + 1}{\gamma + \frac{7}{3}}$$

Faraday Rotation

$$RM(rad\,m^{-2}) = 0.81 \int_L n_e(cm^{-3}) B \, \mathrm{H}\,(\mu\,G) dL(pc)$$

$$\psi = \psi_0 + RM \lambda^2$$

Depolarization

$$U = U_1 + U_2 = E^2(\cos(2\beta_1)\sin(2\chi_1) + \cos(2\beta_2)\sin(2\chi_2))$$

$$Q = Q_1 + Q_2 = E^2(\cos(2\beta_1)\cos(2\chi_1) + \cos(2\beta_2)\cos(2\chi_2))$$

- Depth depolarization
- Bandwidth depolarization
- Beam depolarization

About our own survey

Longitude: 87d 10' 40.44"E

Latitude: 43d 28' 16.14"N

Altitude: 2029 m

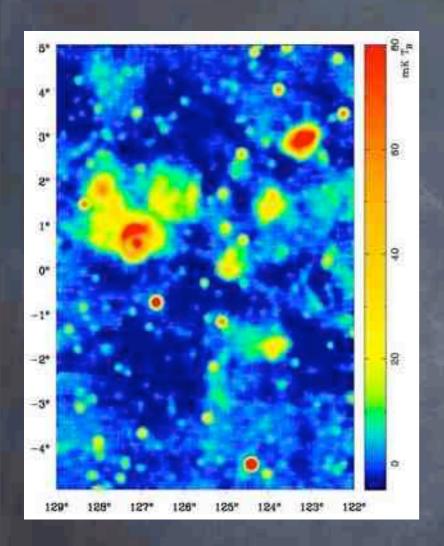
- Urumqi 25m telescope, located in Nanshan, Urumqi, China
- Survey started in Sept 2004
- 5GHz receiver constructed at MPIfR, almost the same as mounted in Effelsberg
- -5 to 5 deg in Galactic latitude, 10 to 230 deg in Galactic longitude
- Broad-band mode(600 MHz) and Narrow-band mode(295MHz)

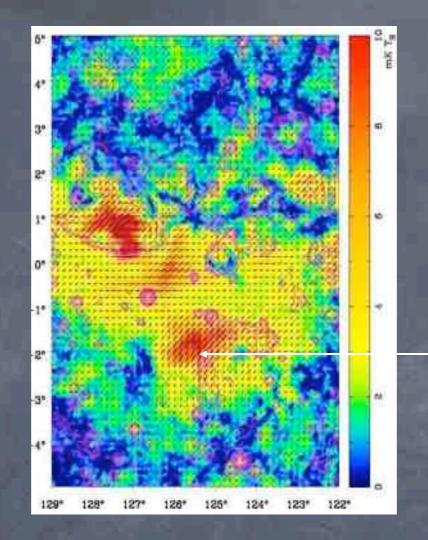
Parameters of survey

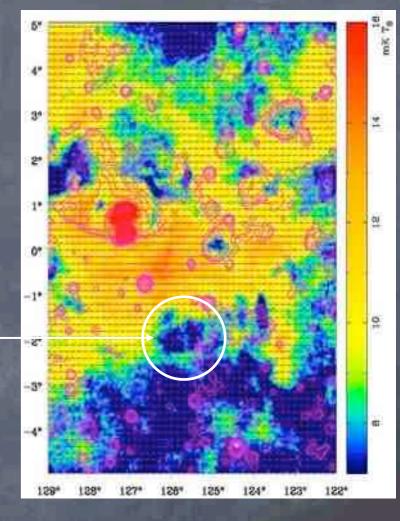
System Temperature	22 K Ta
Telescope Beamwidth	9.5′
Subscan Seperation	3'
Scan Velocity	4'/s
Scan Direction	GL and GB
Theoretical rms-noise for total intensity (1s)	1.4 mK Tb
Theoretical rms-noise for Q/U (1s)	1.0 mK Tb
Central Frequency	4800/4963MHz
Bandwidth	600/295MHz
Aperture Efficiency	62
Beam Efficiency	67
T <i>b</i> [<i>K</i>]/S[Jy]	0.164
Calibrator(Polarized/Non-polarized)	3C286/3C295

Sun et al. 2007

The first survey region





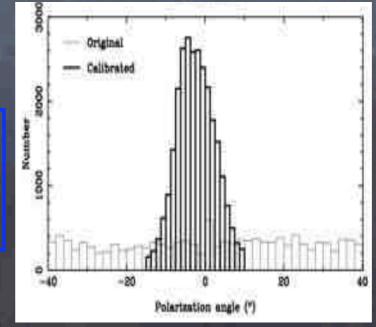


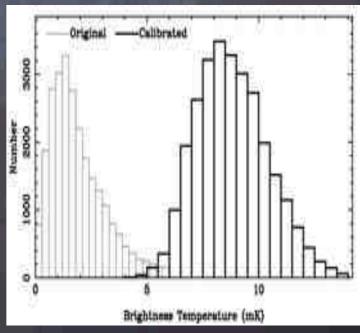
2 New HII regions: G124.0+1.4 and G124.9+0.1

2 Faraday Screens: G125.6-1.8 and G124.9+0.1, HII as FS

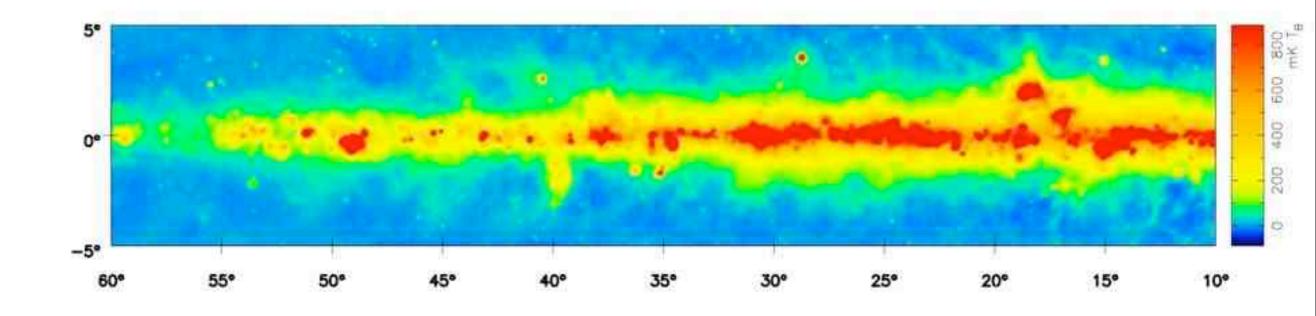
Rule out the spectral curvature of SNR 126.2+1.6

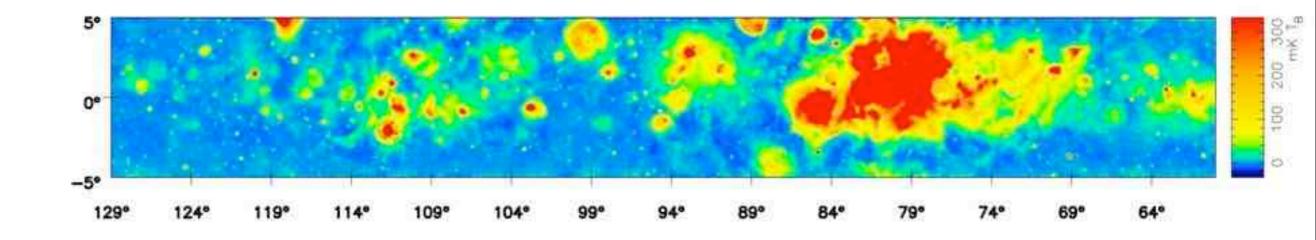
Sun et al. 2007

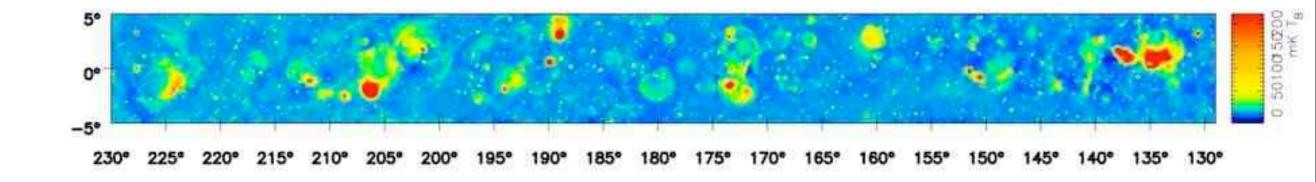


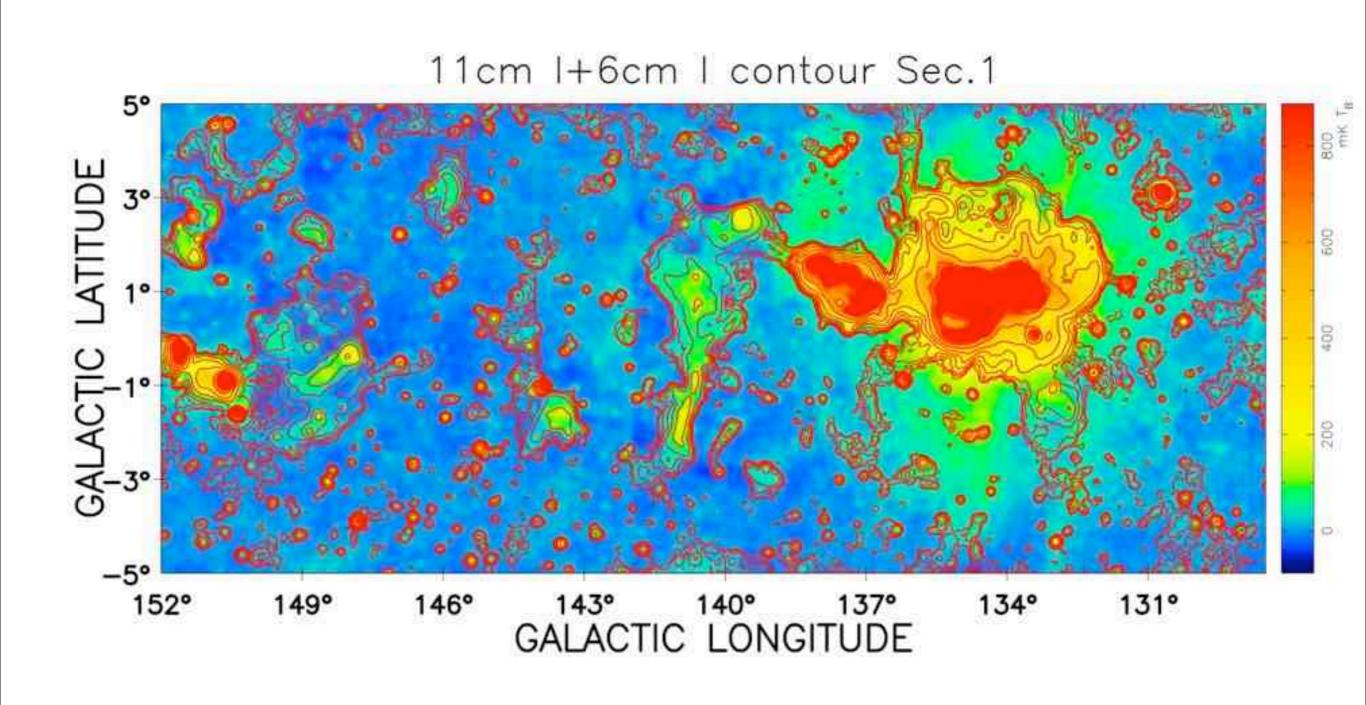


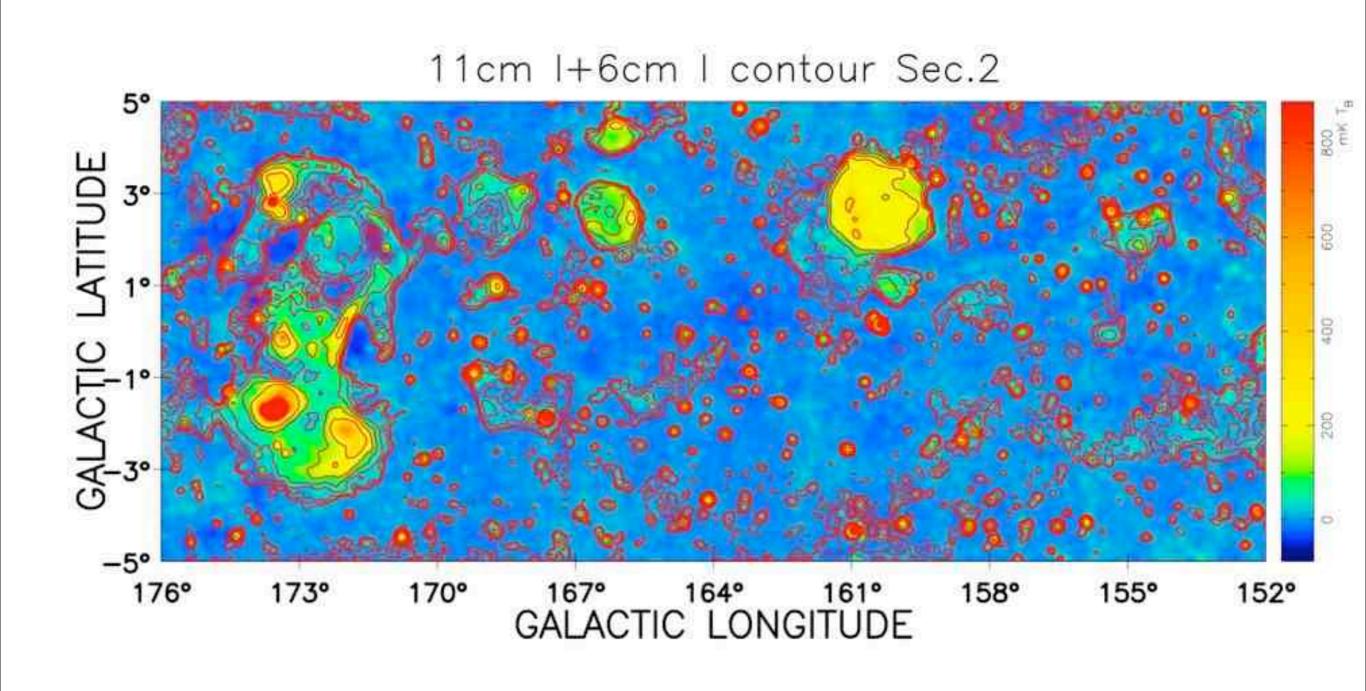


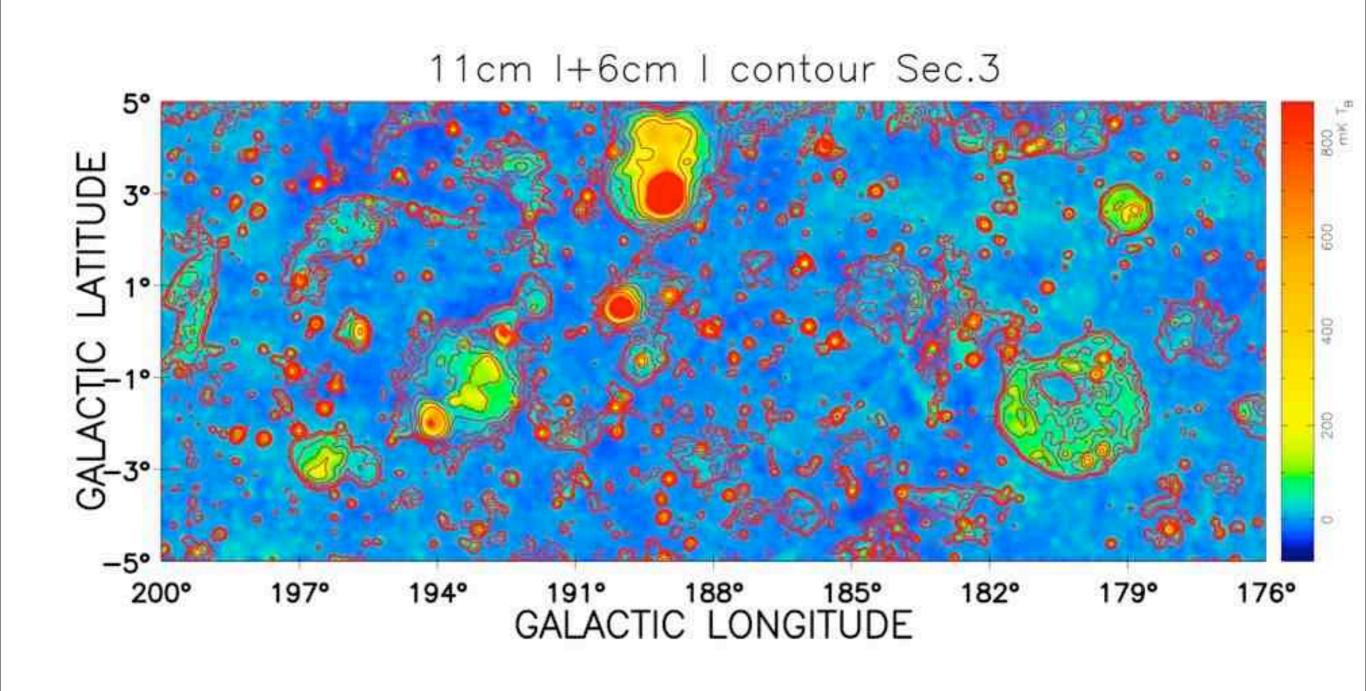


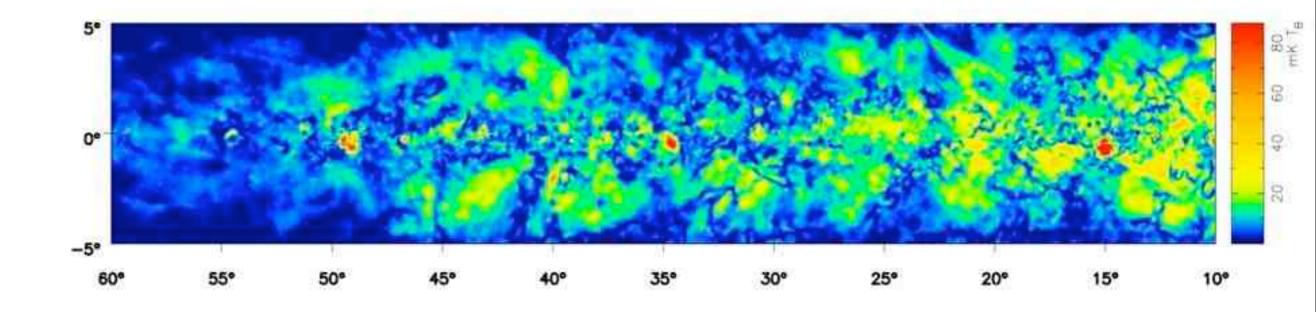


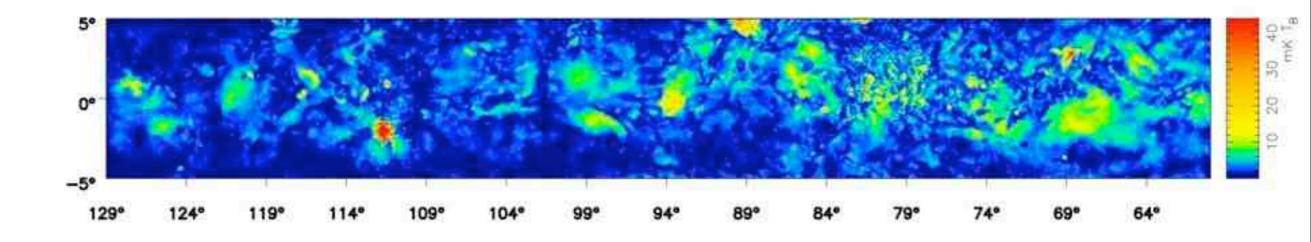


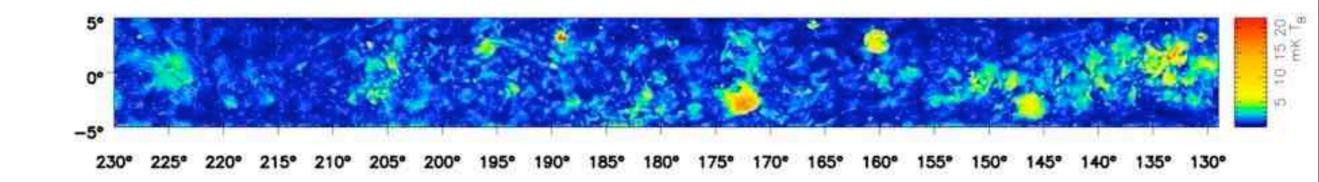






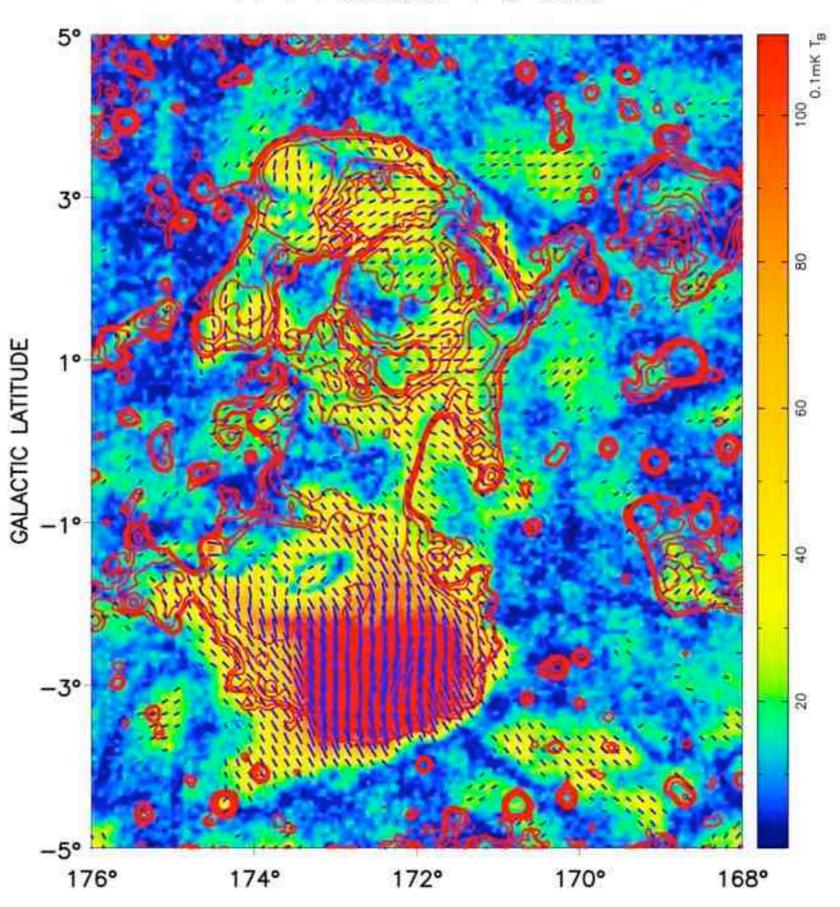






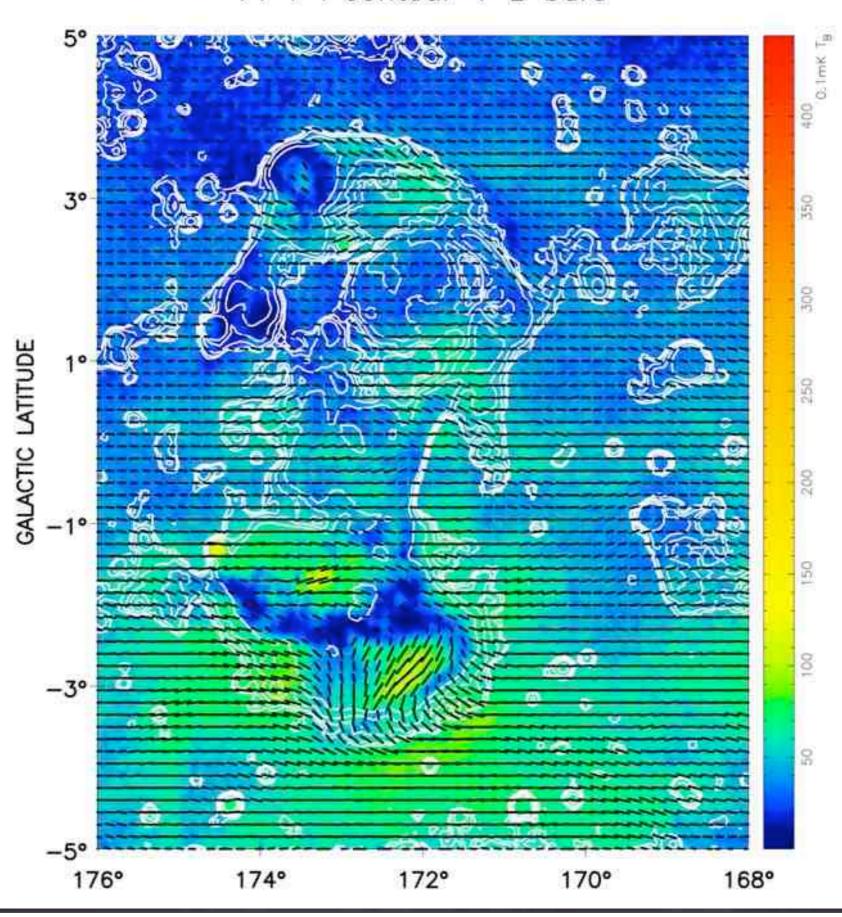
Zero-level restoration by WMAP extrapolation



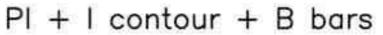


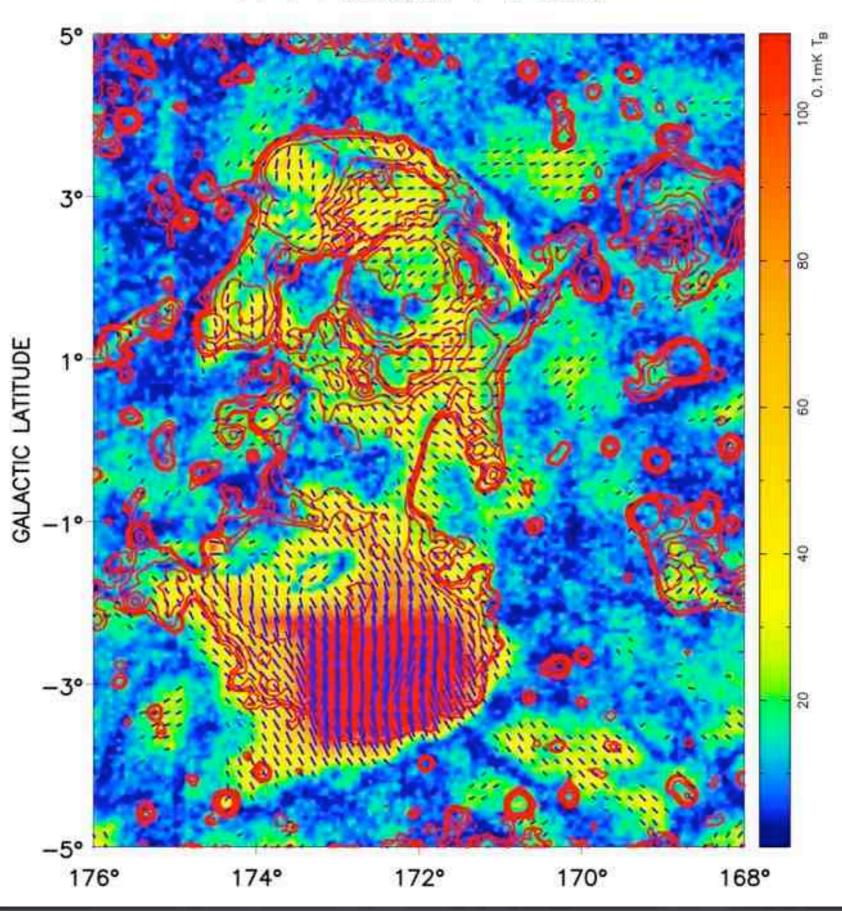
Zero-level restoration by WMAP extrapolation

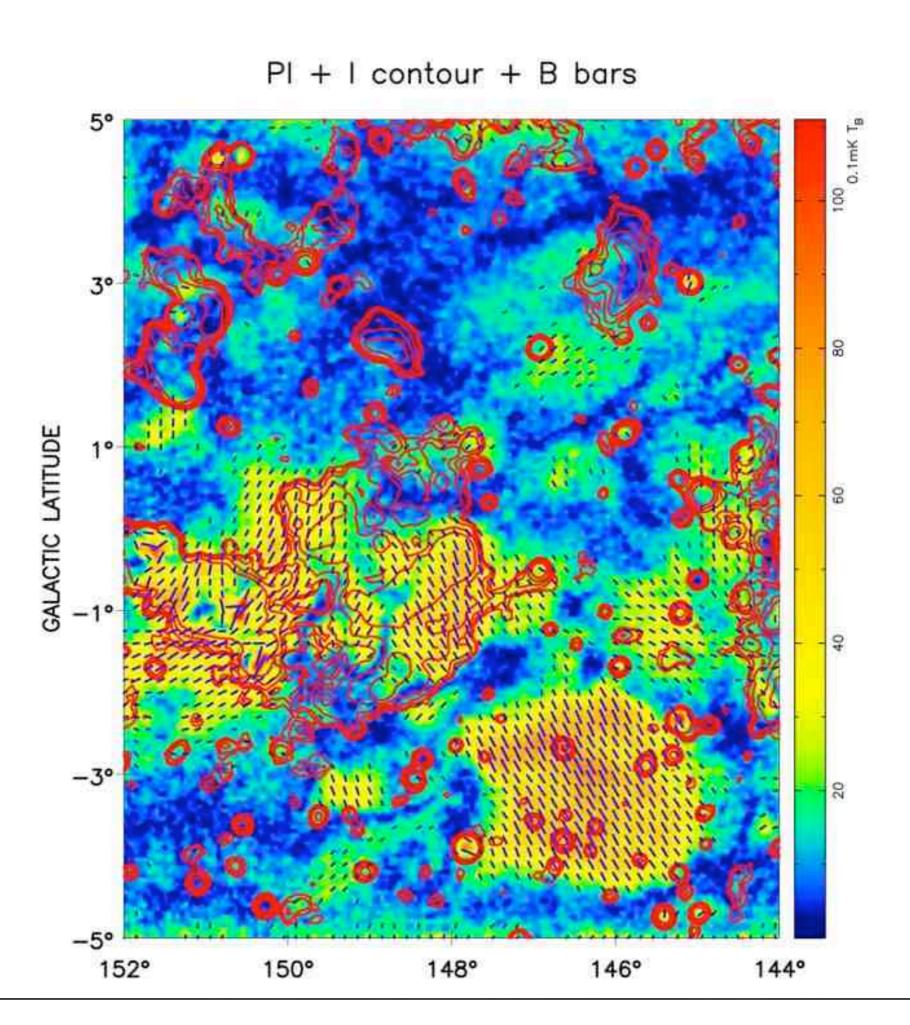
PI + I contour + B bars



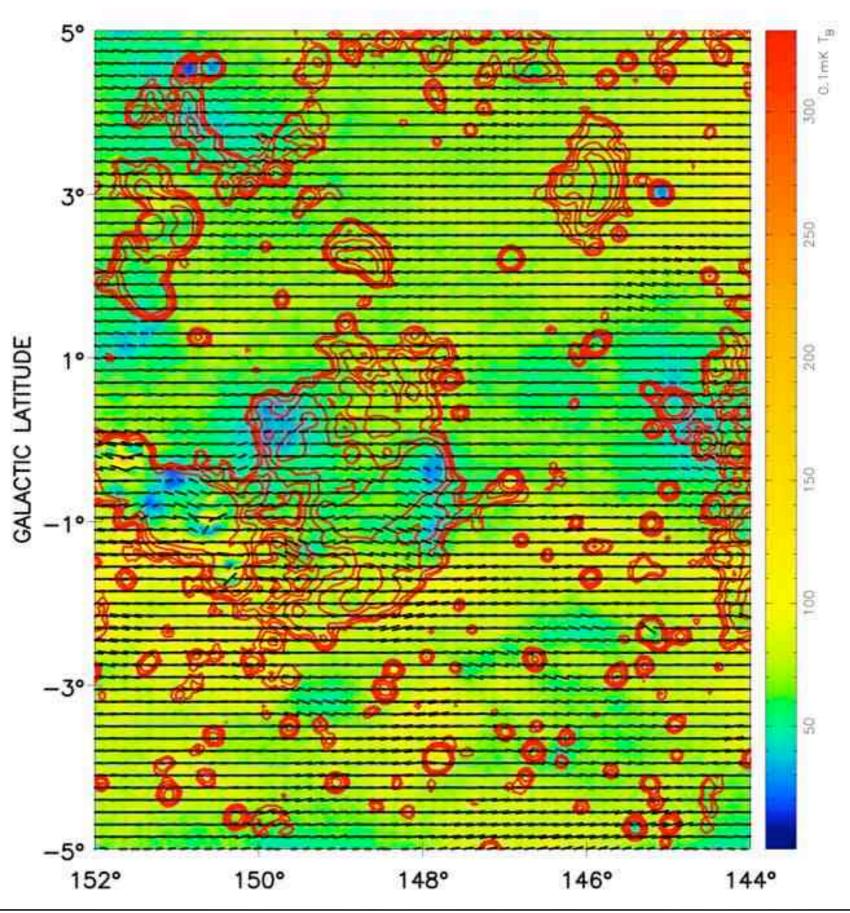
Zero-level restoration by WMAP extrapolation







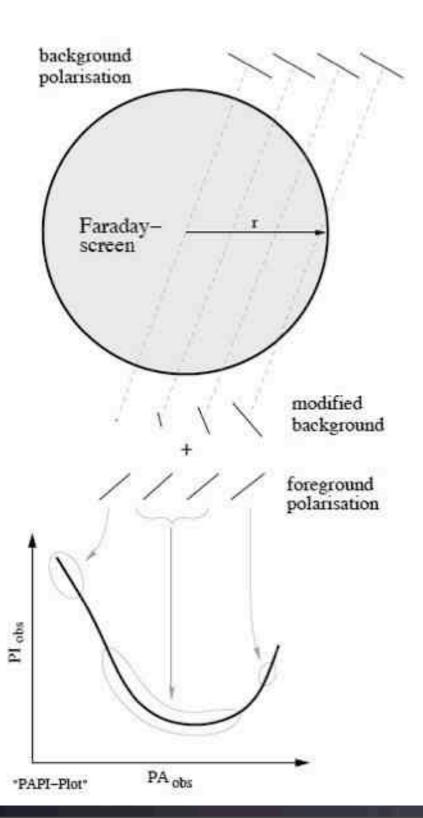




Faraday Screen

- Diffused ionized gas
- HII regions
- Possibly HI clouds
- Surface of molecular clouds

Model of FS

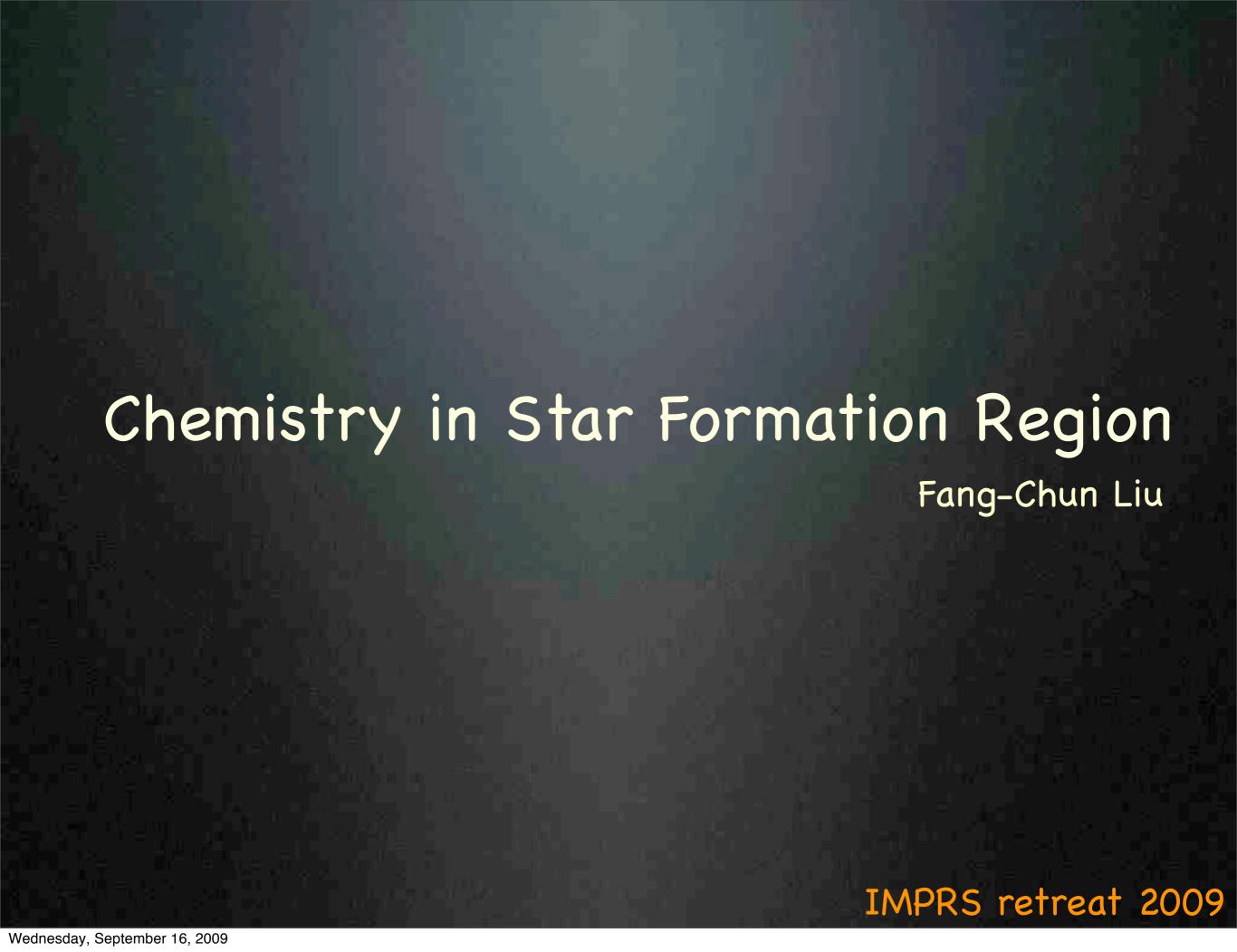


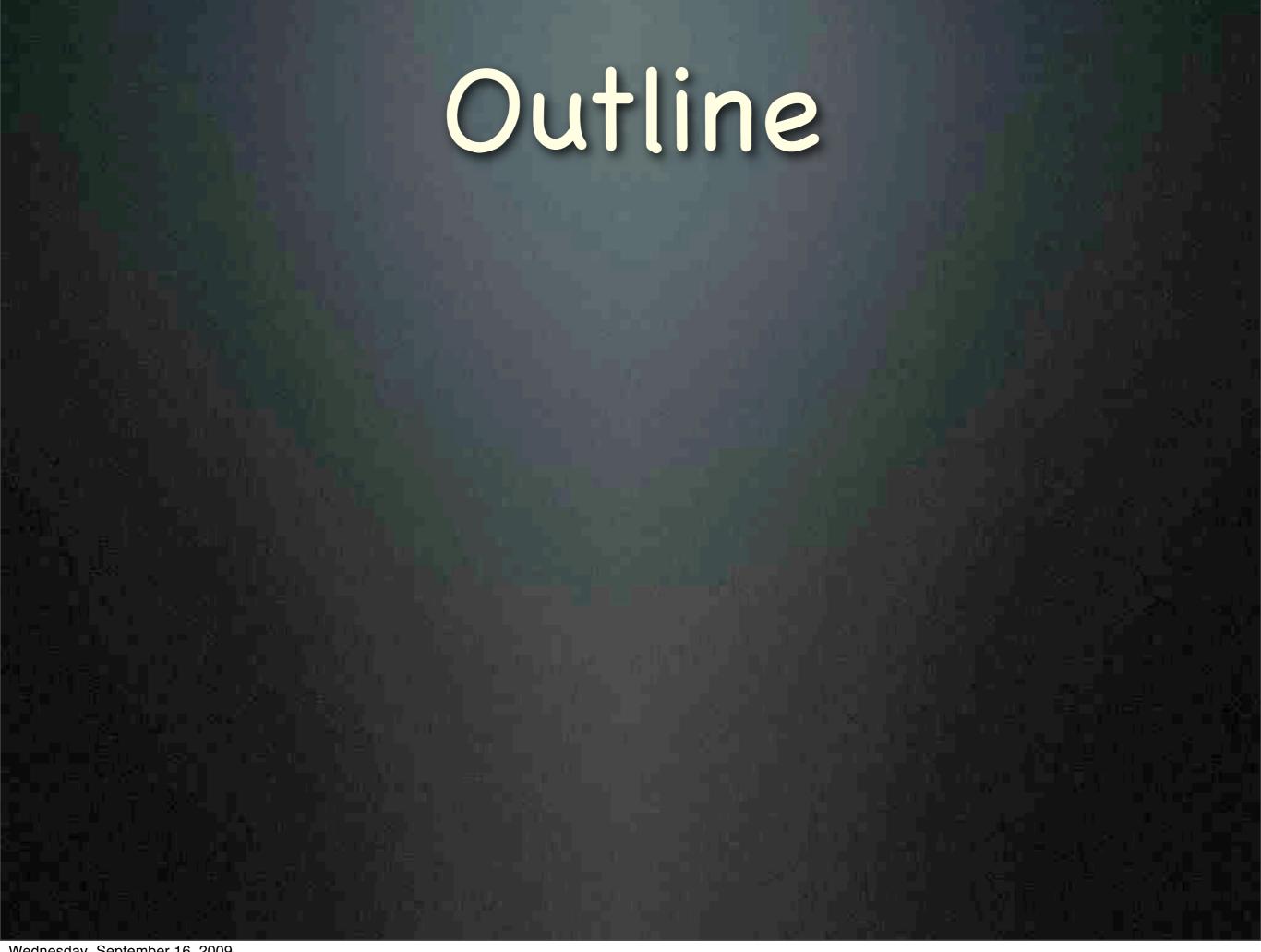
$$\frac{PI_{on}}{PI_{off}} = (f^2(1-c)^2 + c^2 + 2fc(1-c)\cos 2\psi_s)^{1/2}$$

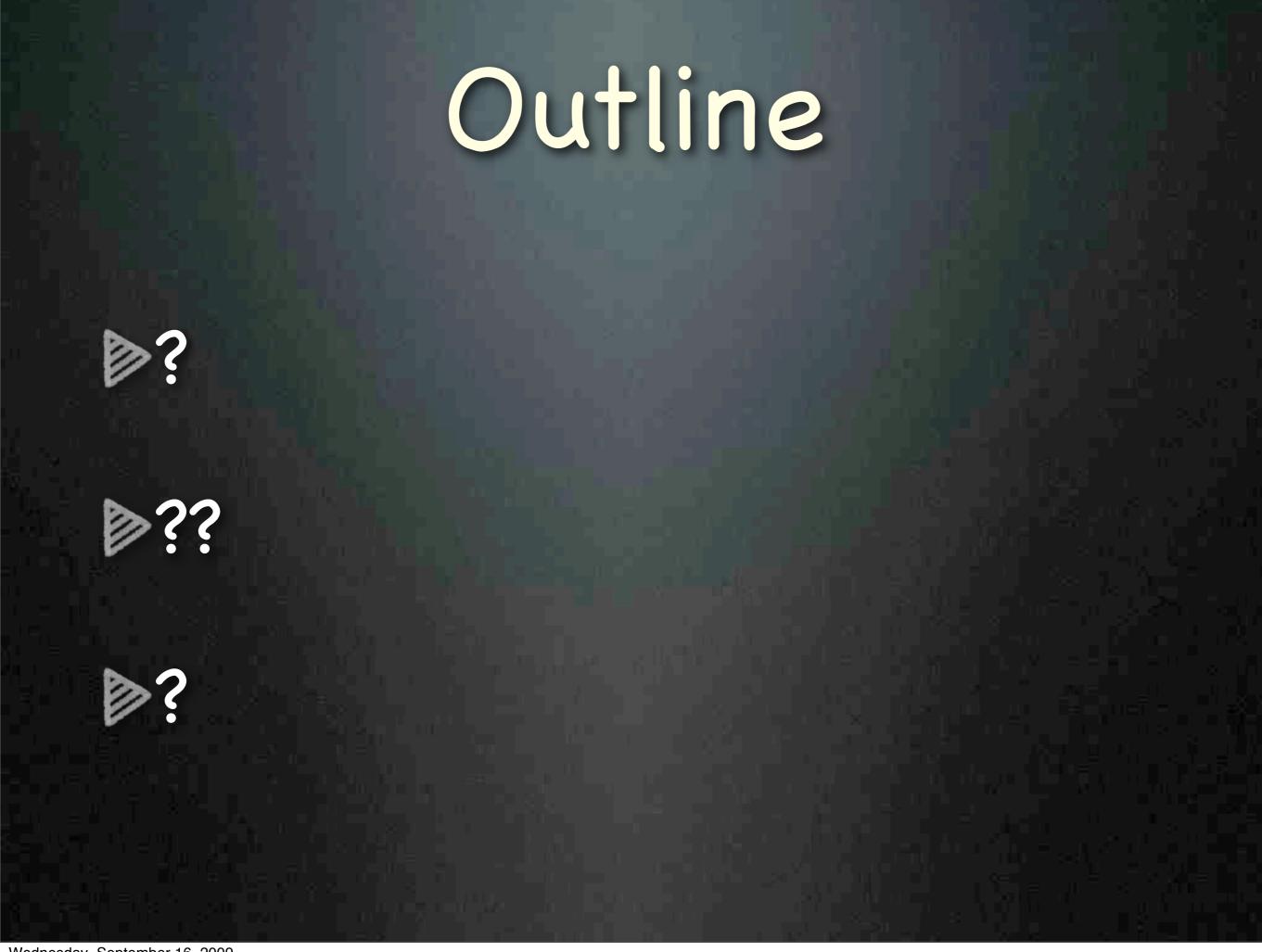
$$\psi_{on} - \psi_{off} = \frac{1}{2} \arctan\left(\frac{f(1-c)\sin 2\psi_s}{c + f(1-c)\cos 2\psi_s}\right)$$

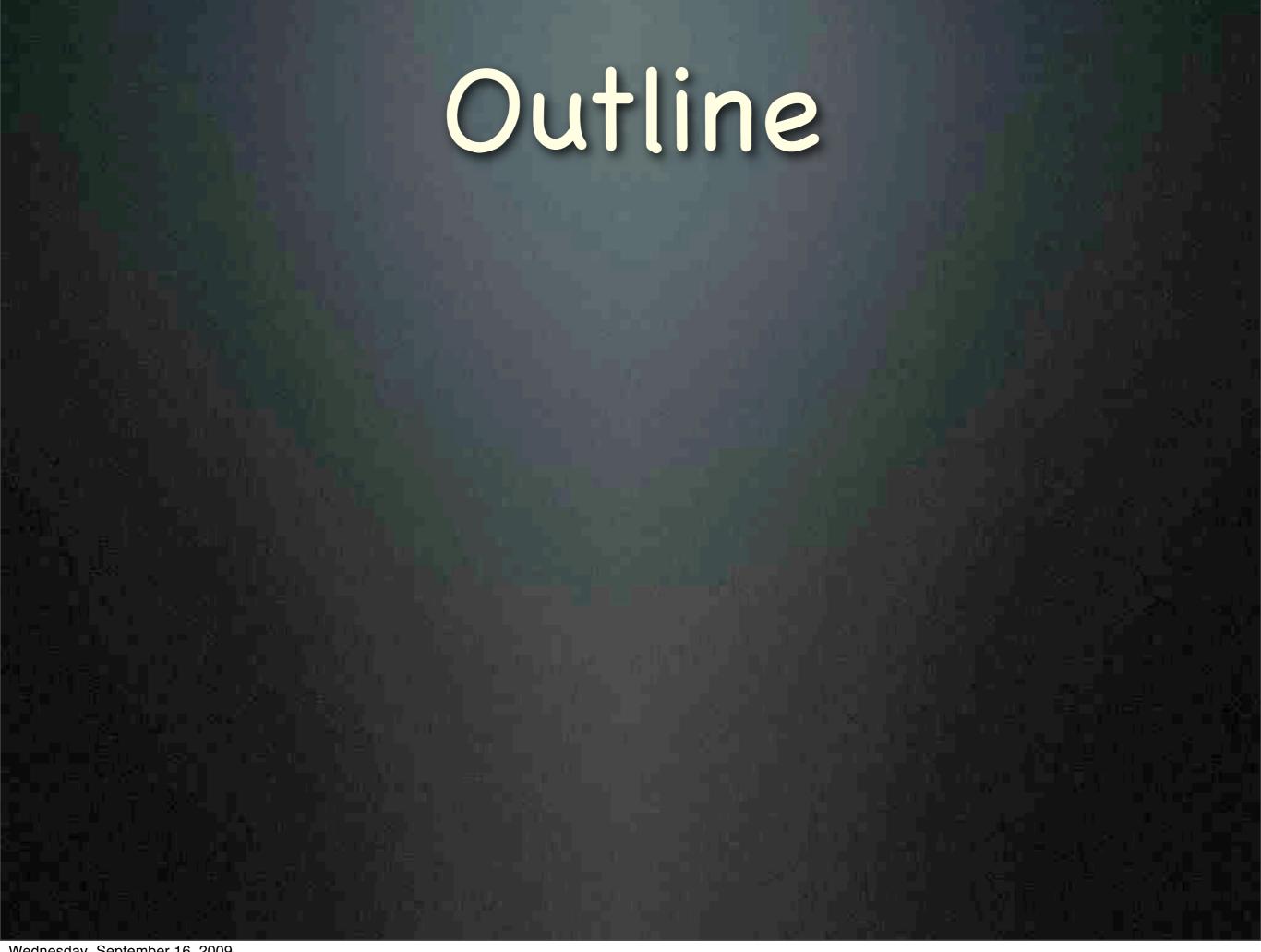
f depolarization factor c foreground PI ratio

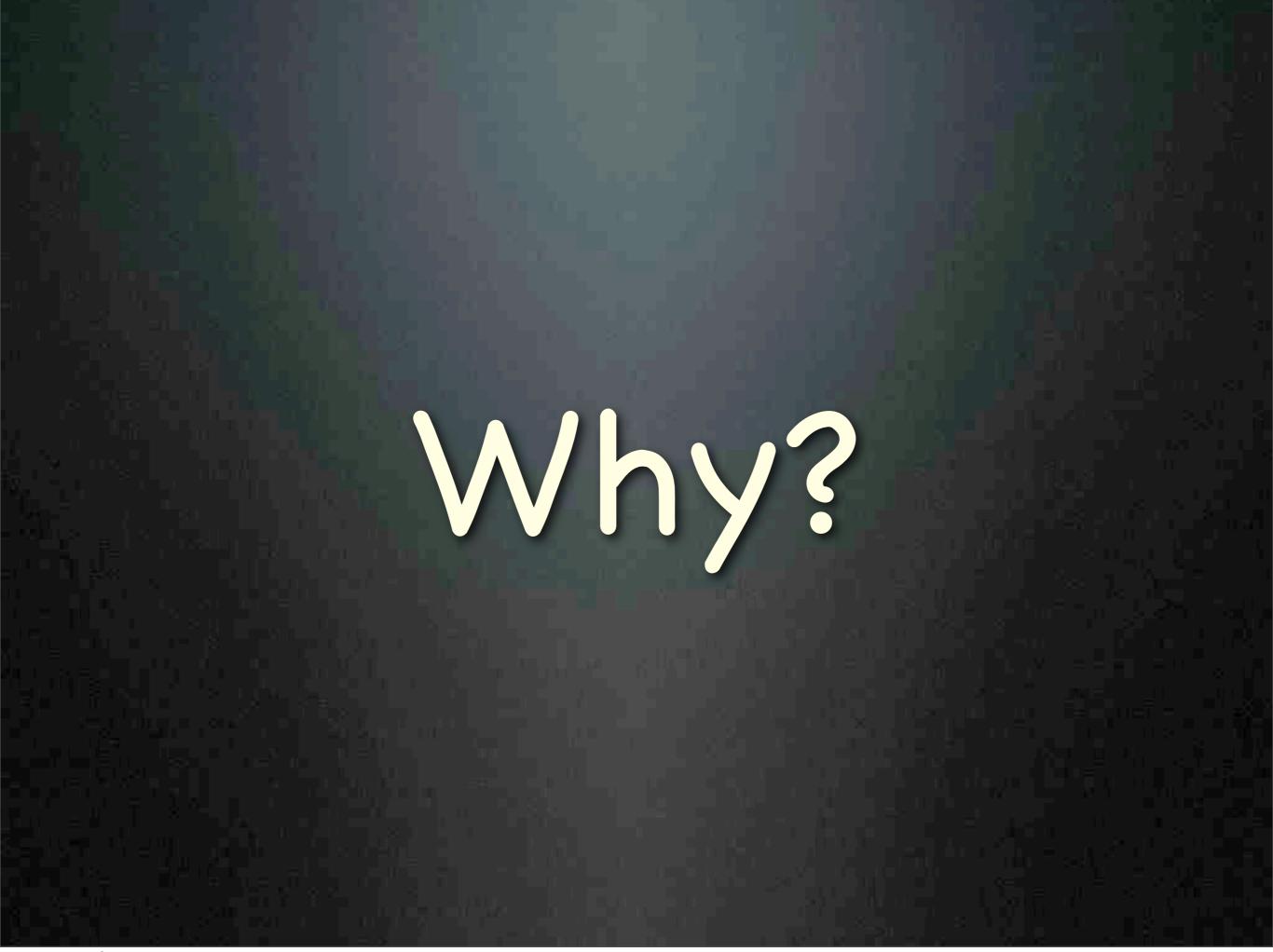


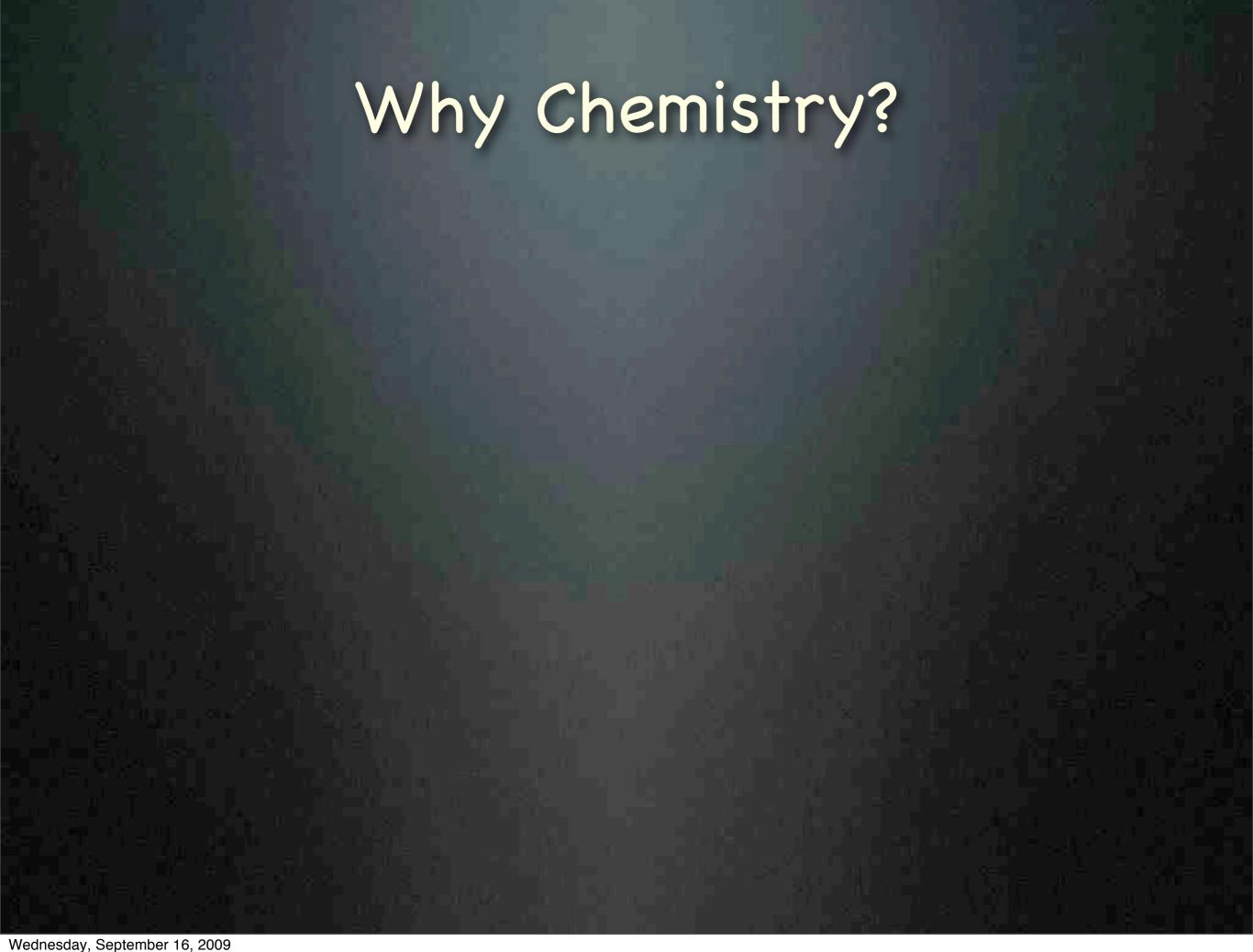










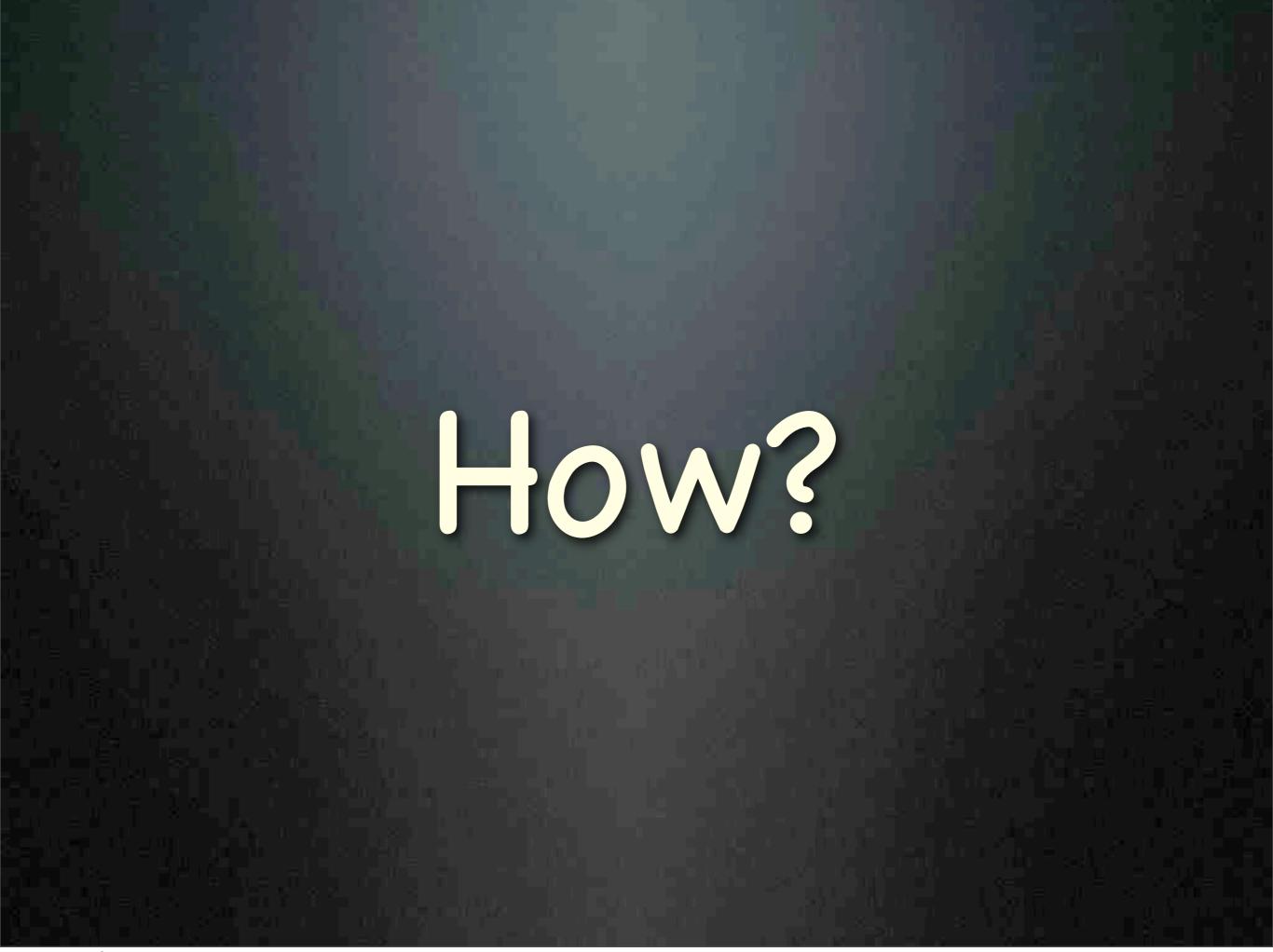


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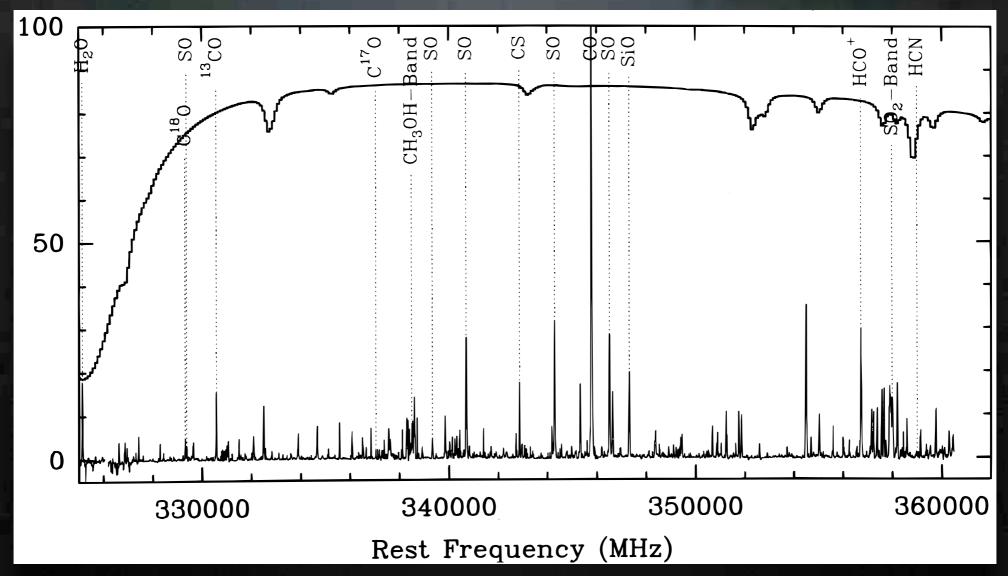
- ▶ Chemistry controls critical physical parameters: the fractional ionization and cooling of the gas.
- Chemistry is a very powerful diagnostic, both of the current and the past physical conditions of the forming protostar.
- ▶ Chemistry (initial composition and later process) affects the chemical composition of the objects that eventually form the star and planetary system.
- Therefore, we need to study the chemistry properties and evolution in the star formation region.



-Observation Techniques

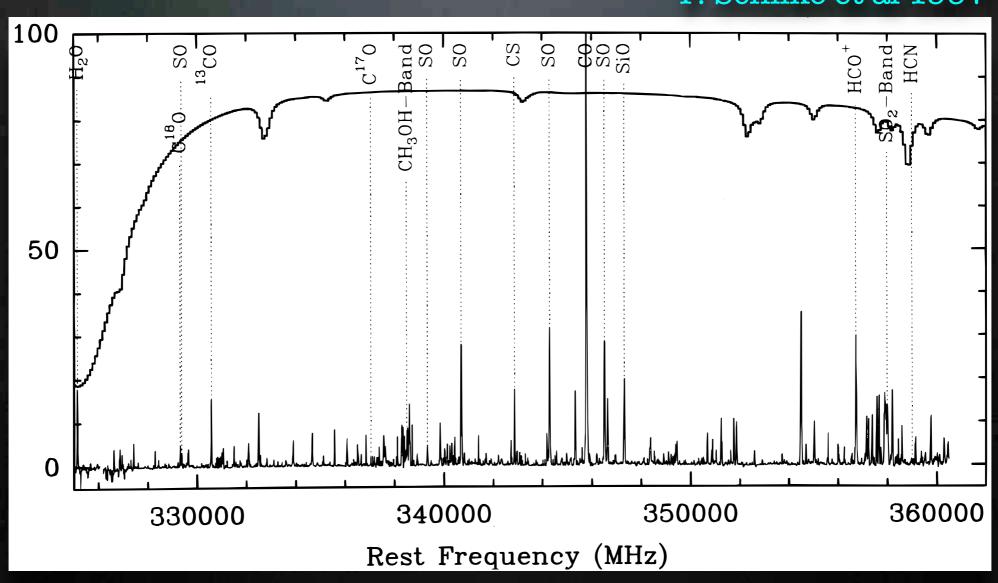
- - 1. Traditionally, most of the chemical information has been derived from (sub)millimeter observations due to the rotation transition.

P. Schilke et al 1997



-Observation Techniques

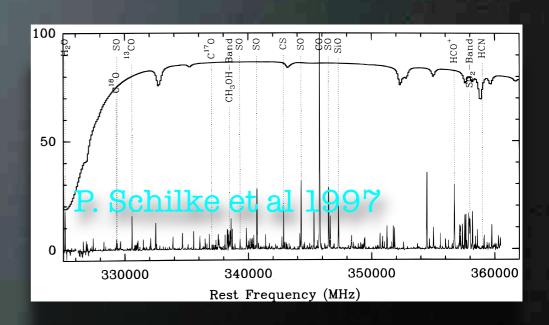
P. Schilke et al 1997





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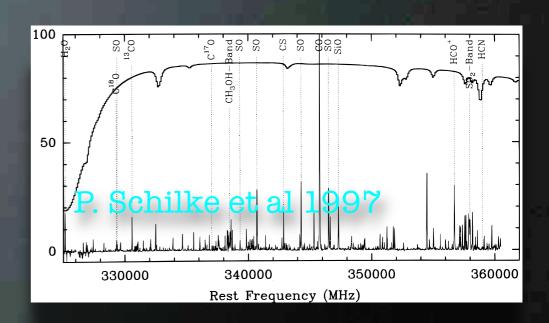


-Observation Techniques

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2. They are not restricted to absorption/emission toward the source but can map the surroundings with high spectral resolution and resolution.

(Kinematic Information and location)

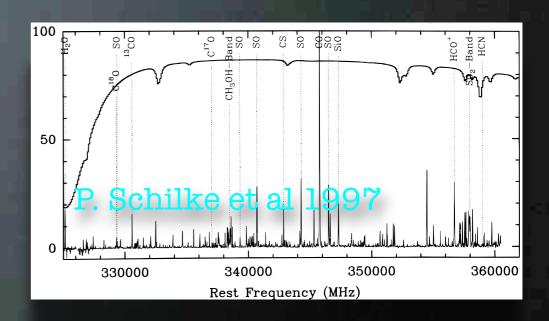


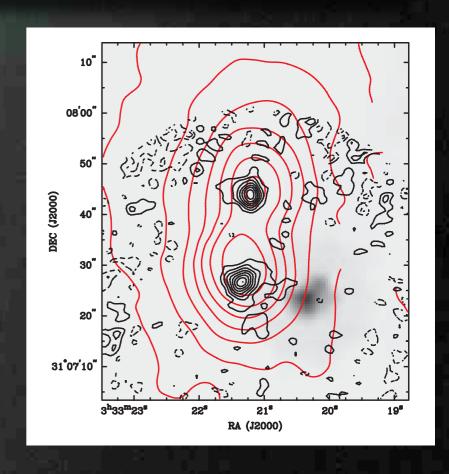
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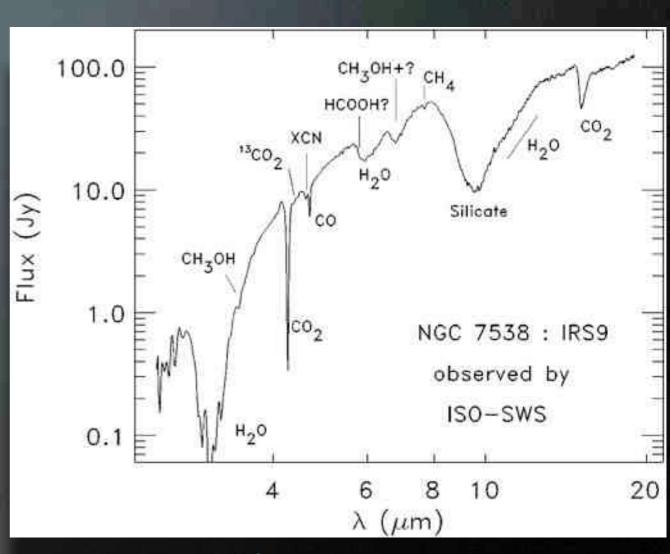
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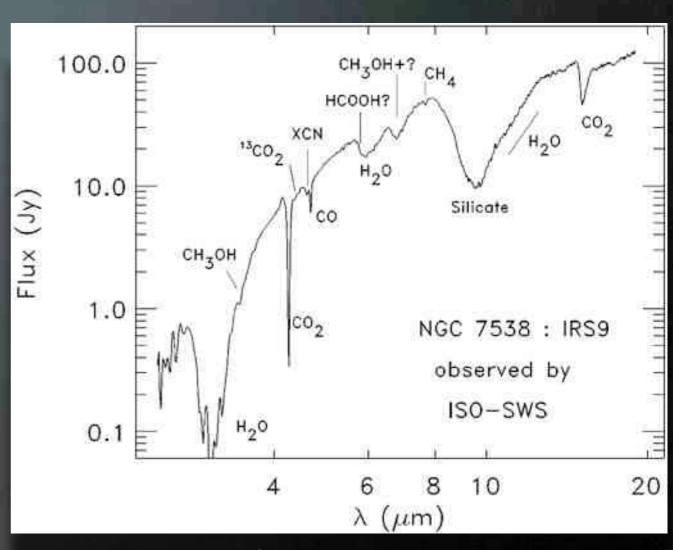






van Dishoeck & Blake 1998

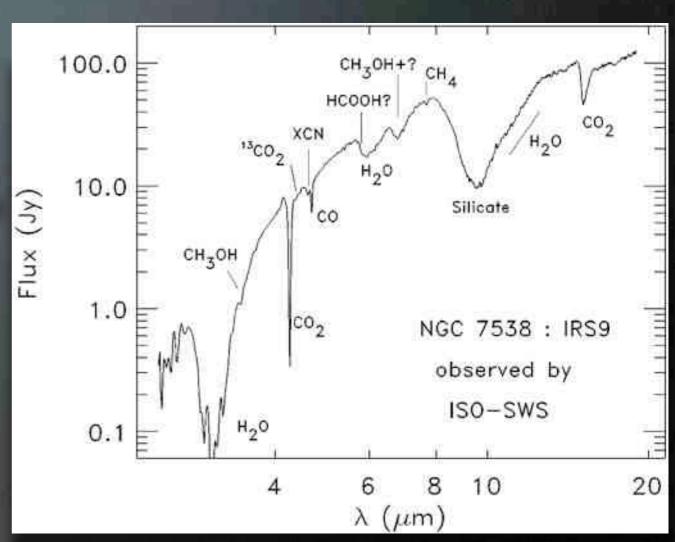
▶ Infrared observations



van Dishoeck & Blake 1998

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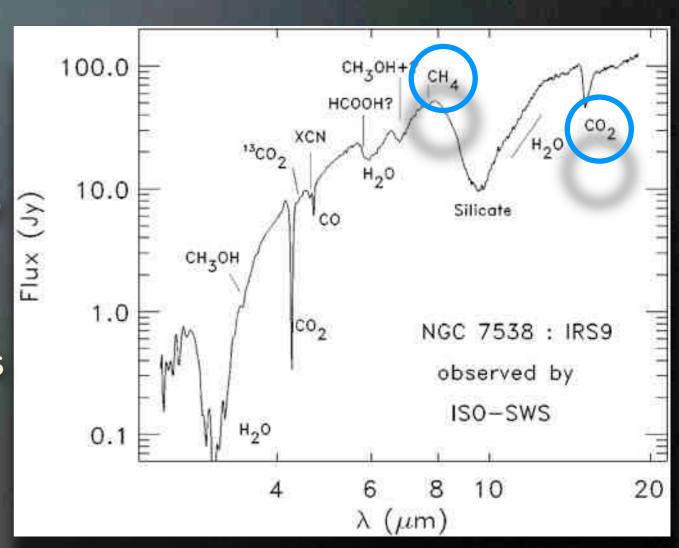
1. It can probe the absorption of material along the line of sight to the embedded young star.



van Dishoeck & Blake 1998

▶ Infrared observations

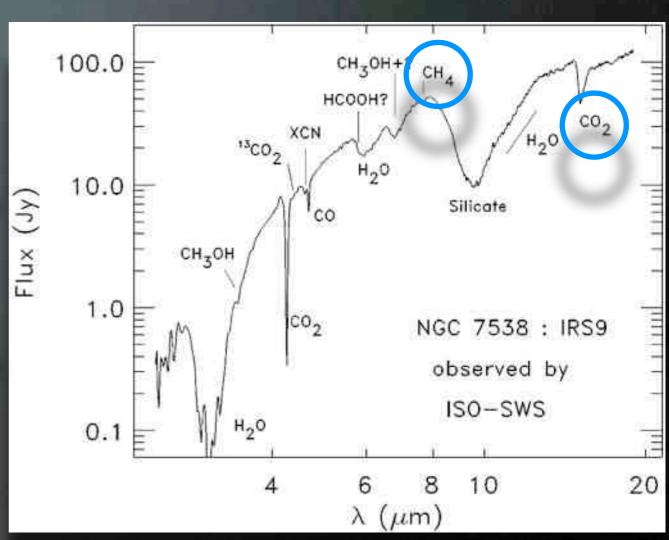
- 1. It can probe the absorption of material along the line of sight to the embedded young star.
- 2. Important molecules without a permanent dipole moment, such as H₃+, CO₂, CH₄, and C₂H₂, possess strong infrared vibrational transitions.



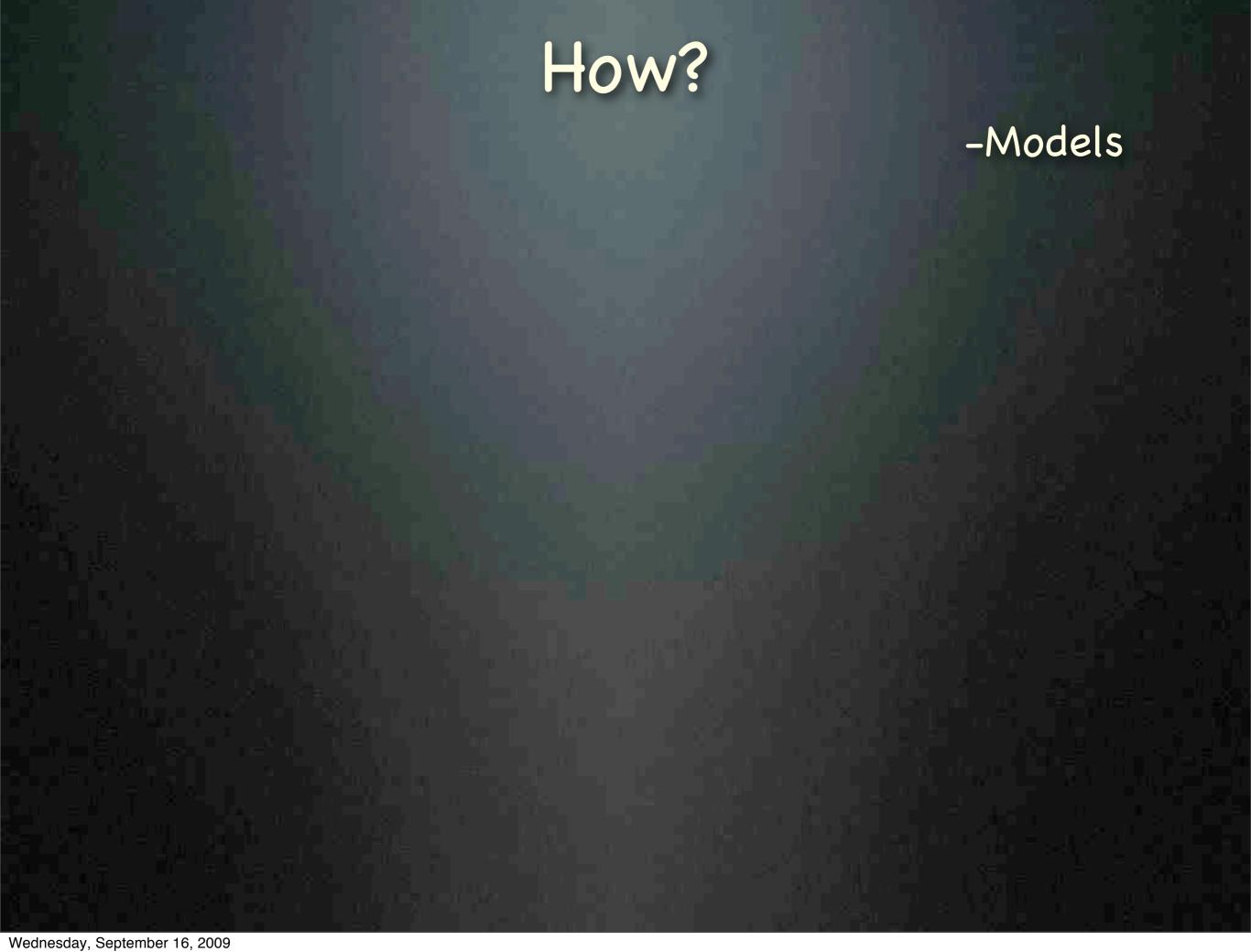
van Dishoeck & Blake 1998

▶ Infrared observations

- 1. It can probe the absorption of material along the line of sight to the embedded young star.
- 2. Important molecules without a permanent dipole moment, such as H₃+, CO₂, CH₄, and C₂H₂, possess strong infrared vibrational transitions.
- 3. Both gas-phase molecules and solid-state species can be detected at infrared wavelengths.



van Dishoeck & Blake 1998



-Models

Two main fundamental models:

-Models

Two main fundamental models:

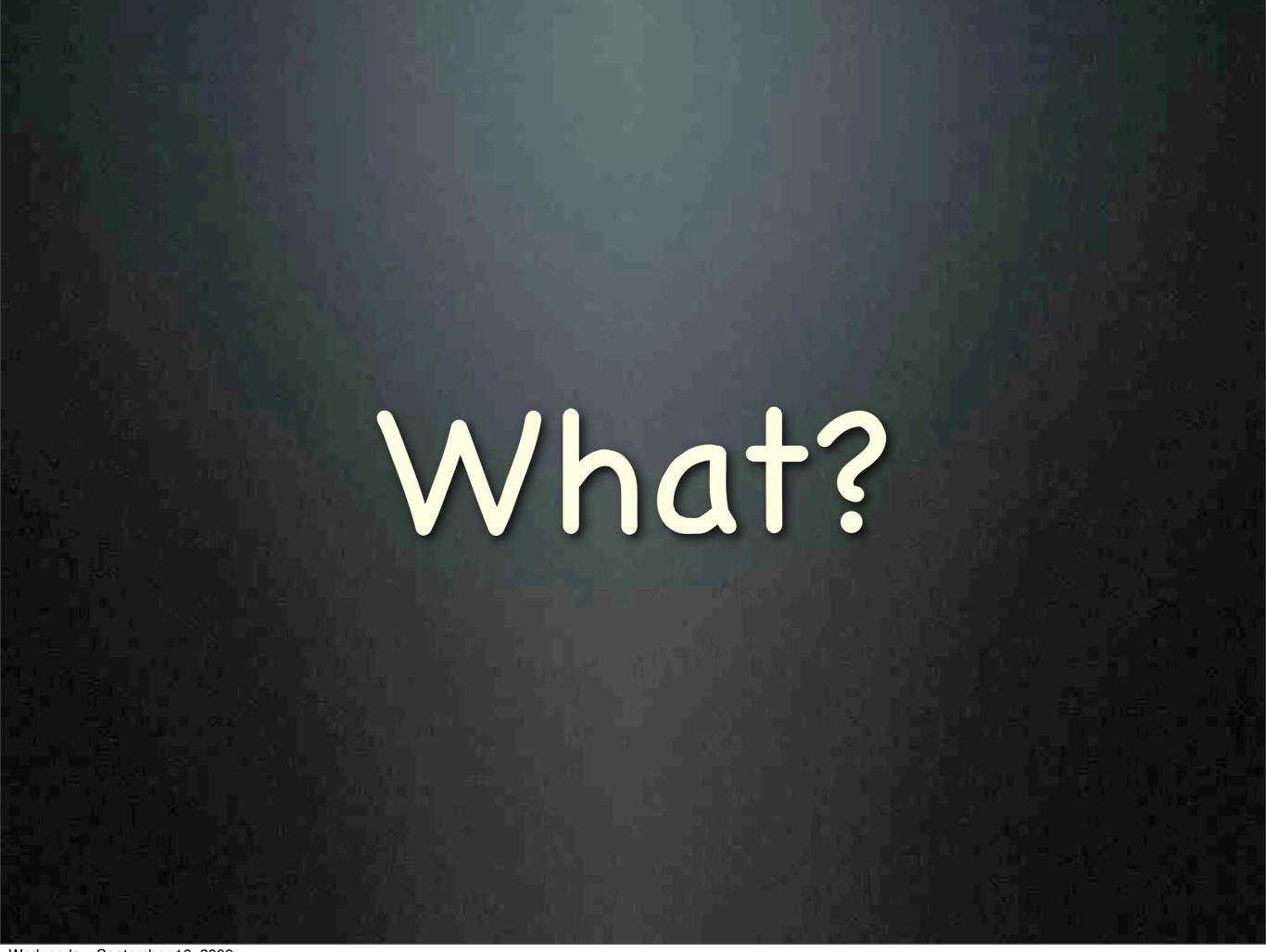
1. Gas-phase chemistry: molecules are form from the reaction in gas-phase. ex: HCO formation.

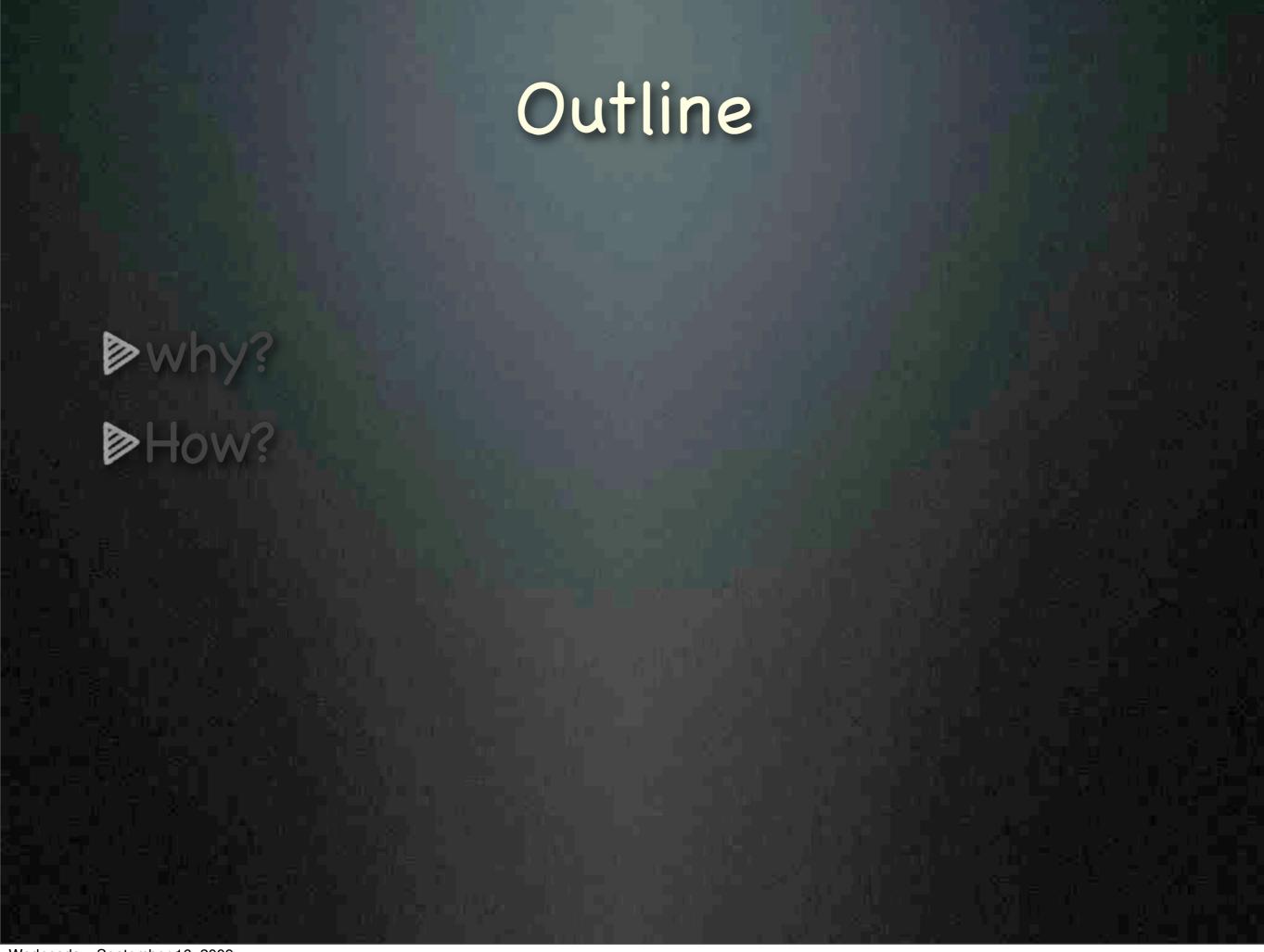
-Models

Two main fundamental models:

1. Gas-phase chemistry: molecules are form from the reaction in gas-phase. ex: HCO formation.

2. Grain-phase chemistry: molecules are form from the reaction in grain-phase. ex: Hz formation.





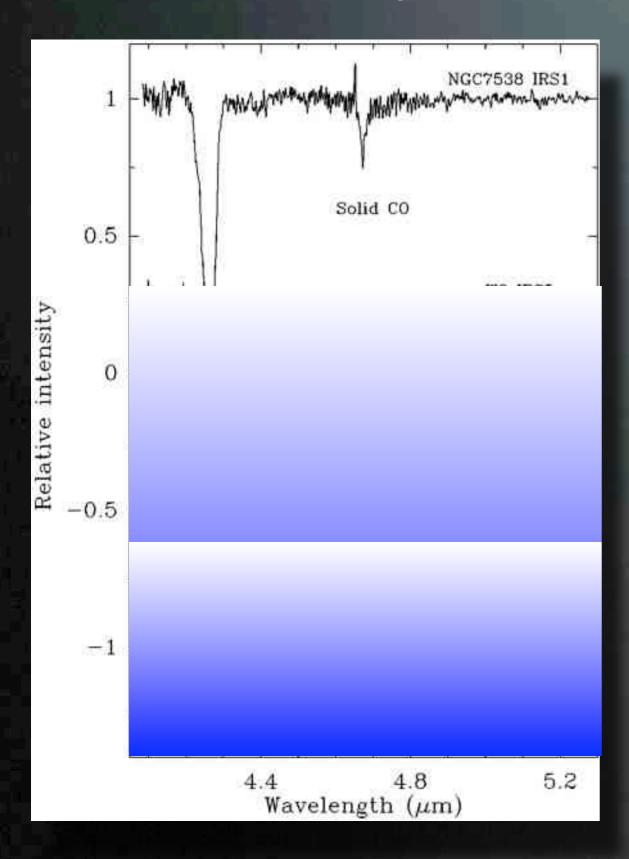
Outline

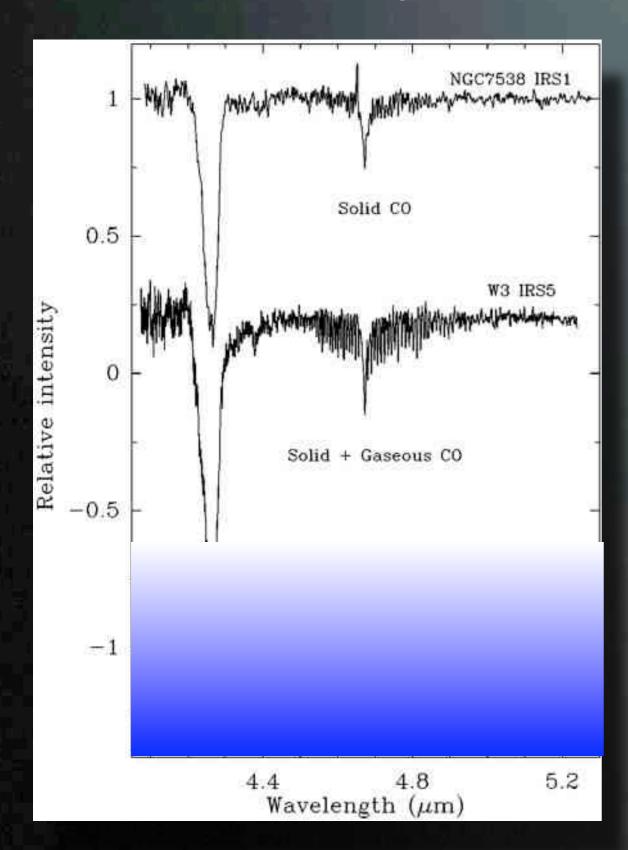
- Dwhy?
- ▶How?
- ▶ Chemistry in
 - Interstellar medium and the Hot Cores
 - Prestellar Cores and Young Protostars

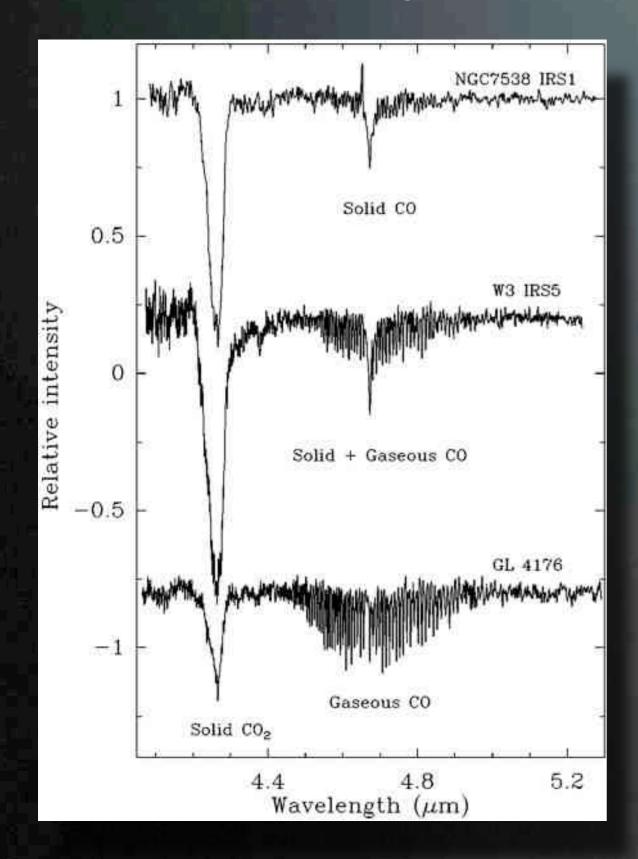
About interstellar medium

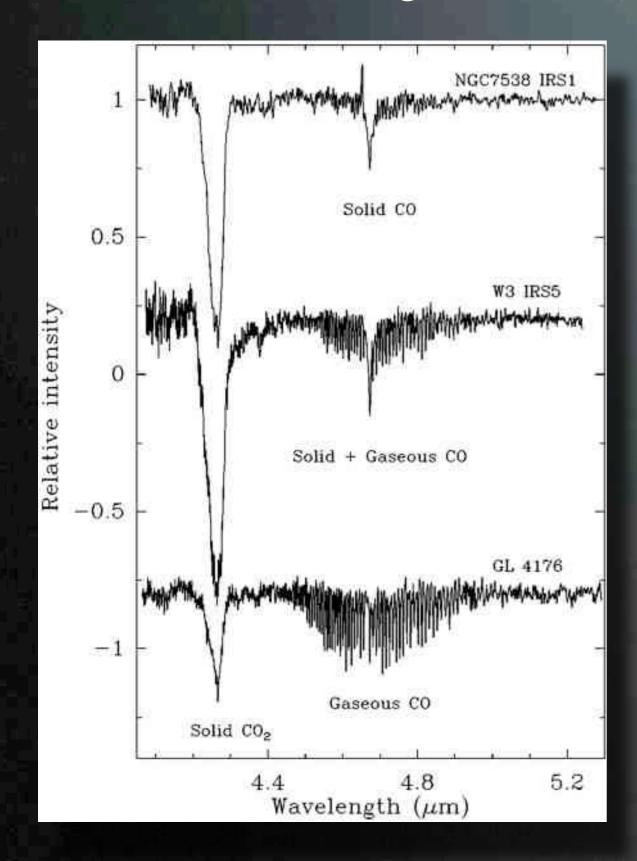


- ▶ Interstellar medium are the sites of a very rich chemistry, as evidenced by the detection of nearly 120 different molecules.
- The observed species range from single diatomic molecules in diffuse clouds to long, unsaturated carbon chains in dark pre-star-forming clouds and saturated organic species near massive YSOs.

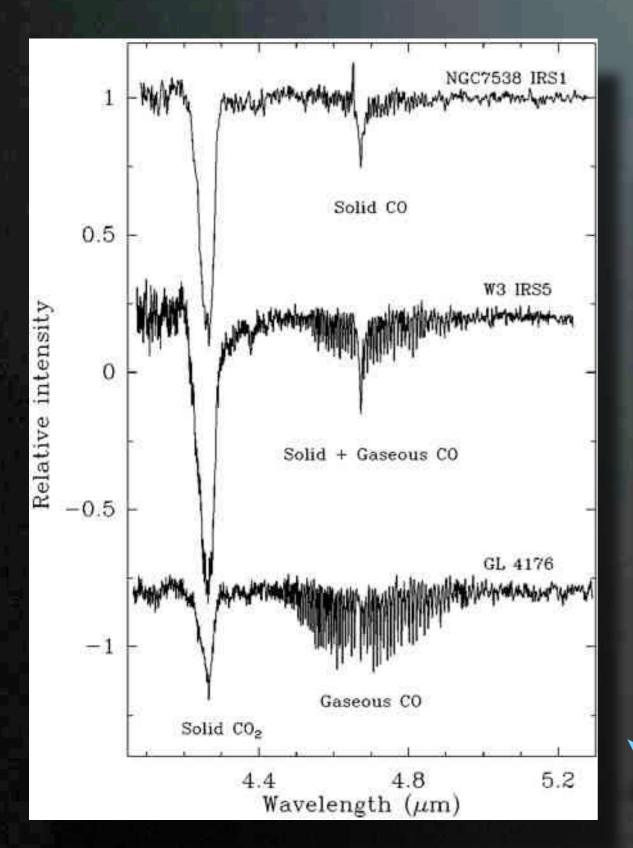








The spectra of the solid-state CO_2 and solid- and gas-phase CO infrared absorption feature toward embedded massive YSOs, illustrating the evaporation of ices and development of a "hot core" region near W3 IRS5 and AFGL 4176.



- The spectra of the solid-state CO_2 and solid- and gas-phase CO infrared absorption feature toward embedded massive YSOs, illustrating the evaporation of ices and development of a "hot core" region near W3 IRS5 and AFGL 4176.
- The relative ratios of these features can be used as an indicator of the evolutionary state (van Dishoeck et al 1996, 1998).

Evolution

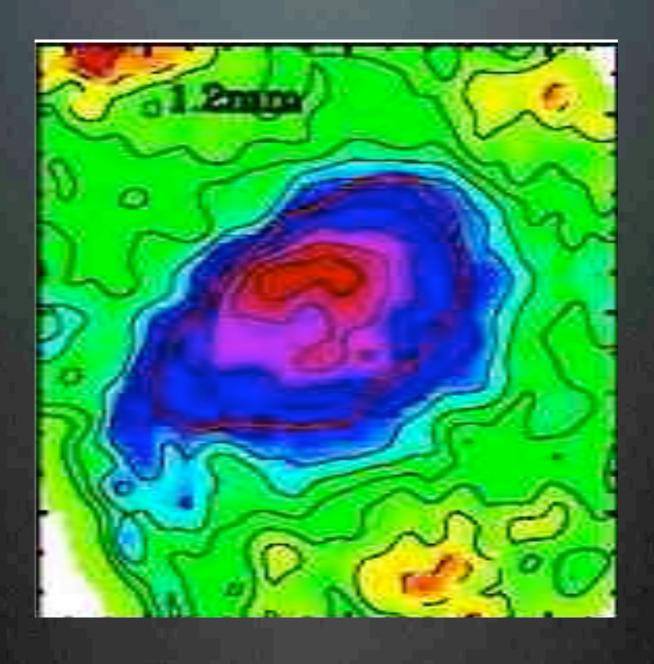
Outline

- Dwhy?
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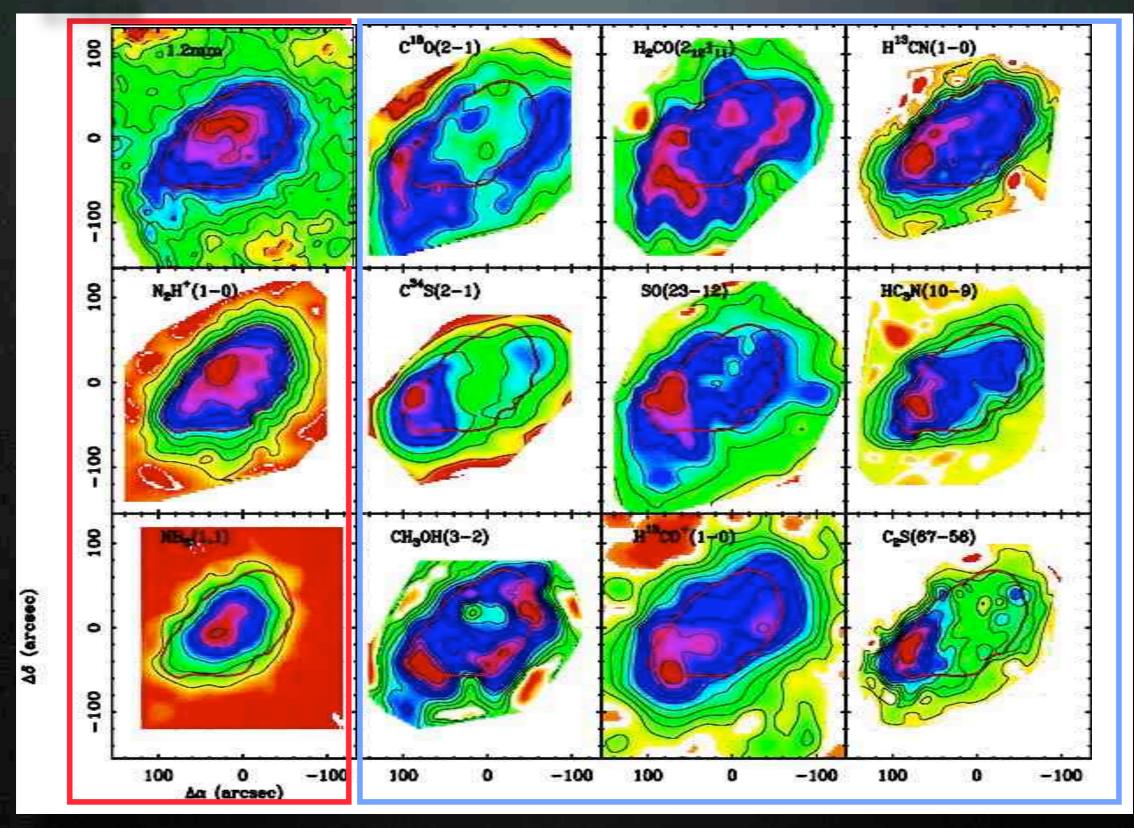
Gravitational bounded cores

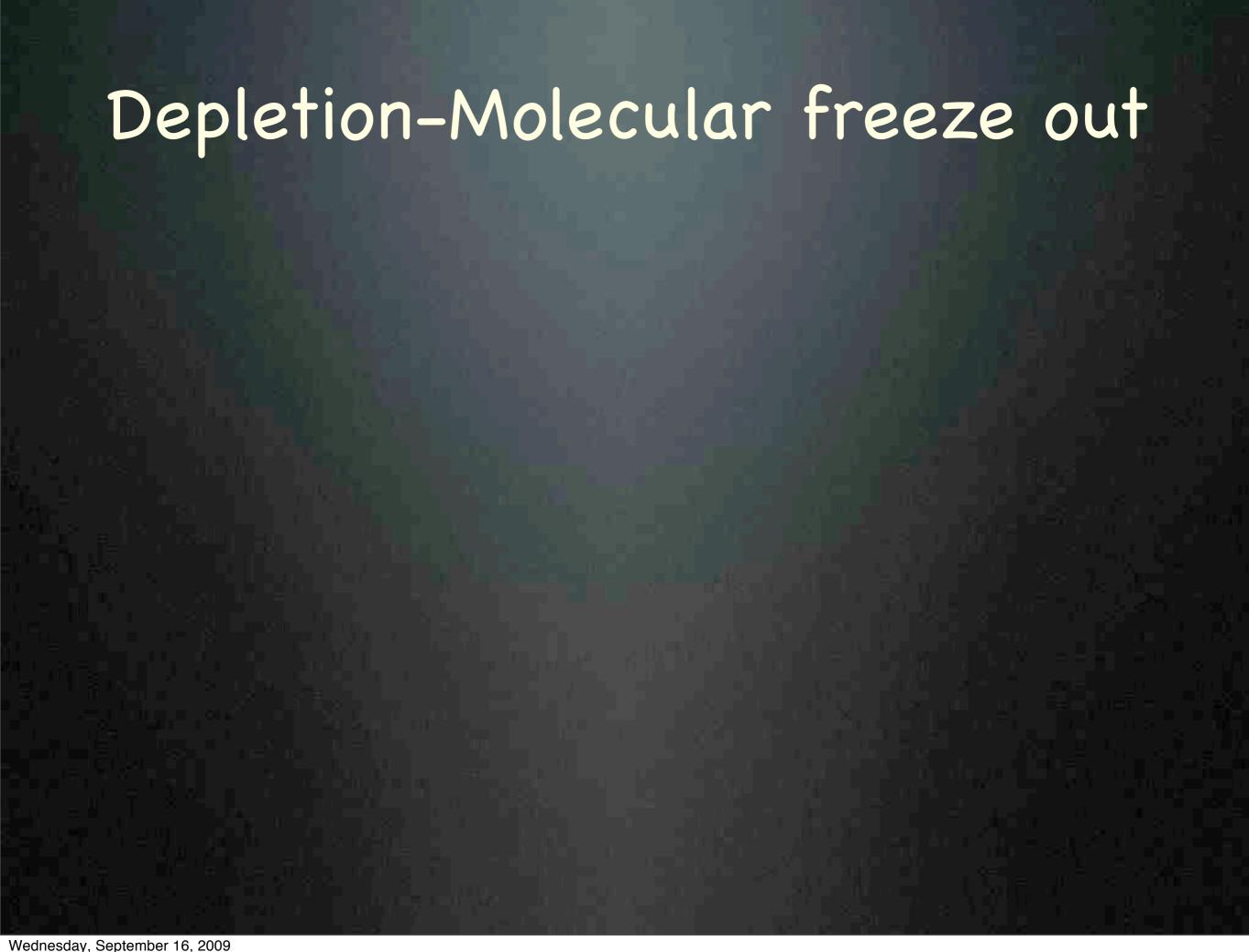
Central condensation without protostellar objects (No IR sources inside)

(Ward-Thompson et al. 1994).



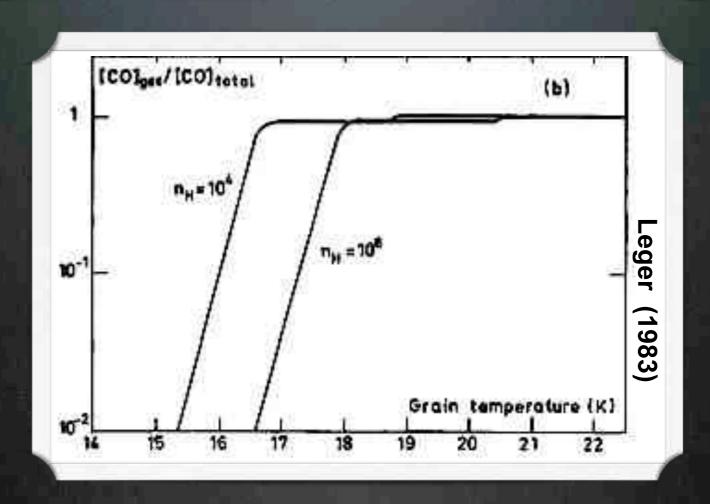
Tafalla et al. 2006





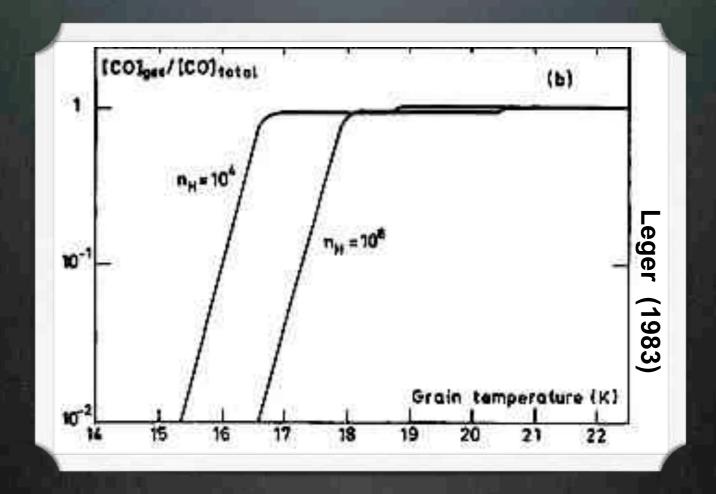
Depletion-Molecular freeze out

- ▶ Gas-grain equilibrium (sticking vs evaporation)
 - if Tgrain > Tfreezeout, most molecules in gas phase
 - if Tgrain < Tfreezeout, most molecules on grains



Depletion-Molecular freeze out

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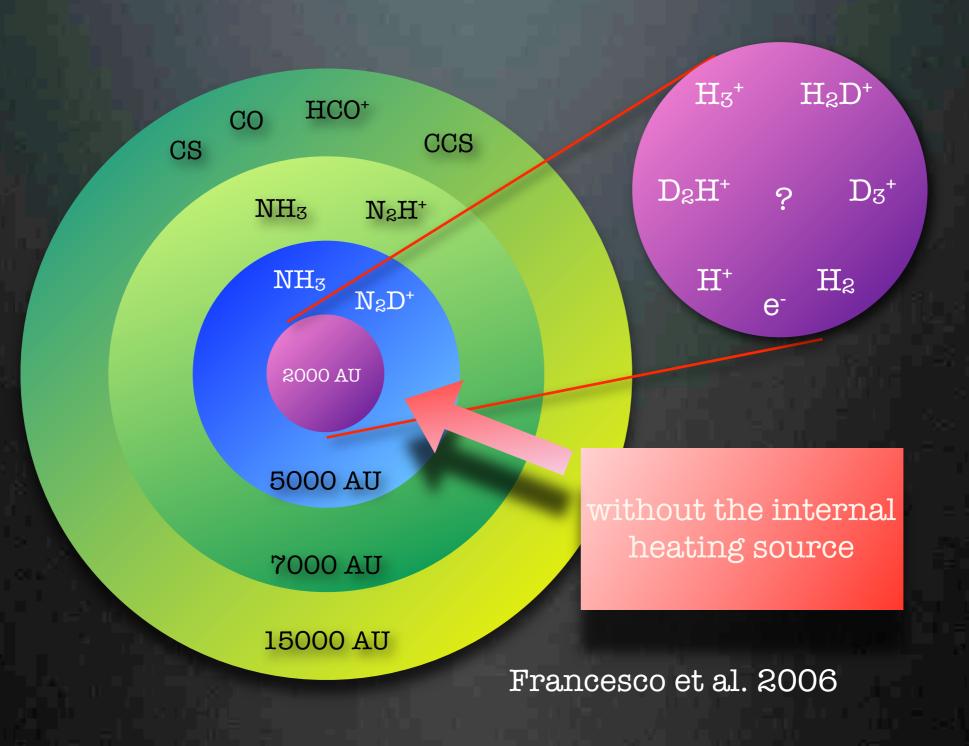


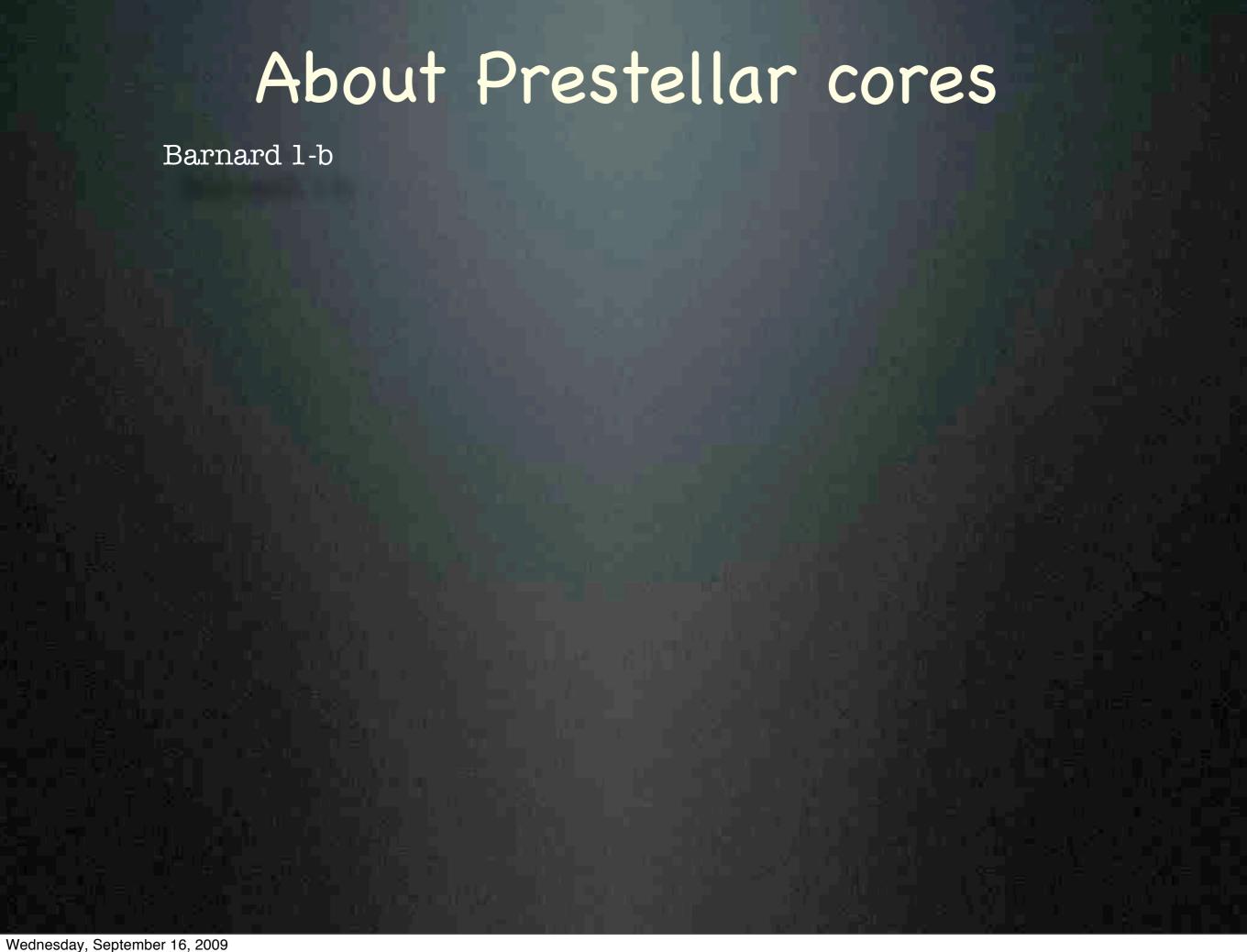
At low temperatures: molecules stick on grains and do not evaporate back to gas phase: freeze-out

Depletion-Molecular freeze out

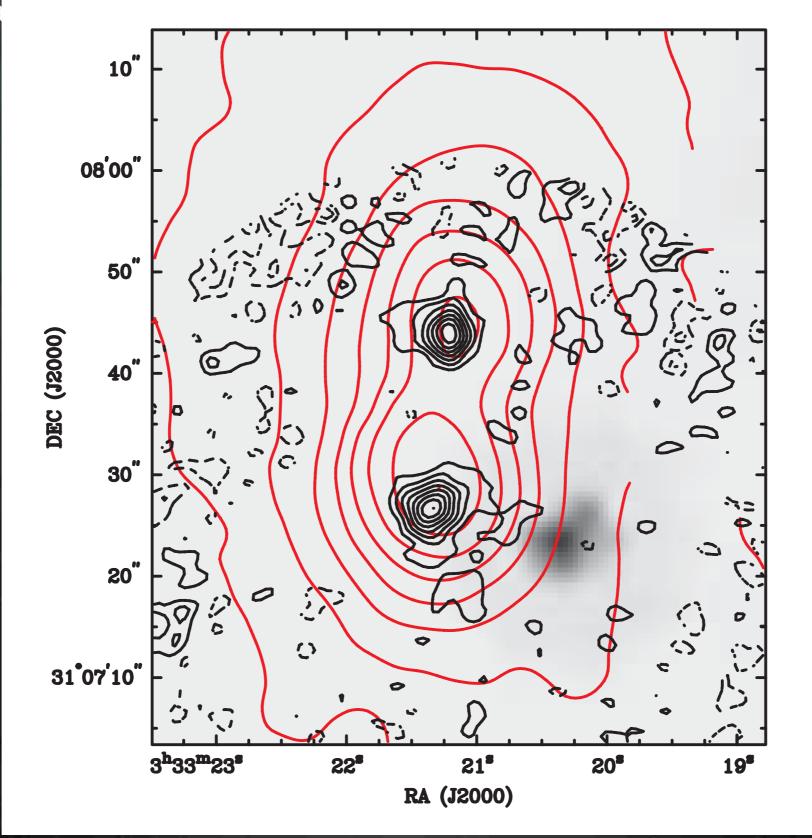
- Most species disappear from gas phase at ≈ 5x10⁴ cm⁻³
- CO, CS, HCN, HCO⁺, H₂CO, C₂S, CH₃OH, SO, HC₃N, C₃H₂, ...
- poor tracers of core interior

- Only survivers
- (H_2) , NH_3 , N_2H^+ , H_3^+ and D-isotopologues (i.e., H_2D^+)
- only line tracers of internal core (dust in continuum)

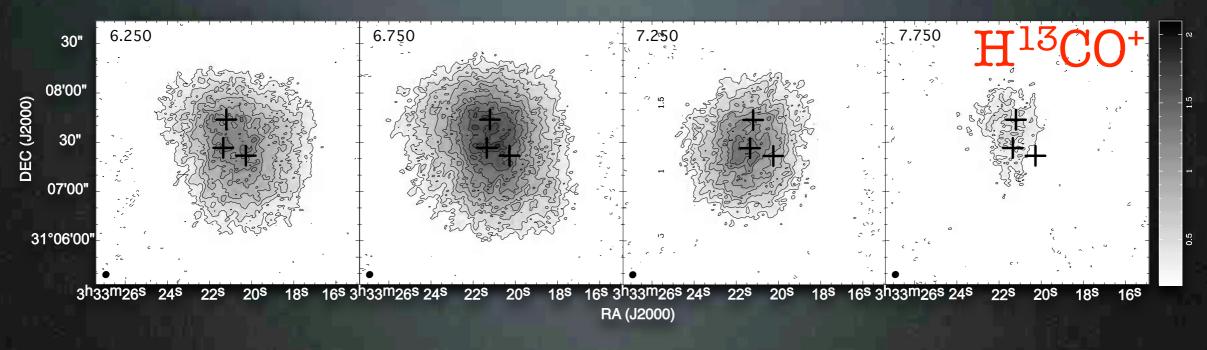




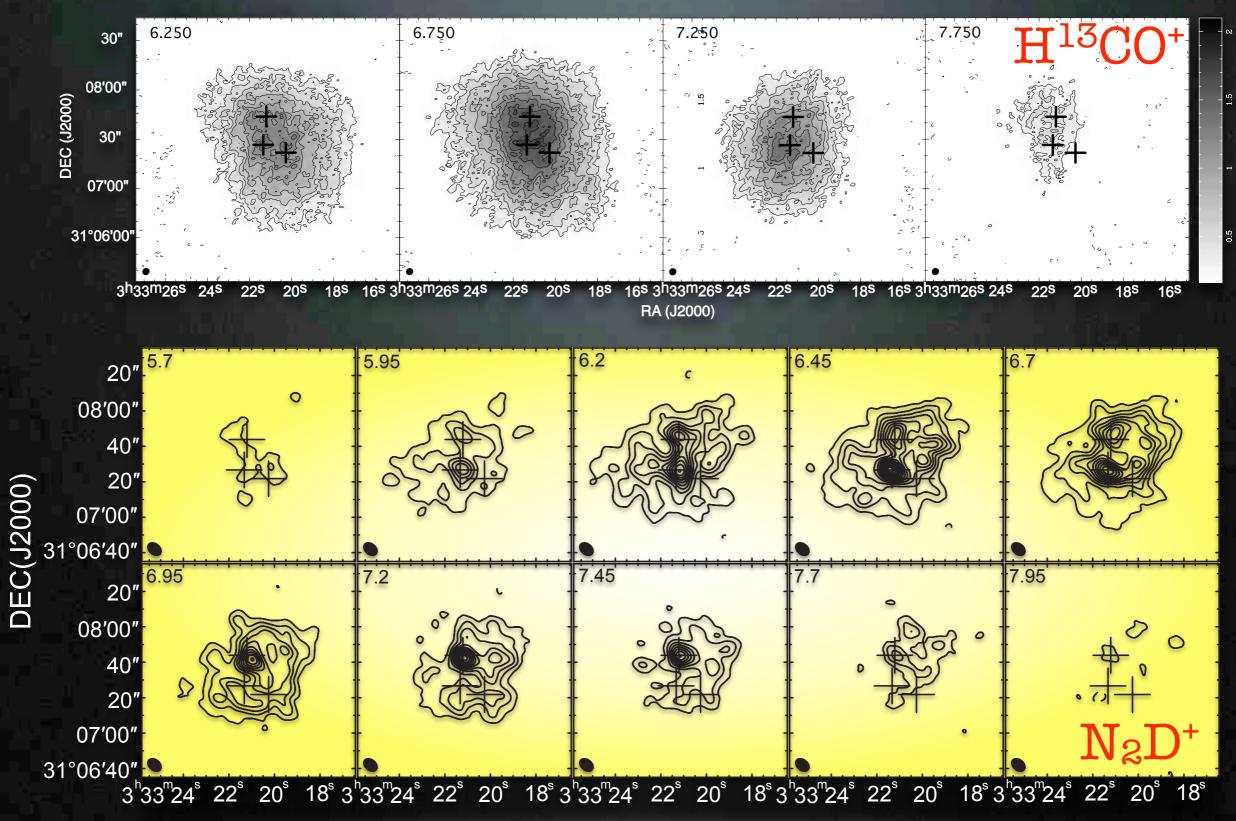


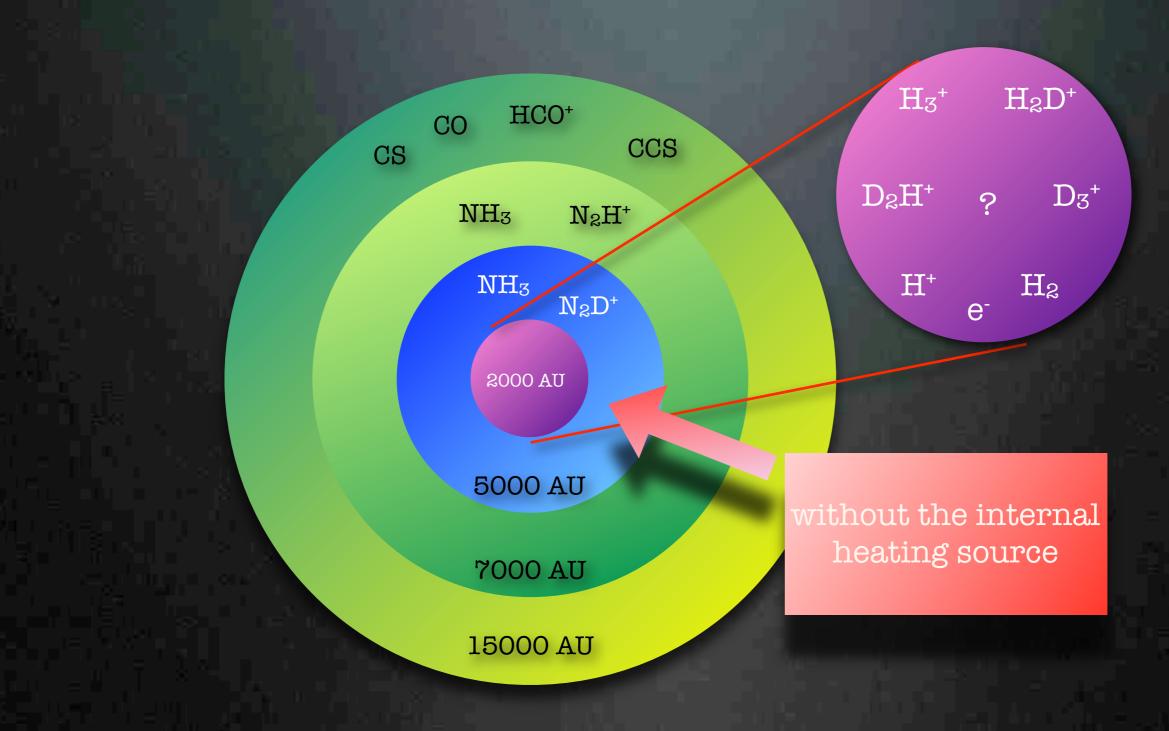


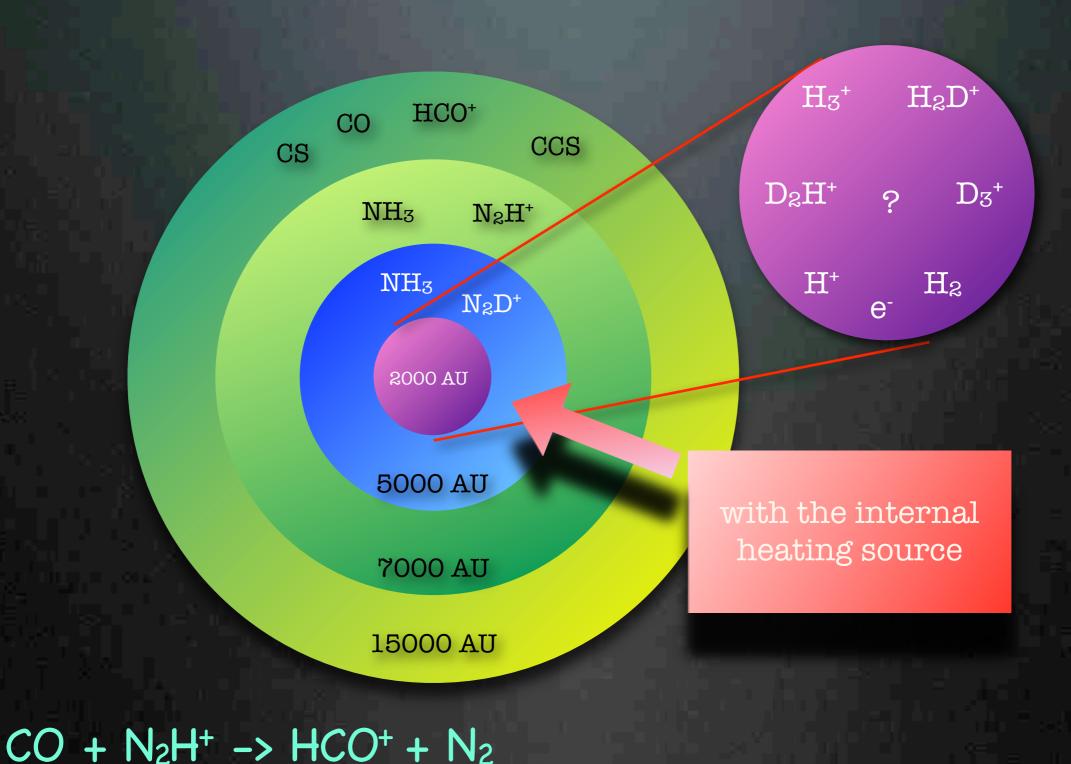
Barnard 1-b



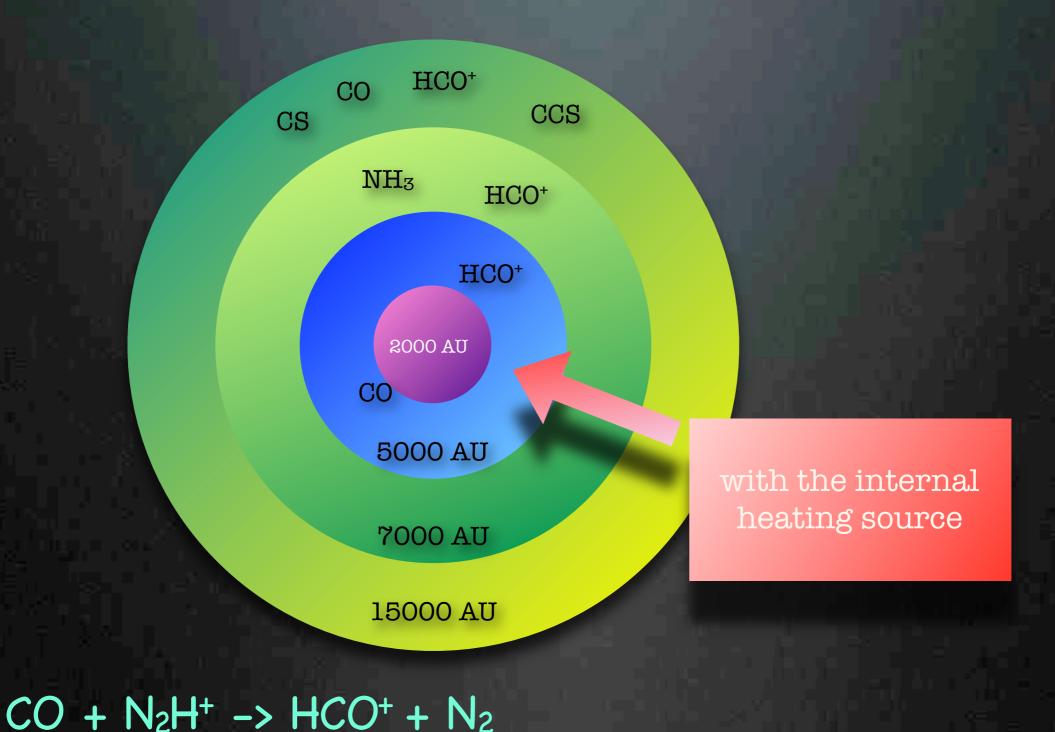




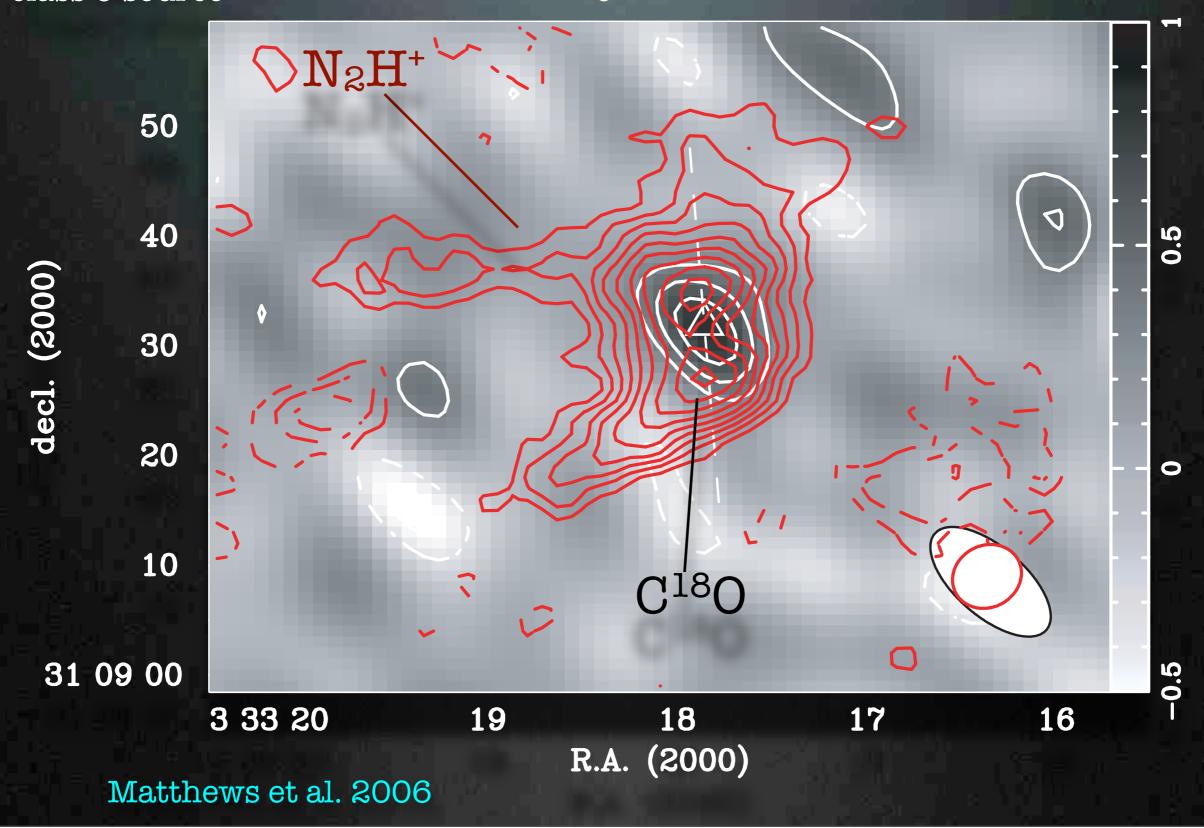




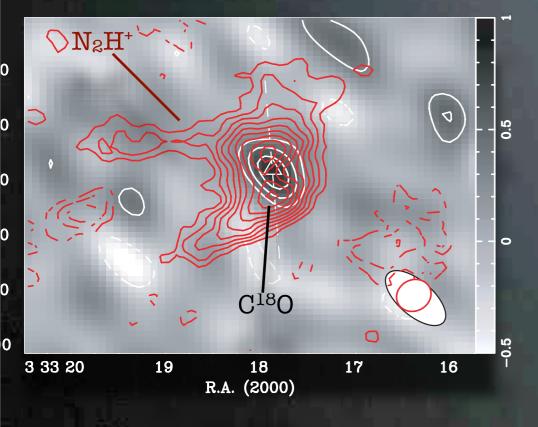
Wednesday, September 16, 2009



About Deeply Embedded Young Stellar Barnard 1-c class 0 source Objects

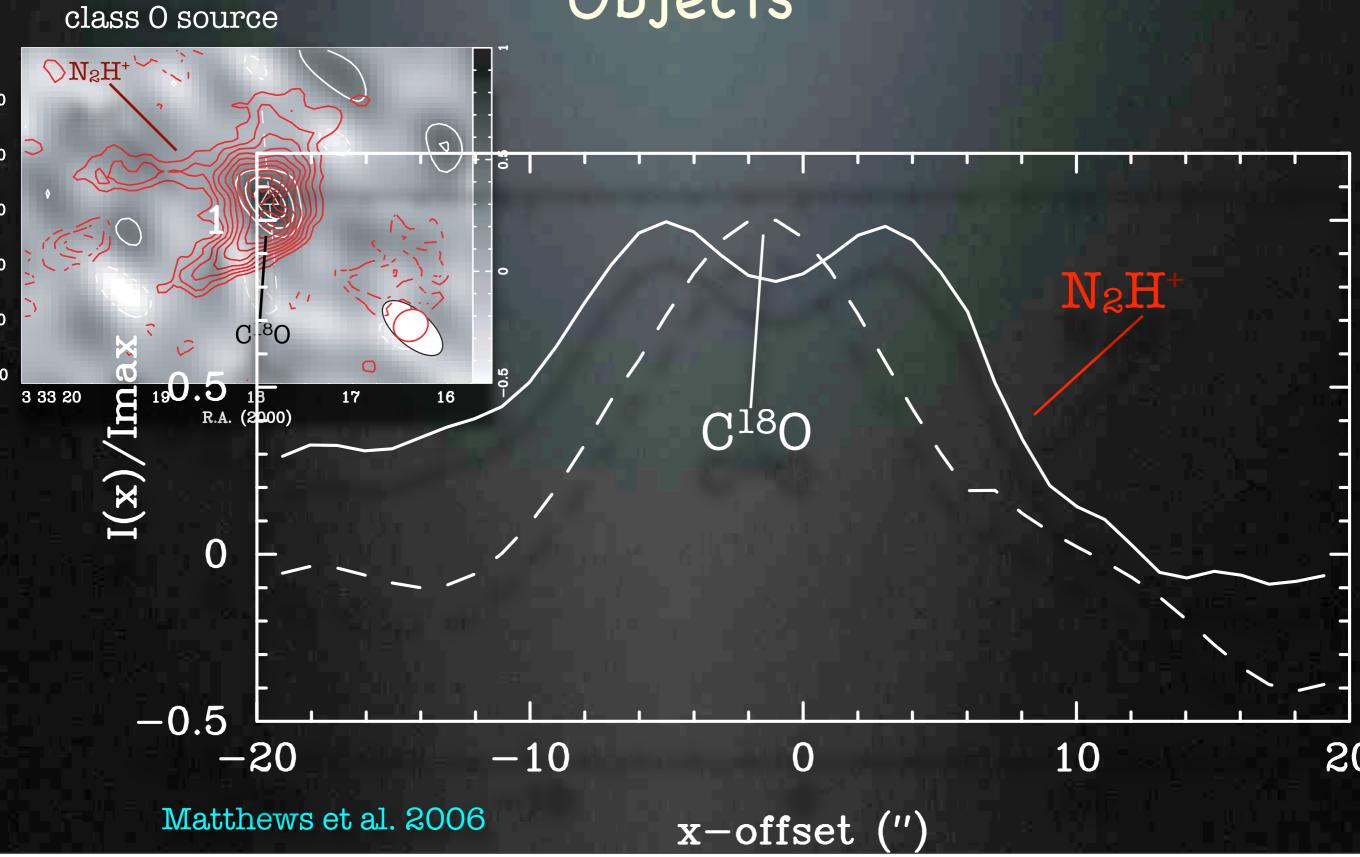


About Deeply Embedded Young Stellar Barnard 1-c class 0 source Objects

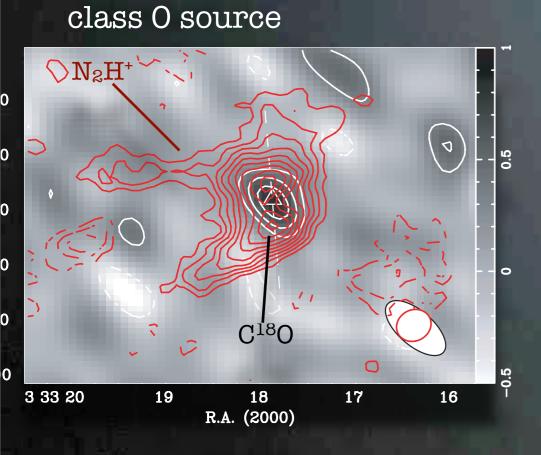


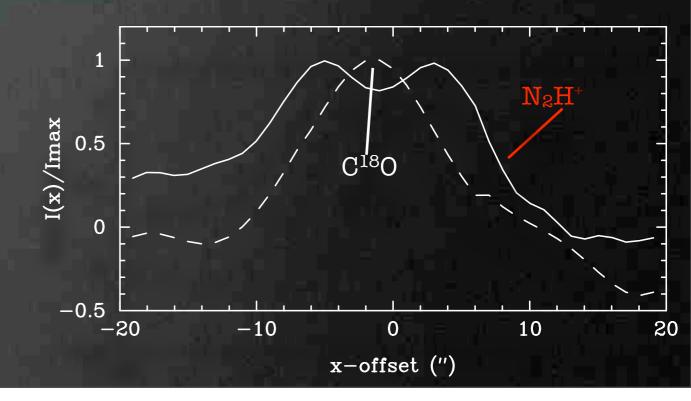
Matthews et al. 2006

About Deeply Embedded Young Stellar Barnard 1-c Class O source Objects



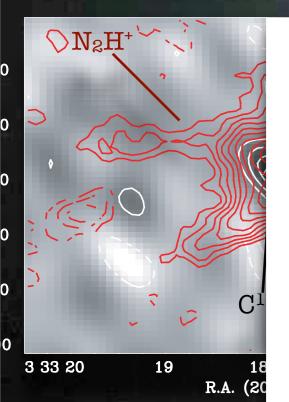
About Deeply Embedded Young Stellar Barnard 1-c Class O source Objects

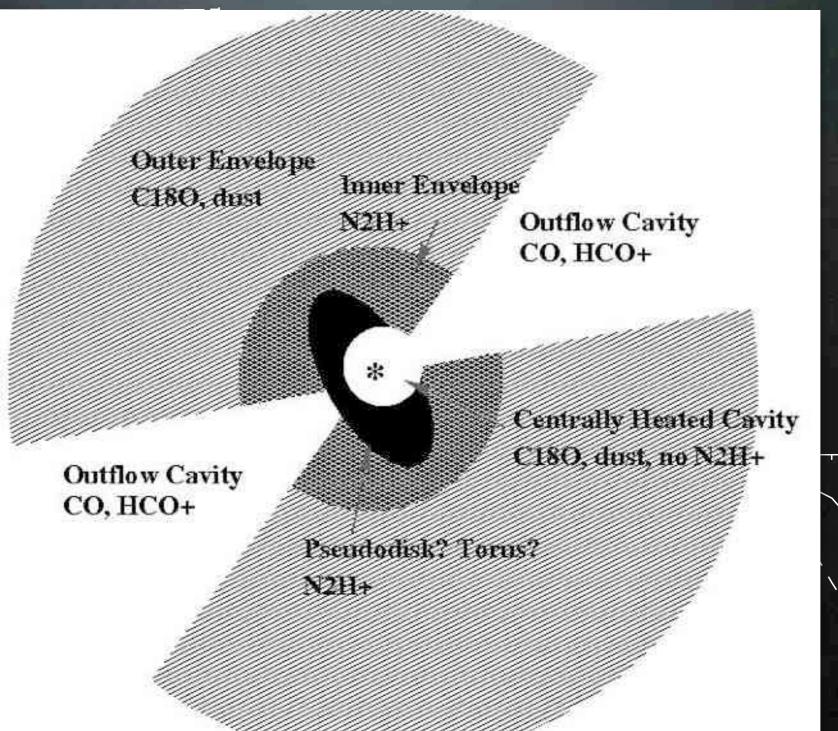




Matthews et al. 2006

About Deeply Embedded Young Stellar Barnard 1-c class 0 source Objects

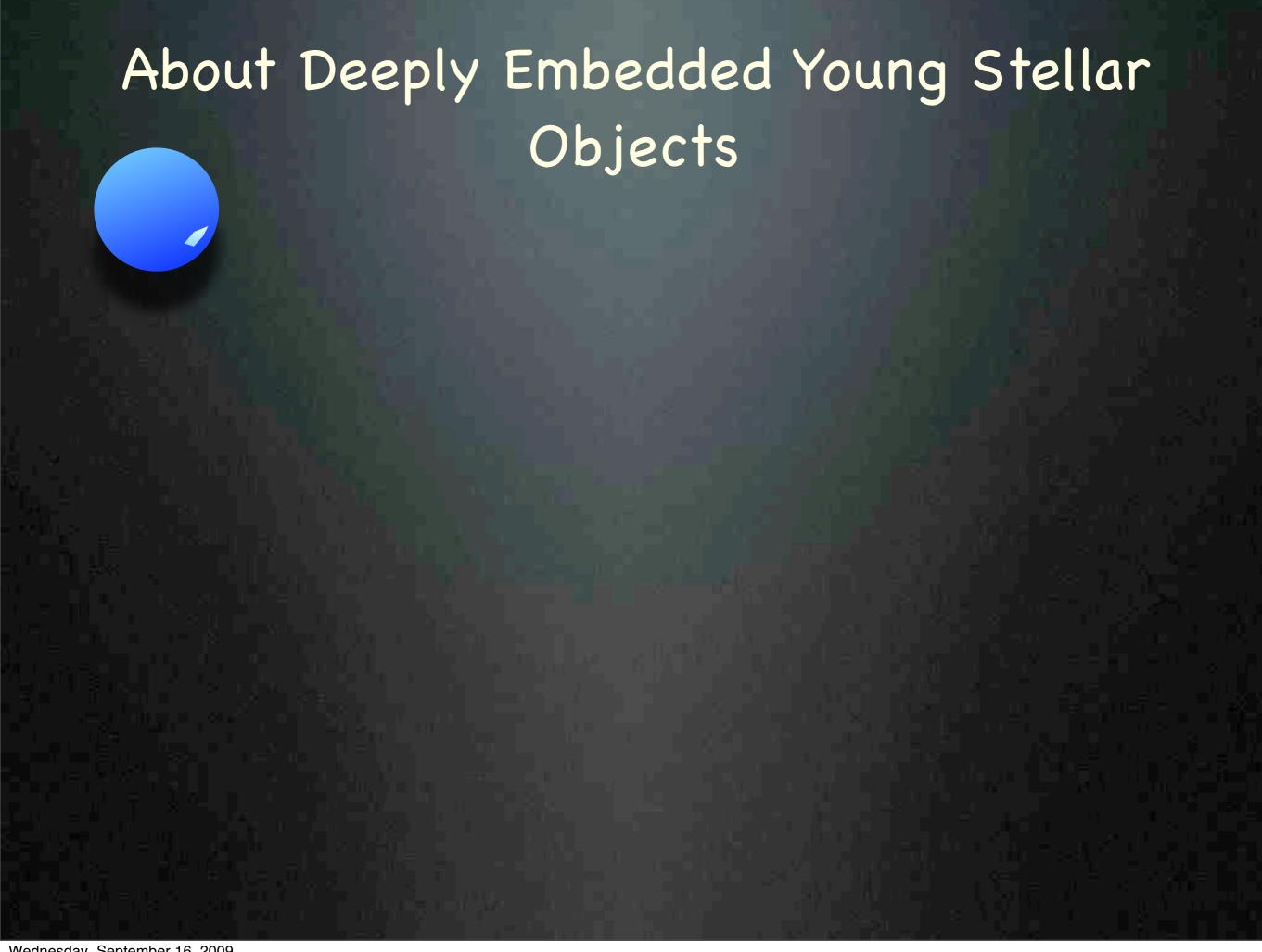




N₂H⁺

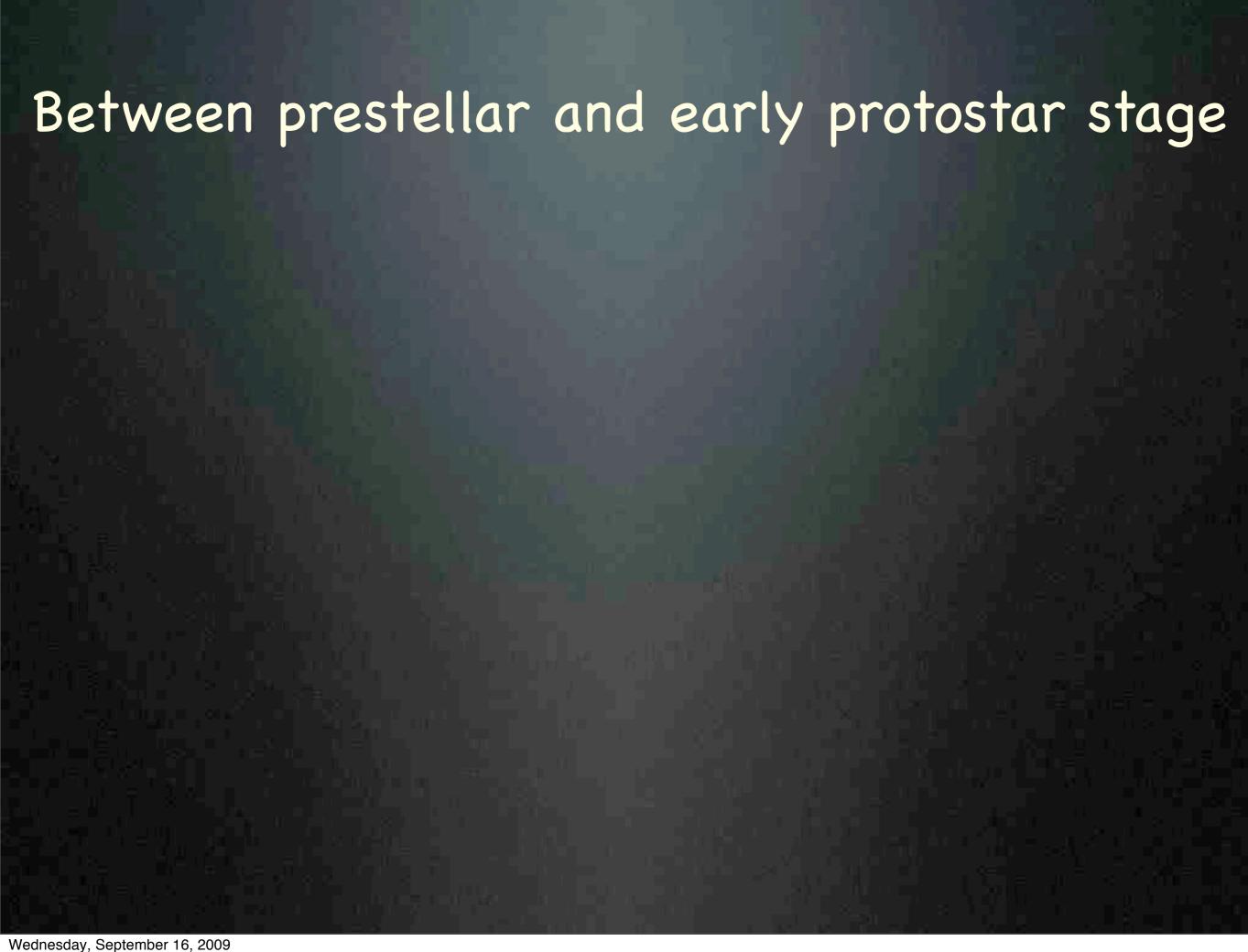
Matthews et al. 2006

x-offset (")

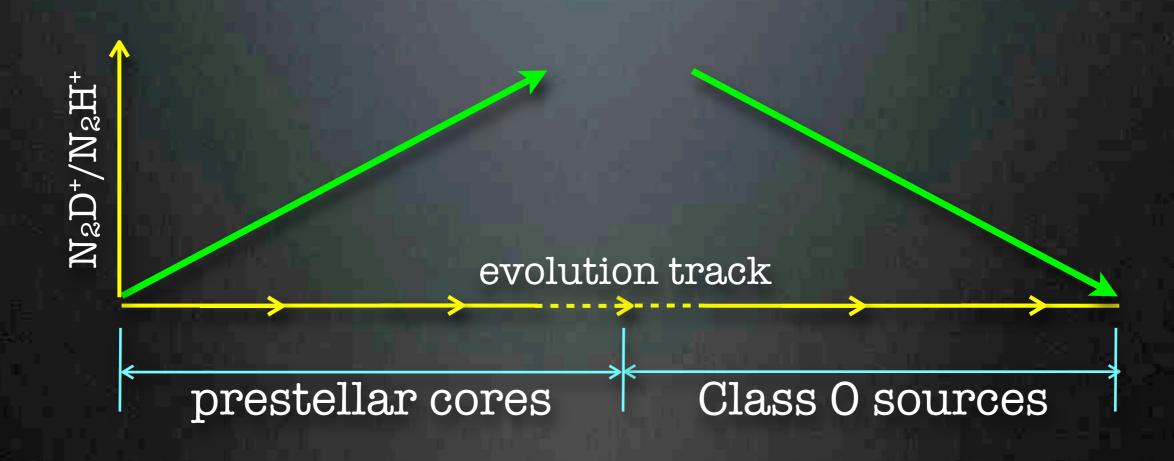


1. The gas is heated by the collisions with the warm dust. This implies that within r < 60 AU of the young star, the infall gas is heated to 100 K, resulting in the sublimation of $\frac{1}{100}$ -rich ices into the gas.

- 1. The gas is heated by the collisions with the warm dust. This implies that within r < 60 AU of the young star, the infall gas is heated to 100 K, resulting in the sublimation of $\frac{1}{100}$ or ich ices into the gas.
- 2.In addition, once the gas is heated to 200-300 K, the gas-phase chemical reaction convert O and H₂, resulting in high abundances of H₂O in the inner 10-100 AU.



Between prestellar and early protostar stage



Between prestellar and early protostar stage

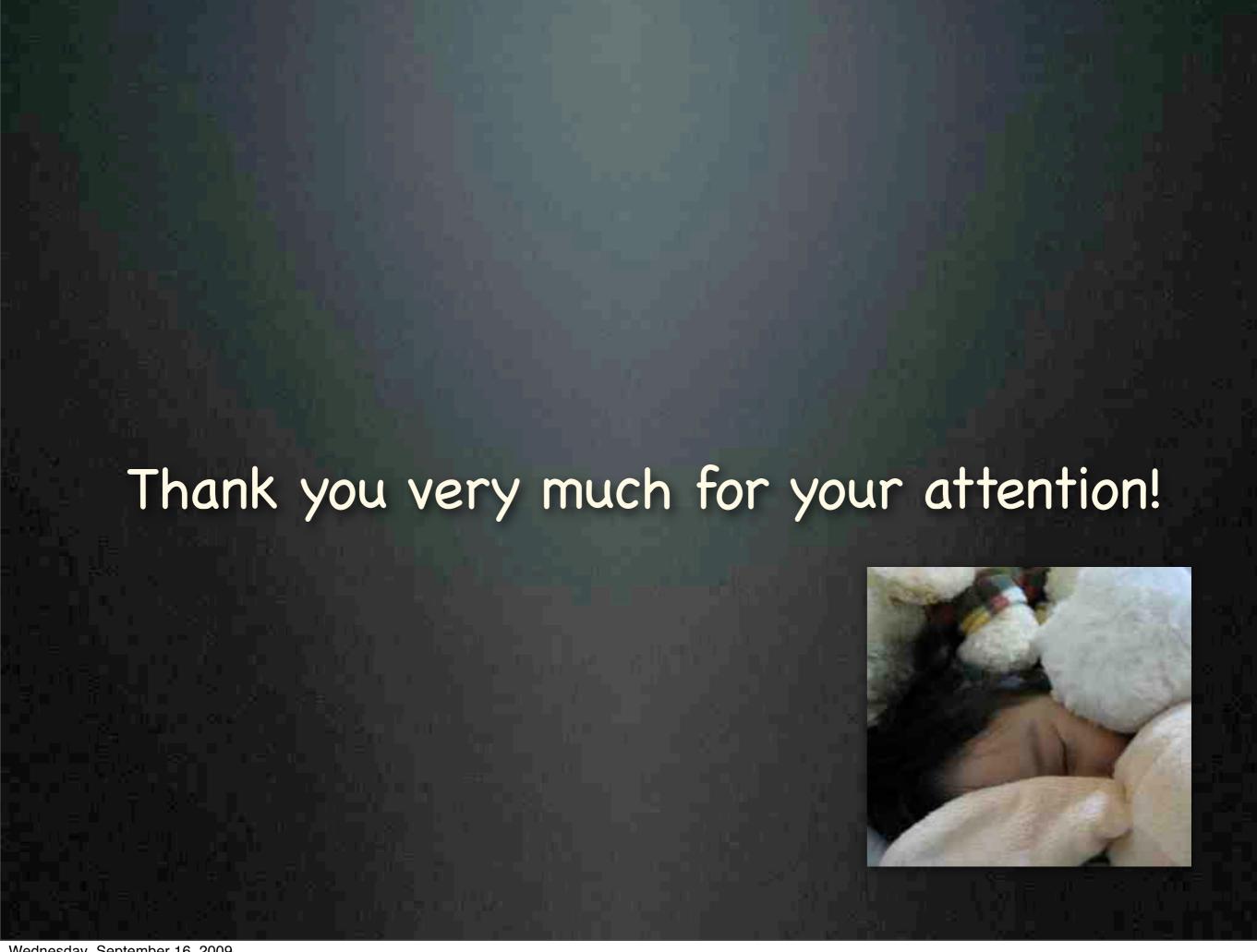
Therefore, the understanding of chemistry lets us to study:

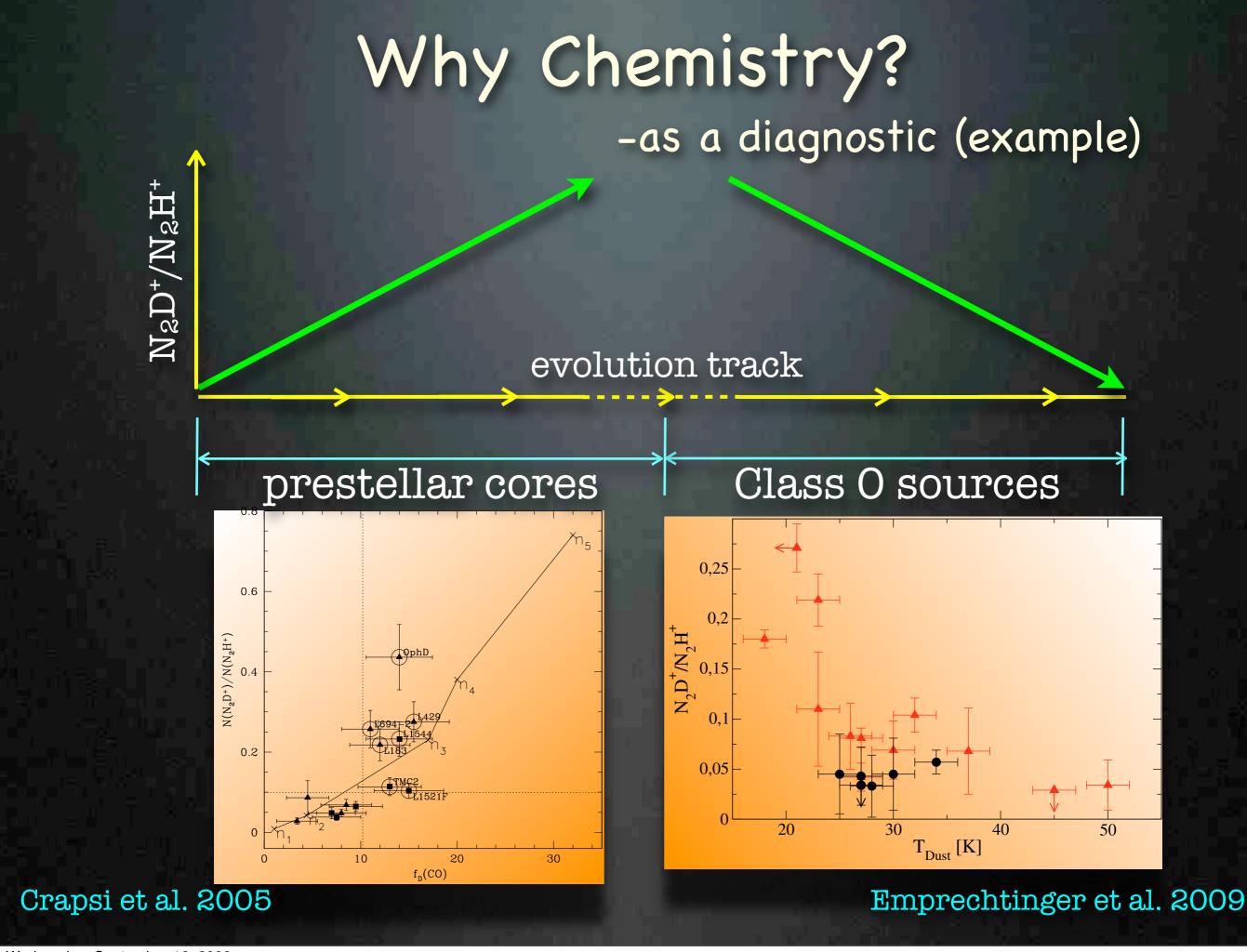
- 1. the initial condition of the star formation
- 2. the physical condition and kinematics of different sources with different evolutionary stages.

Future

Higher angular resolution observations (lower beam dilution and good resolution) can not only help us to understand the chemistry properties itself more, but also help us to understand the physical condition around the star formation in detail.

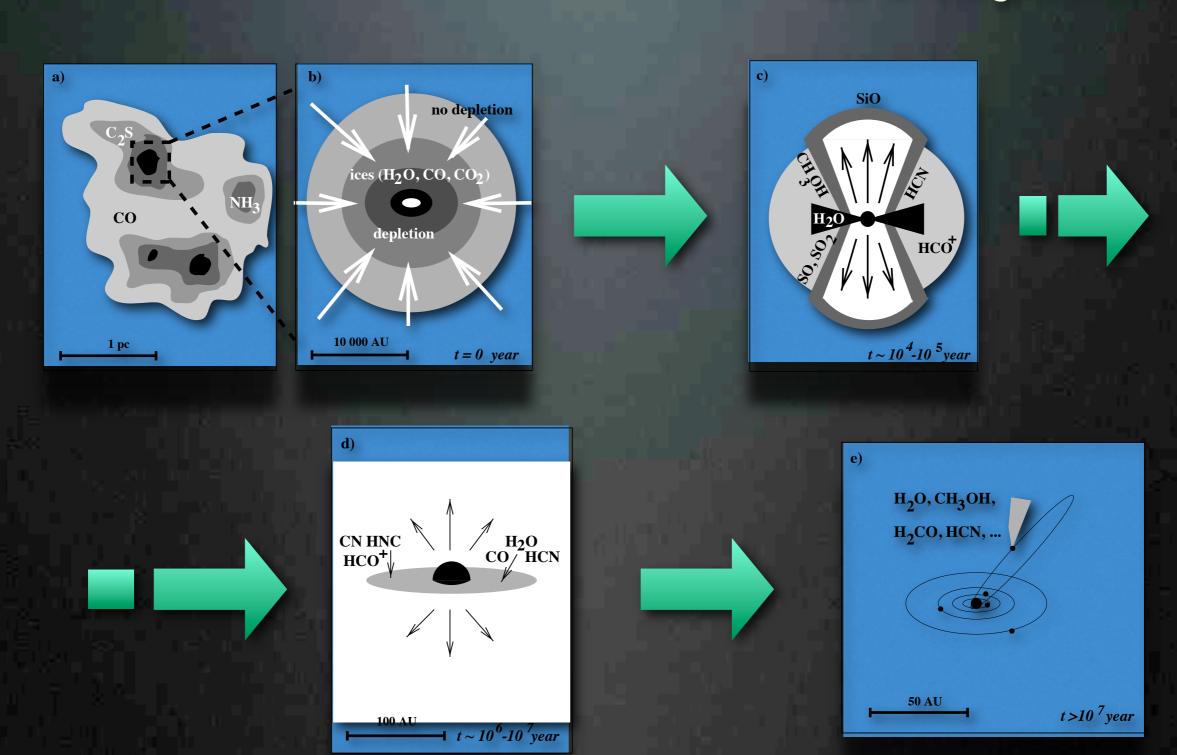






Why Chemistry?

-as a diagnostic

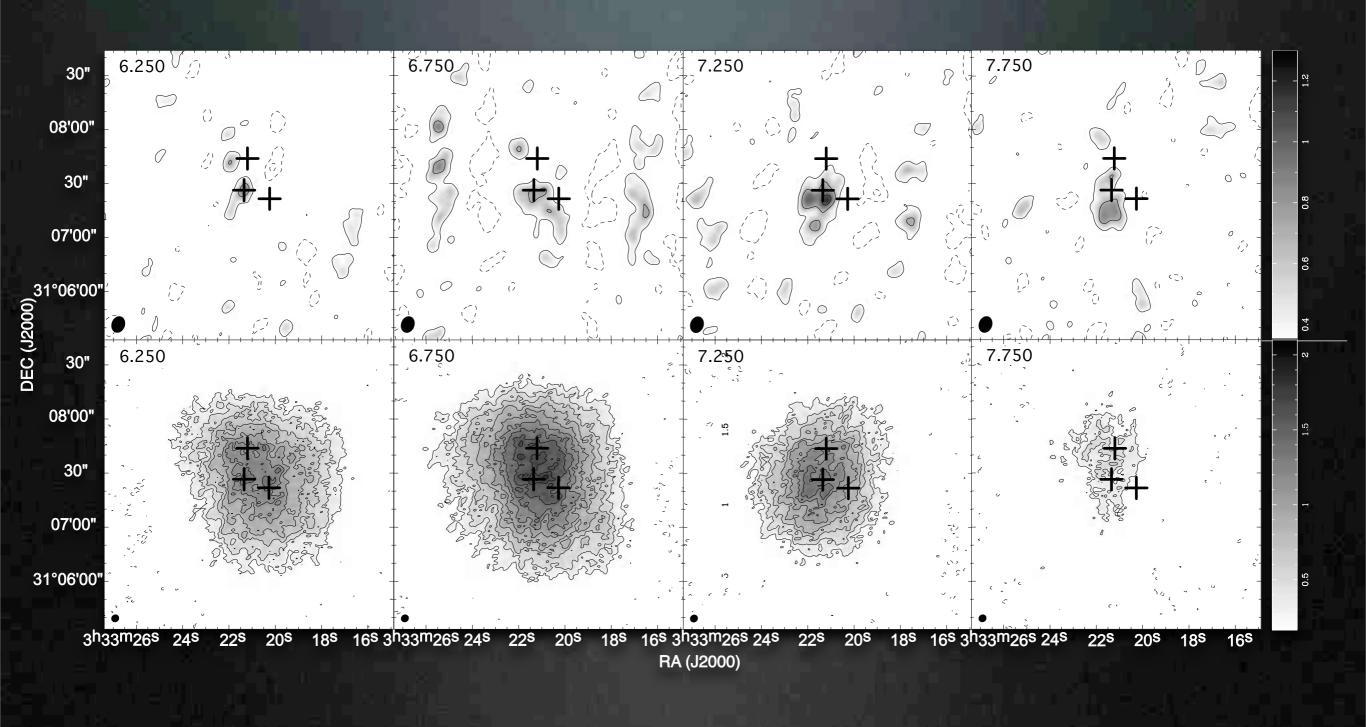


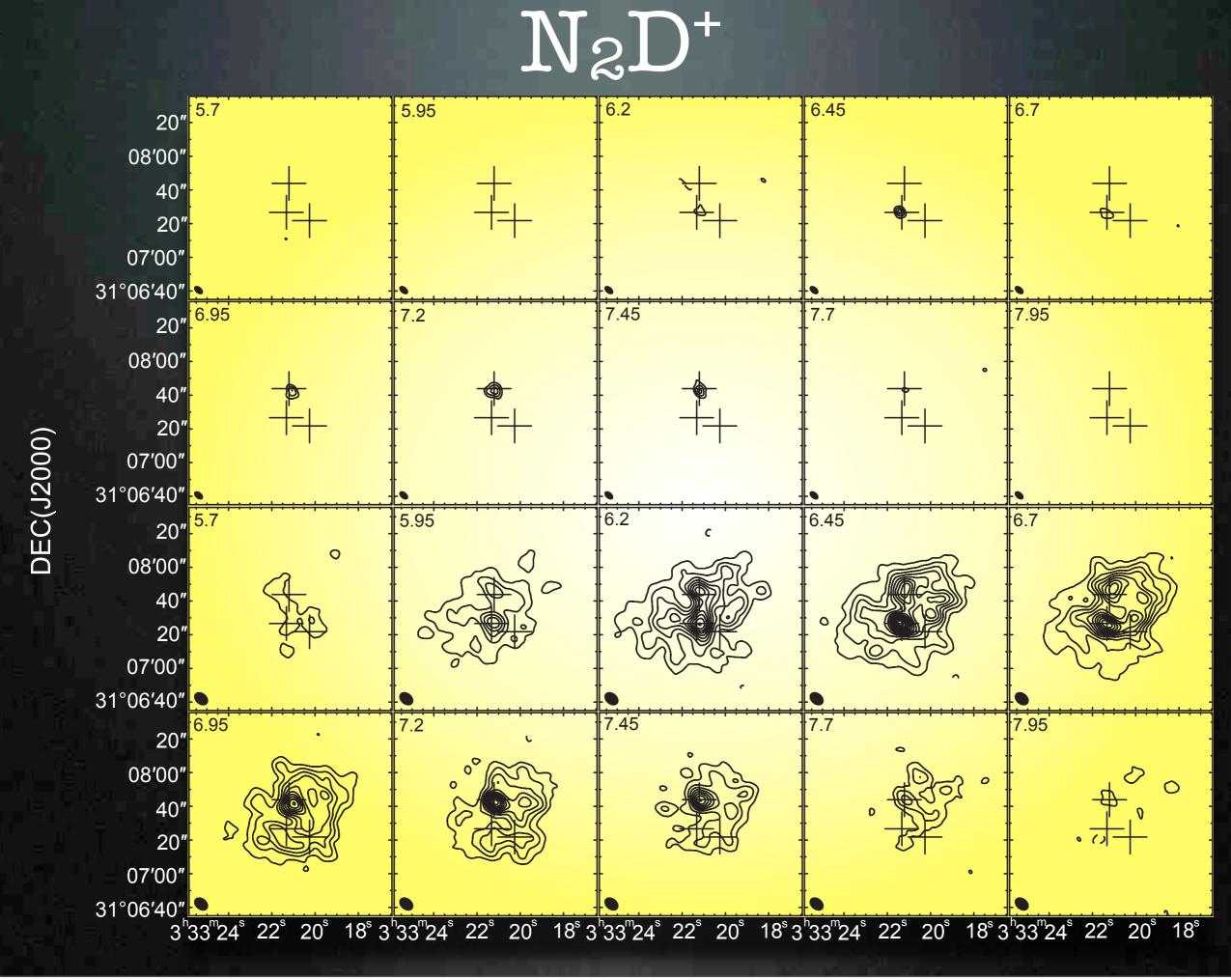
van Dishoeck & Blake 1998

Increased deuteration due to CO depletion

- CO depletion has profound consequences in core chemistry
 - triggers a number of second-order effects
- Deuterium fractionation of molecules is driven by $H_3^+ + HD \iff H_2D^+ + H_2 + 230 \text{ K}$
- At low temperature (e.g., 10 K), H₂D⁺ is enhanced Deuterium is passed down to other species such DCO, DCN
- If no CO depletion
 - $\overline{H_2D^+}$ abundance is limited by CO destruction (+e) -D enrichment of order of 1-10 %
- If CO depletion (and low e)
 - H_2D^+ is further enhanced, which further enhances N_2D^+ , NH_2D , etc.

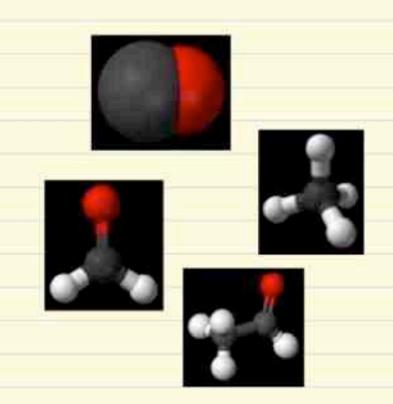
H¹³CO⁺





Fundamentals of Interstellar Chemistry

村福君 Du, FUJUN



References:

[2] A.G.G.M. Tielens 2005, The physics and Chemistry of the Interstellar Medium

IMPRS Retreat

THE SUNYAEV-ZEL'DOVICH EFFECT

Xun Shi Felipe Navarrete Brenda Miranda



Outline



1. Introduction

- 2. The physics of the Sunyaev-Zel'dovich effect
- 3. Measurement techniques
- 4. Astrophysical applications of SZ effect

1. Introduction: Astrophysical Context

Inverse-Compton scattering

High energy: synchrotron self-Compton process

(AGN's)

Low energy: SZ effect

(Any reservoir of hot plasma)



- 1. Cosmological probe
- 2. Study the gas properties of galaxy clusters
- 3. Study the evolution of structure in the Universe
- 4. Redshift independent

1. Introduction: CMBR

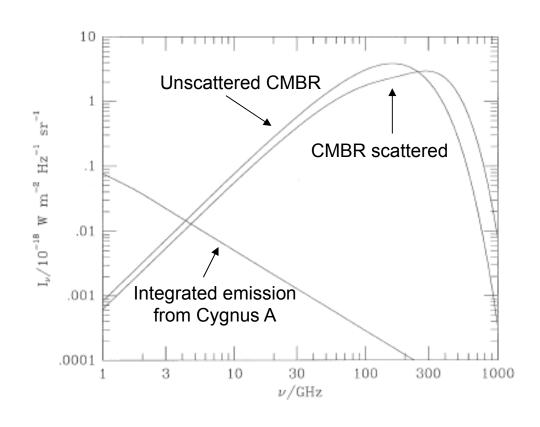
Cosmic Microwave Background Radiation (CMBR)

- Isotropic
- T_{rad} ~ 2.725 K
- Specific intensity

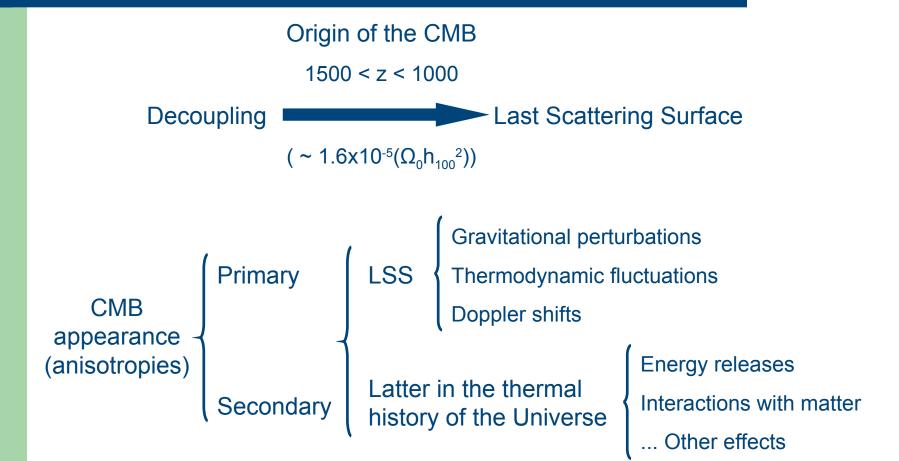
$$I_{v} = \frac{2hv^{3}}{c^{2}} (e^{hv/k_{B}T_{rad}} - 1)^{-1}$$

• *v_{max}* ~ 160 GHz

 $\lambda_{max} \sim 1.9 \text{ mm}$



1. Introduction: CMBR



1. Introduction: Galaxy clusters and the CMBR

Basic physic of the Sunyaev-Zel'dovich effect

Cluster of galaxies: $M \sim 3x10^{14} M_{sol}$, $R_{eff} \sim Mpc$. In hydrostatic equilibrium, T_e

Electrons scatter photons of the CMBR (low energy scattering):

Thomson cross-section σ_{τ} and Optical depth τ $\approx n_{a}\sigma_{\tau}R_{eff} \sim 10^{-2}$

Mean change of photon energy per scattering: $\Delta v / v \approx (k_B T_a / m_a c^2) \sim 10^{-2}$

Overall change in brightness of the CMBR ~ 10⁻⁴

Primordial effects:

non-localized not associated with structures at others wave bands

Detectable!! ... but distinguishable?

SZ effects:

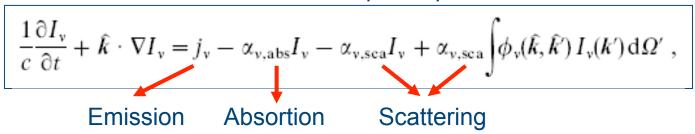
localized seen towards structures visible in the optical and X-ray band

2. The physics of the SZ effect: Outline

- Radiation basics
- Inverse-Compton scattering
- Sunyaev-Zel'dovich effect in three flavors:
 - * Thermal SZ effect
 - * Non-thermal SZ effect
 - * Kinematic SZ effect

2. The physics of the SZ effect: Radiation Basics

Radiative transport equation



Description by means:

• Photon distribution function or the occupation number:

$$f_{\alpha}(\mathbf{r}, \mathbf{p}, t) = h^{-3} n_{\alpha}(\mathbf{r}, \mathbf{p}, t)$$

(Statistical mechanics of photons)

• Specific intensity and Brightness temperature:

temperature:
$$I_{\rm v}(\hat{k},r,t)=\sum_{\alpha=1}^2 \left(\frac{h^4v^3}{c^2}\right)\!f_{\alpha}\!(r,\!p,t)\;,$$

$$T_{\rm RJ}\!(v)=\frac{c^2I_{\rm v}}{2k_{\rm B}v^2}\;.$$

(Astrophysical work)

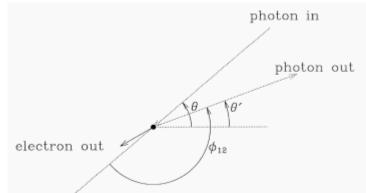
Inverse-Compton emission step by step:

- a. Effect of a single photon-electron scattering
- b. Scattering of photons by an electron population
- c. Effect on radiation spectrum
 - c1. The Kompaneets approximation

a. Single photon-electron scattering

Compton scattering formula:

$$\varepsilon' = \frac{\varepsilon}{1 + (\varepsilon/m_{\rm e}c^2)(1 - \cos\phi_{12})},$$



The probabily that a single scattering of a photon causes a frequency shift s=log(v "/v) from an electron with speed v $_{\rm e}$ = β $_{\rm e}$

$$P(s; \beta) ds = \int p(\mu) d\mu \, \phi(\mu'; \mu) \left(\frac{d\mu'}{ds}\right) ds$$
.

$$p(\theta) d\theta = p(\mu) d\mu = (2\gamma^4 (1 - \beta \mu)^3)^{-1} d\mu$$

where:
$$\phi(\mu'; \mu) d\mu' = \frac{3}{8} (1 + \mu^2 \mu'^2 + \frac{1}{2} (1 - \mu^2) (1 - \mu'^2)) d\mu'$$

 $v'' = v (1 + \beta \mu') (1 - \beta \mu)^{-1}$ $\mu' = \cos \theta'$.

Then

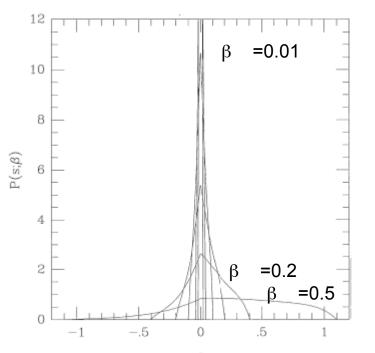
$$P(s;\beta) = \frac{3}{16\gamma^4\beta} \int_{\mu_1}^{\mu_2} (1+\beta\mu')(1+\mu^2\mu'^2 + \frac{1}{2}(1-\mu^2)(1-\mu'^2))(1-\beta\mu)^{-3} d\mu , (1)$$

Integrating ...

as β

Asymmetry **1**by relativistic beaming

Width f because s for a given photon angular deflection



b. Scattering of photons by an electron population

Distribution of photon frequency shifts caused by a population of electrons:

$$P_1(s) = \int_{\beta_{\text{lim}}}^1 p_{\text{e}}(\beta) \, \mathrm{d}\beta \, P(s; \beta) \tag{2}$$

$$p_{e}(\beta \quad \text{): electron } \beta \quad \text{distribution} \\ \text{Power law (non-thermal)}$$

 $P(s;\beta)$: given by eq. (1), probability that a frequency shift s occur from a single scattering from an electron with speed

c. Effect on radiation spectrum

If every photon in the incident spectrum,

$$I_0(v) = \frac{2hv^3}{c^2} (e^{hv/k_B T_{\text{rad}}} - 1)^{-1}$$

Is scattered once, the resulting spectrum is given by

$$I(v) = \int_{-\infty}^{\infty} P_1(s) I_0(v_0) \, ds$$
 (3)

where $P_1(s)$, given by eq. (2), is the scattering kernel.

Then, the change in the radiation spectrum at frequency v is.

$$\Delta I(v) \equiv I(v) - I_0(v) = \frac{2h}{c^2} \int_{-\infty}^{\infty} P_1(s) \, ds \left(\frac{v_0^3}{e^{hv_0/k_B T_{\text{rad}}} - 1} - \frac{v^3}{e^{hv/k_B T_{\text{rad}}} - 1} \right)$$
 (4)

The generalization of equation (3) for an arbitrary optical depth:

$$I(v) = \int_{-\infty}^{\infty} P(s) I_0(v_0) ds \quad (5)$$

where P(s) is the redistribution function after n scatterings

$$P(s) = e^{-\tau_e} \left(\delta(s) + \tau_e P_1(s) + \frac{1}{2!} \tau_e^2 P_2(s) + \cdots \right)$$

For an optically thin medium, with $\tau_e <<1$ $P(s) = (1 - \tau_e) \delta(s) + \tau_e P_1(s)$

The resulting intensity change:

$$\Delta I(v) = \frac{2h}{c^2} \tau_e \int_{-\infty}^{\infty} P_1(s) \, ds \left(\frac{v_0^3}{e^{hv_0/k_B T_{rad}} - 1} - \frac{v^3}{e^{hv/k_B T_{rad}} - 1} \right)$$
 (6)

c1. The Kompaneets approximation: non-relativistic limit for a scattering process

$$\frac{\partial n}{\partial y} = \frac{1}{x_{\rm e}^2} \frac{\partial}{\partial x_{\rm e}} x_{\rm e}^4 \left(\frac{\partial n}{\partial x_{\rm e}} + n + n^2 \right)$$

where $x_e = h_V / k_B T_e$ and,

$$y = \frac{k_{\rm B}T_{\rm e}}{m_{\rm e}c^2} \frac{ct}{\lambda_{\rm e}} = \int n_{\rm e} \, \sigma_{\rm T} \, \mathrm{d}l \frac{k_{\rm B}T_{\rm e}}{m_{\rm e}c^2}$$

The resulting spectrum can be written,

$$I(v) = \int_{-\infty}^{\infty} P_{K}(s) I_{0}(v_{0}) ds$$
 where $P_{K}(s) = \frac{1}{\sqrt{4\pi y}} \exp\left(-\frac{(s+3y)^{2}}{4y}\right)$

The spectral change caused by scattering,

$$\Delta n = x y \frac{e^{x}}{(e^{x} - 1)^{2}} (x \coth(x/2) - 4)$$

$$\Delta I(x) = x^{3} \Delta n(x) I_{0}$$

$$I_{0} = (2h/c^{2})(k_{B}T_{rad}/h)^{3}$$

2. The physics of the SZ effect: Thermal SZ effect

Produce by interaction of the CMB photons with electrons that have high energy due to their temperature. Likely sites to occur:

- 1. the athmospheres of galaxy clusters,
- 2. the ionazed content of the Universe as a whole, and
- 3. the ionized gas close to us.

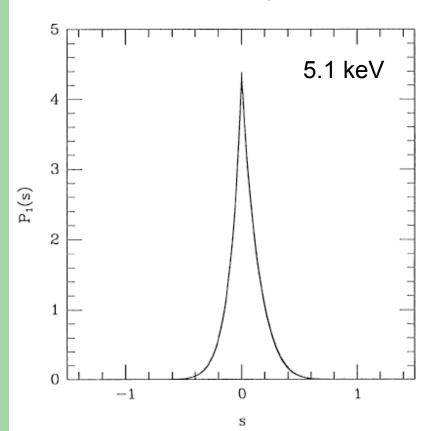
Assuming an electron relativistic Maxwellian distribution,

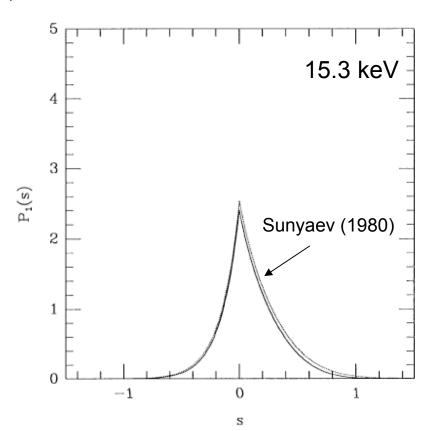
$$p_{e}(\beta) d\beta = \frac{\gamma^{5} \beta^{2} \exp(-\frac{\gamma}{\Theta}) d\beta}{\Theta K_{2}(\frac{1}{\Theta})}$$

where
$$\Theta = \left(\frac{k_{\rm B}T_{\rm e}}{m_{\rm e}c^2}\right)$$
 is the dimensionless electron temperature,

2. The physics of the SZ effect: Thermal SZ effect

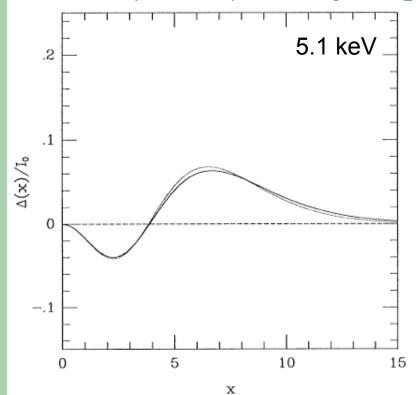
The obtained scattering kernel (eq. 2), $P_1(s)$, is shown for two temperatures

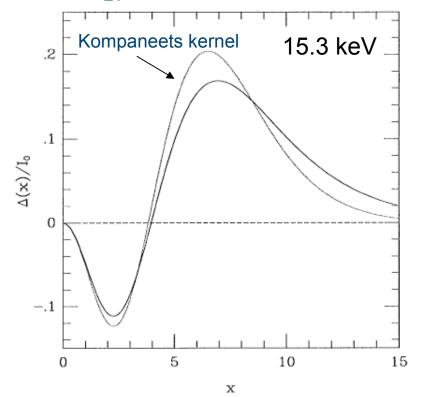




2. The physics of the SZ effect: Thermal SZ effect

Integrating eq. 4 using the $P_1(s)$ function shown previously, the change in the radiation spectrum (caused by a single scattering), looks like this:





2. The physics of the SZ effect: Non-thermal SZ effect

Caused by a non-thermal (relativistic) populations of electrons, found in:

- 1. cluster radio halo sources
- 2. radio galaxy lobes

For a power-law distribution of electrons energies:

$$p_{\mathbf{e}}(\gamma) \, \mathrm{d}\gamma = \begin{cases} A \, \gamma^{-\alpha} \, \mathrm{d}\gamma, & \gamma_1 \le \gamma \le \gamma_2 \\ 0, & \text{otherwise} \; . \end{cases}$$

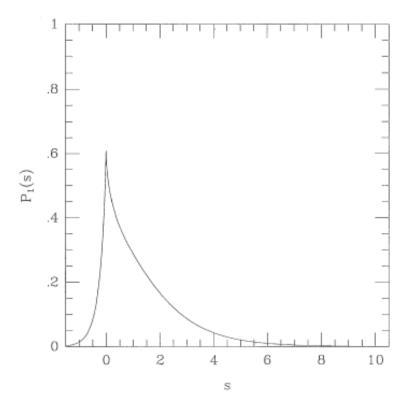
with a normalizing constant

$$A = \begin{cases} \log \gamma_2 - \log \gamma_1, & \alpha = 1 \\ (1 - \alpha)(\gamma_2^{1-\alpha} - \gamma_1^{1-\alpha})^{-1}, & \alpha \neq 1 \end{cases}$$

Abell 2163

2. The physics of the SZ effect: Non-thermal SZ effect

The scattering kernel, P1(s), for a power-law electron distribution with energy index α =2.5.

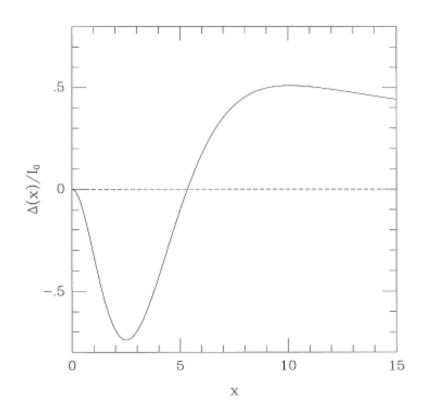


Upscattering tail much more prominent than in thermal case!

More electrons $\gamma >> 1$ in this distribution

2. The physics of the SZ effect: Non-thermal SZ effect

The fracctional spectral deformation caused by a single scattering

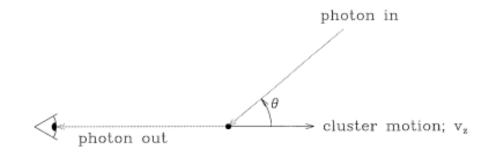


Similar in shape to the thermal case but with a deeper minimum and more extended tail

Thermal SZ effect dominates non-thermal SZ effect

2. The physics of the SZ effect: Kinematic SZ effect

The kinematic SZ effect arises if the scattering medium causing the thermal (or non-thermal) SZ effect is moving relative to the Hubble flow.



The change in specific intensity and brightness temperature produced are:

$$\Delta I = -\beta \tau_{\rm e} I_0 \frac{x^4 e^x}{(e^x - 1)^2}$$

$$\Delta T_{\rm RJ} = -\beta \tau_{\rm e} T_{\rm rad} \frac{x^2 e^x}{(e^x - 1)^2} \longrightarrow \frac{\Delta T_{\rm rad}}{T_{\rm rad}} \approx -\tau_{\rm e} \frac{v_z}{c}$$

Comparison with the magnitude thermal SZ effect:

$$\frac{\Delta T_{\text{kinematic}}}{\Delta T_{\text{thermal}}} = \frac{1}{2} \frac{v_z}{c} \left(\frac{k_B T_e}{m_e c^2}\right)^{-1} = 0.085 (v_z/1000 \text{ km s}^{-1}) (k_B T_e/10 \text{ keV})^{-1}$$

Thank you!!



Since 1972 when the Sunyaev-Zeldovich effect was proposed in a theoretical way many efforts have been carried out to detect it.

Techniques

- Single Dish
- Interferometers
- Bolometers

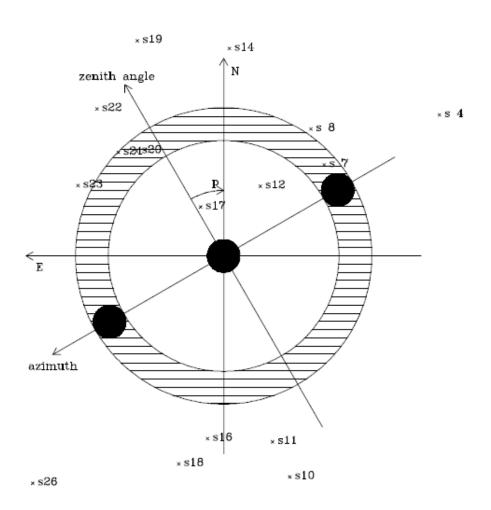
Single dish Radiometers

 Telescopes tend to have beam-sizes of few arcminutes at microwave frequencies. It is similar to the expected dimensions of galaxy clusters.

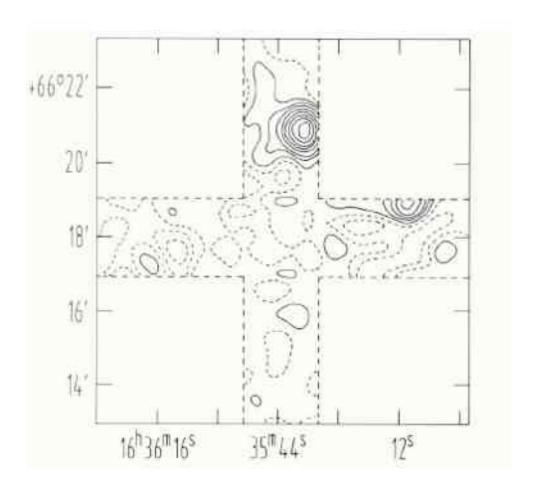
Problems:

 Radio source contamination, calibration and systematic errors introduced by the radiometer or spillover.

Observing



Uyaniker 1997 10.55Ghz



 $750 \pm 200 \, \mu K$

Interferometric

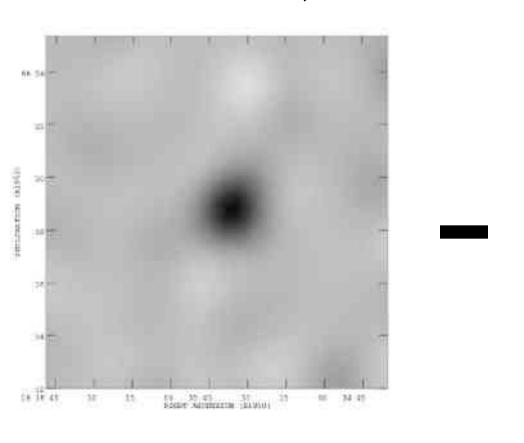
Combination of long and short baselines.

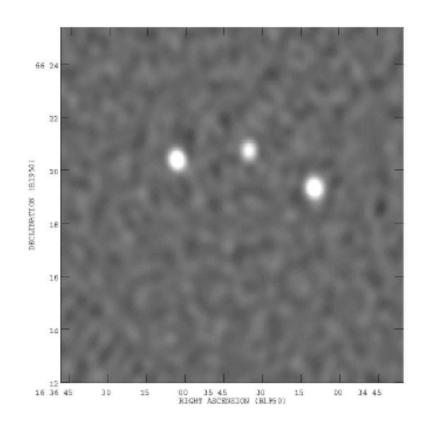
Long baselines identify individual sources (high resolution)

Short baselines mix all the signals.

•Solution:

Jones et al 1993, Abell 2218





Short Baselines: 18 m

 $-580 \pm 110 \mu Jy$

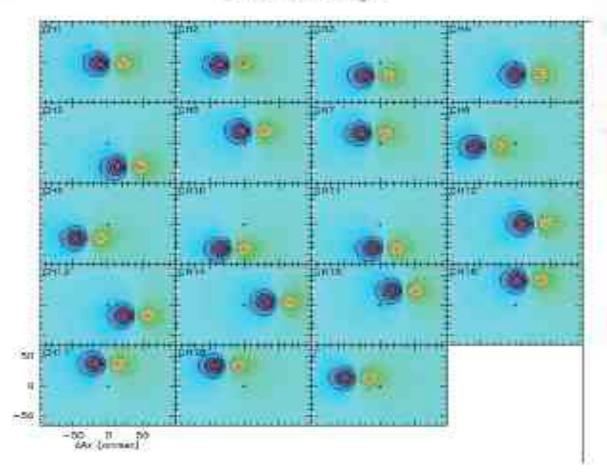
Long Baselines: 36-108 m

Bolometric

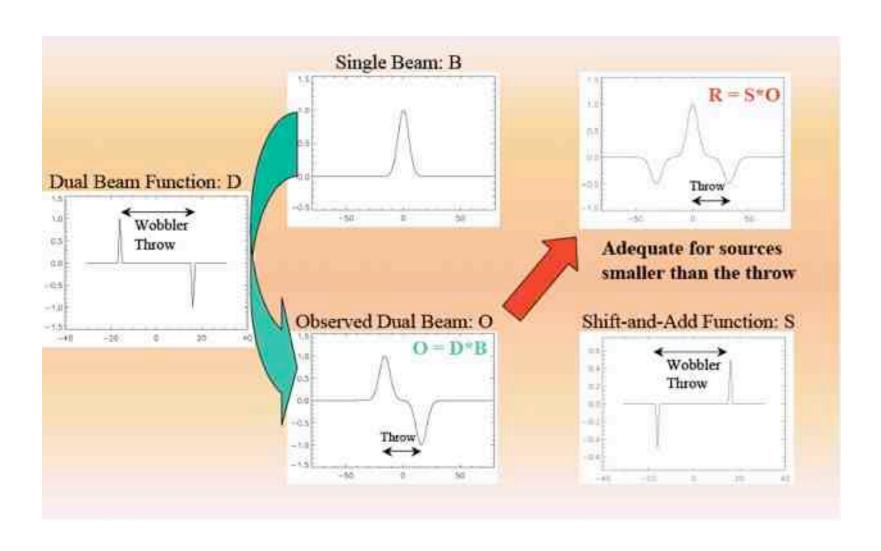
At frequencies higher than 100 GHz, coherent detectors reach their quantum noise limit due to the simultaneous photon position and frequency measurement uncertainty.

Incoherent detectors measure the integrated power of the incident radiation and do not retain any phase information. Due to their superior noise performance above 100 GHz, direct detectors are primarily used for CMB observations at high frequencies.

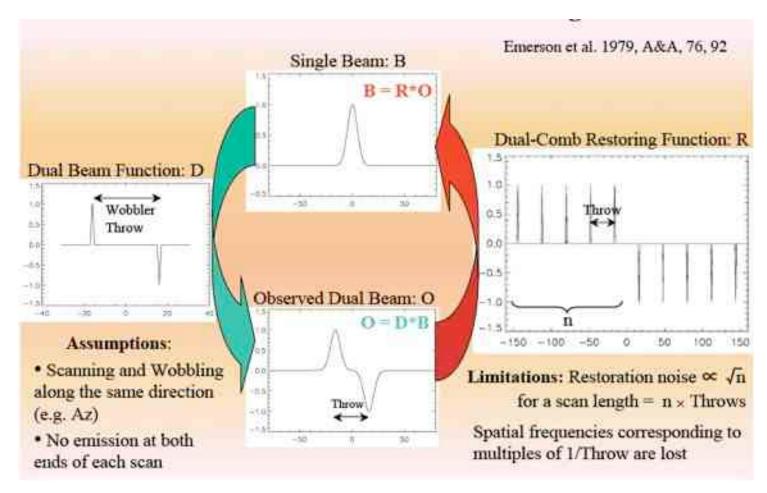
Dual-beam maps



Shift and Add

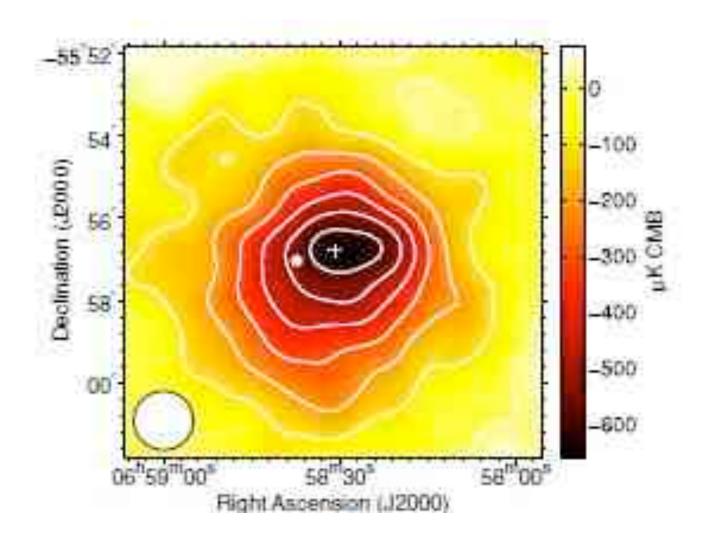


EHK



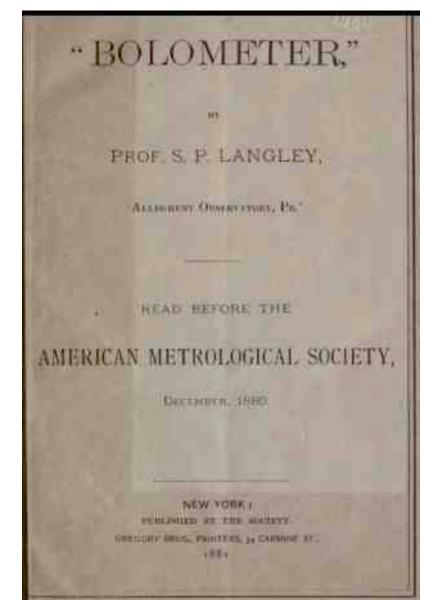
Deconvolve double beam

Convolve with telescope beam



Halverson et al. 2009

The evolution of the bolometer

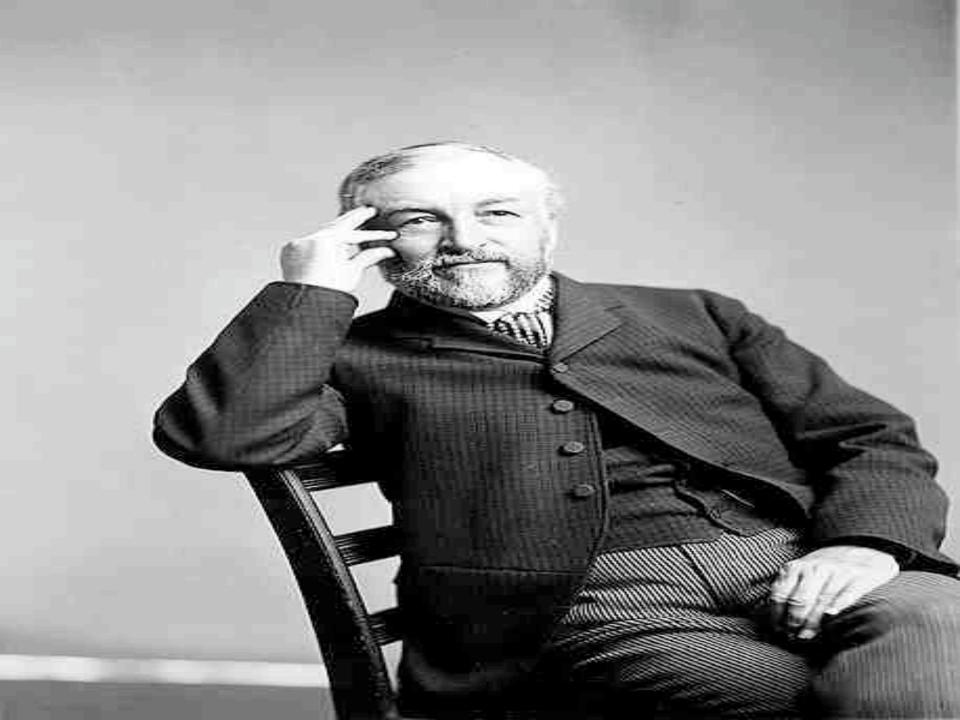




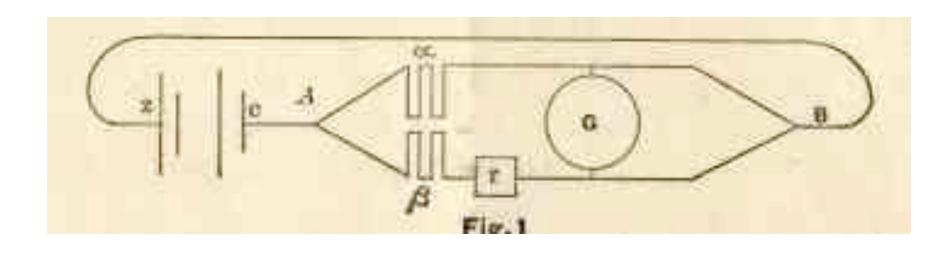
Our Hero



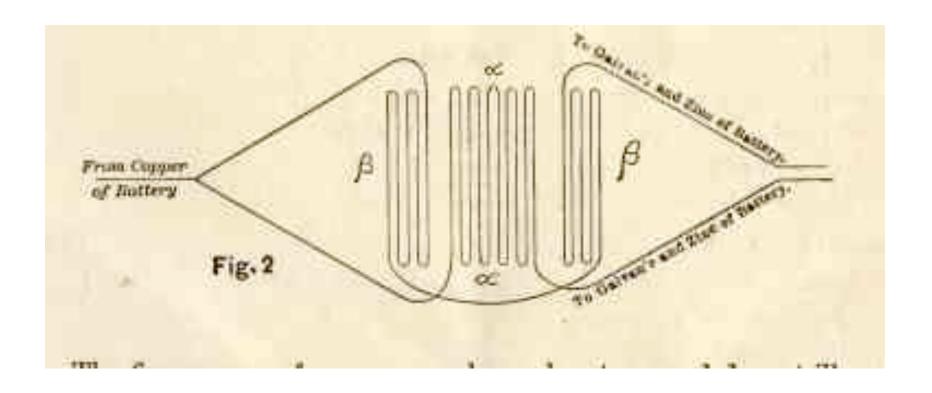
Samuel Langley (1834-1906)

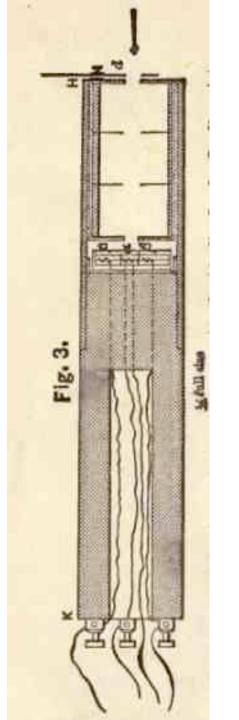


The First Bolometer (1878)



$$\vec{\tau} = \vec{\mu} \times \mathbf{B}$$







Wroblewski





Olszewski

"his investigations on the properties of the matterat low temperatures which lead, inter alia, to the production of liquid helium" Nobel Prize Committee, 1913



Liquid Helium (1908)

Superconductivity (1911)

Heike Kamerlingh

TES (Transition Edge Sensor) Bolometers

Super Conductor Curve

SQUID

